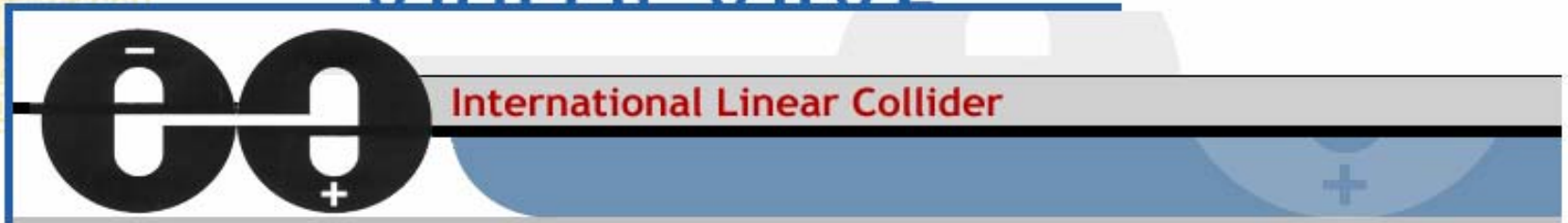


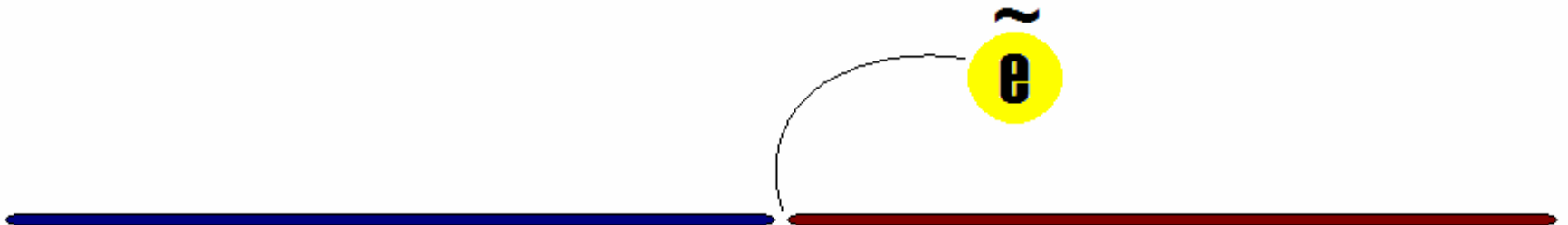


SANTA CRUZ



The Selectron Mass Resolution at the 1 TeV Linear Collider

Troy Lau
UC Santa Cruz
March 3 2005
SLAC





THE UC SANTA CRUZ GROUP

Bruce Schumm

Past

Sharon Gerbode (now at Cornell)
Heath Holguin (now a UCSC grad student)
Paul Mooser
Adam Pearlstein (now at Colorado State)

Present

Troy Lau (will be at ??)
Ayelet Lorberbaum
Joe Rose



Tools of the trade

LCDIsajet – SUSY event generation/simulation

Java Analysis Studio – event analysis, cuts

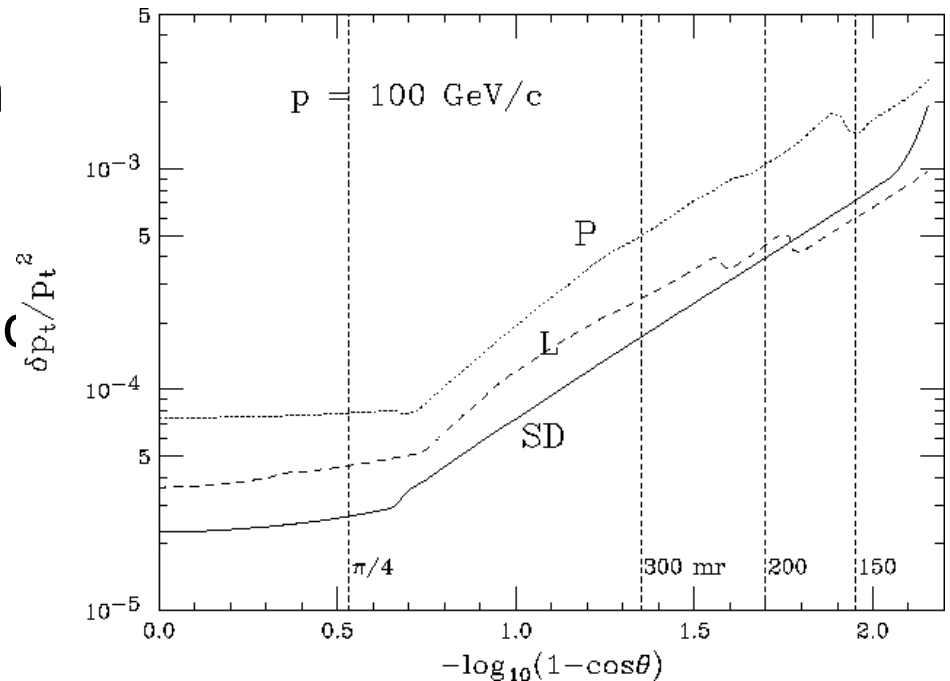
MATLAB – statistical analysis

Excel – in depth energy distribution investigation,
graphing



Motivation

To explore the effects of limited detector resolution on our ability to measure SUSY parameters in the **forward** ($\cos(\theta) > .8$) and central regions of the detector.

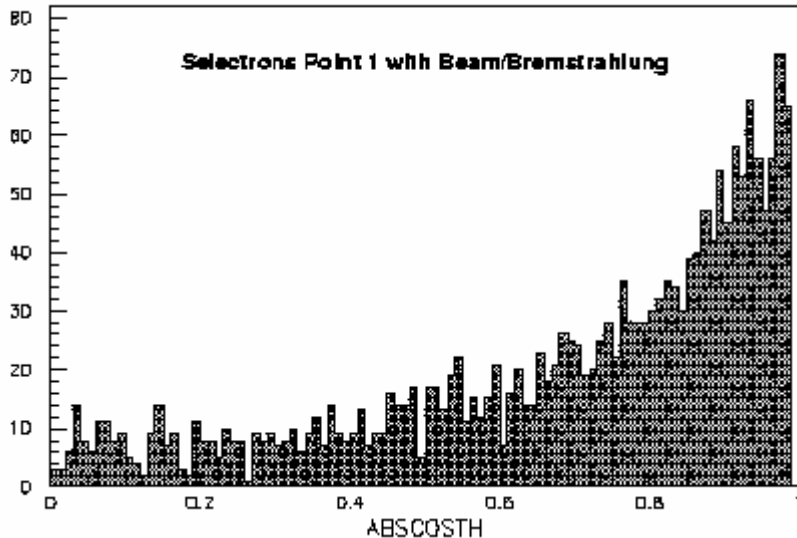




Why at 1 TeV ?

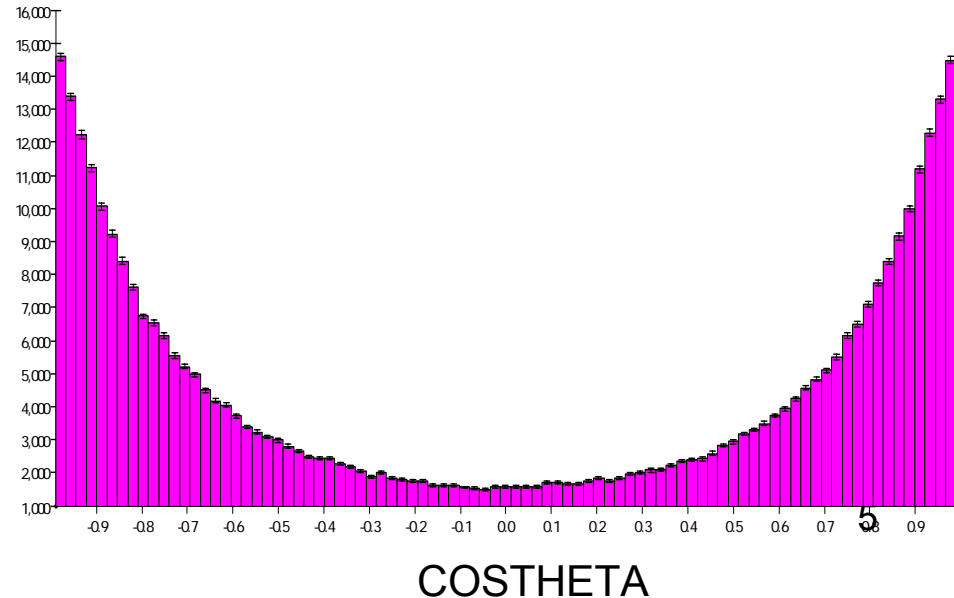
Selectron/electron production is peaked in the forward direction at 1 TeV for “low” mass selectrons.

right handed selectrons



electrons

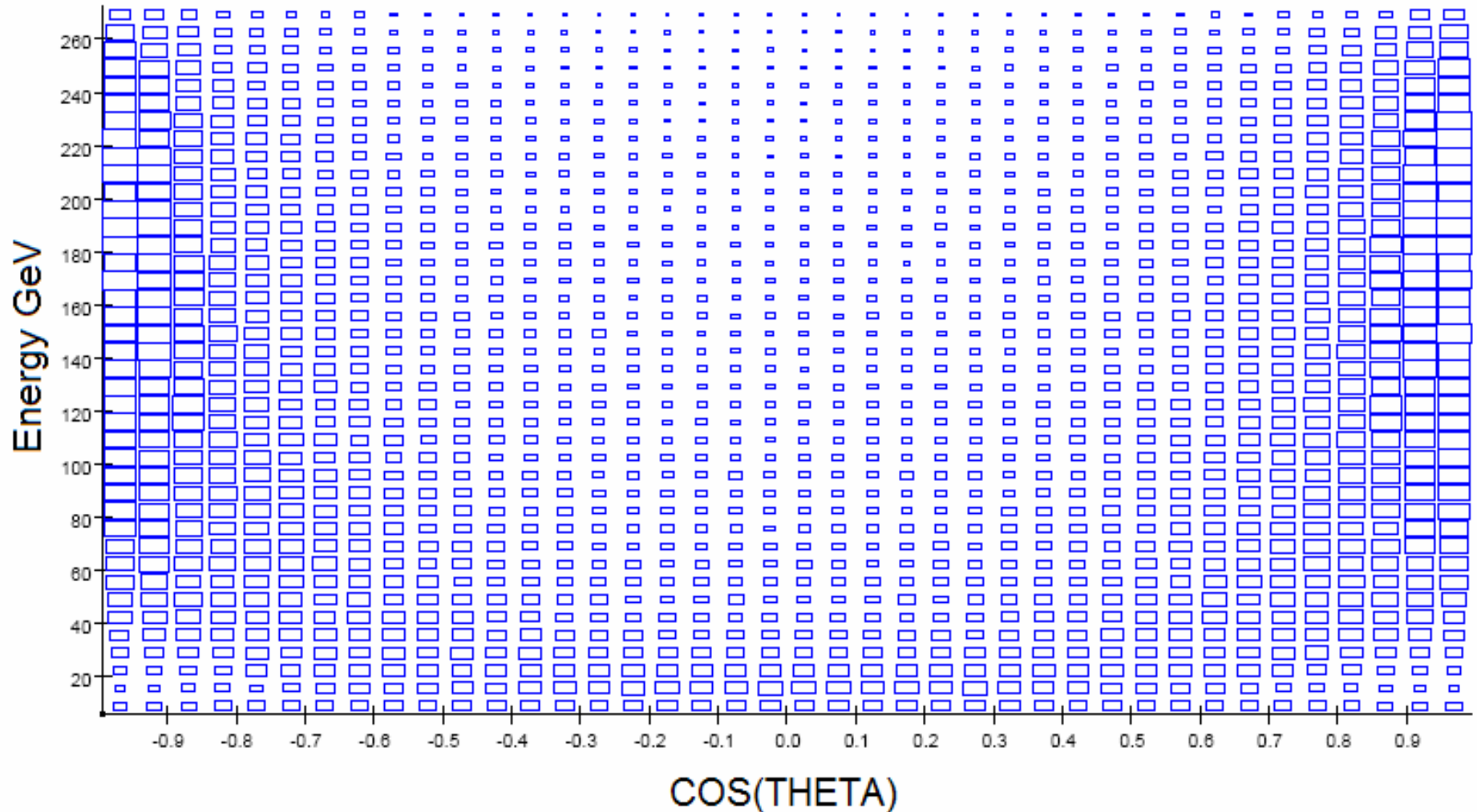
SUSY: Particle cos(theta) (no cuts)





Electron production is peaked in the forward region for higher energies.

SUSY: PARTICLE COSTHETA VS ENERGY (cuts)



Compilation of SUSY particle spectra from Snowmass 2001 benchmark models

Nabil Ghobbae[†], Hans-Ulrich Martyn^{*}

[†] DESY, Hamburg, Germany, ^{*} I. Physikalisches Institut der RWTH, Aachen, Germany

Abstract

A comparative study of supersymmetric particle spectra calculated by the programs ISAJET, SUSYGEN and PYTHIA is presented for various SUSY scenarios defined at the Snowmass 2001 workshop.

At the Snowmass 2001 'Summer Study on the Future of Particle Physics' a consensus was reached to define a list of SUSY models as benchmarks to be investigated in future collider studies. Various scenarios, so-called 'Snowmass Points and Slopes' (SPS), were proposed^{1,2} in terms of a few parameters describing 'typical' to 'extreme' R_p conserving supersymmetrically breaking mechanisms of mSUGRA, GMSB and AMSB. All benchmark points respect currently existing experimental constraints.

	mSUGRA scenario	m_0	$m_{1/2}$	A_0	$\tan \beta$	sign μ
SPS 1	typical point	100	250	-100	10	+
SPS 2	focus point region	1450	300	0	10	+
SPS 3	model line into coannihilation region	90	400	0	10	+
SPS 4	large $\tan \beta$	400	300	0	50	+
SPS 5	light stop	150	300	-1000	5	+
SPS 6	non-unified gaugino masses $M_1 = 180, M_2 = M_3 = 300$	150	300	0	10	+
	GMSB scenario	Λ	M_{mess}	N_{mess}	$\tan \beta$	sign μ
SPS 7	NISU ³ = $\tilde{\tau}_1$	40,000	80,000	3	15	+
SPS 8	NISU ³ = $\tilde{\chi}_1^0$	100,000	200,000	1	15	+
	AMSB scenario	m_0	$m_{1/2}$		$\tan \beta$	sign μ
SPS 9	small $\Delta m(\tilde{\chi}_1^+ - \tilde{\chi}_1^0)$	400	60,000		10	+

masses and scales in GeV

However, at Snowmass it was recommended to take the SUSY particle spectrum as generated by the program ISAJET³ as the reference for benchmark models, instead of the few high energy

¹ 'SUSY benchmark discussion' at Snowmass 2001, <http://otia.phys.nyu.edu/~schmittra/snowmass>

² M Battaglia et al, 'The Snowmass points and slopes: benchmarks for SUSY searches', Snowmass proceedings, in preparation

³ H Baer et al, hep-ph/0001086, ISAJET, <http://paige.home.cern.ch/paige>



Physics parameters

mSUGRA Parameters $M_0 = 100 \text{ GeV}$ (Universal Scale mass)

SPS1A $m_{1/2} = 250 \text{ GeV}$ (Universal Gaugino Mass)

$A_0 = -100 \text{ GeV}$ (Trilinear coupling in Higgs sector)

$\tan\beta = 10$ (Ratio of two VEV)

$\text{sign}\mu = 1$ (Higgsino mixing parameter)

Right selectron mass = 143.112 GeV

X^0_1 LSP mass = 95.473 GeV

1 SPS 1 – mSUGRA scenario

m_0	100 GeV
$m_{1/2}$	250 GeV
A_0	-100 GeV
$\tan \beta$	10
sign μ	+

'typical' scenario
 $m_0 = 0.4 m_{1/2} = -A_0$

1.1 Spectrum & parameters of ISAJET 7.58

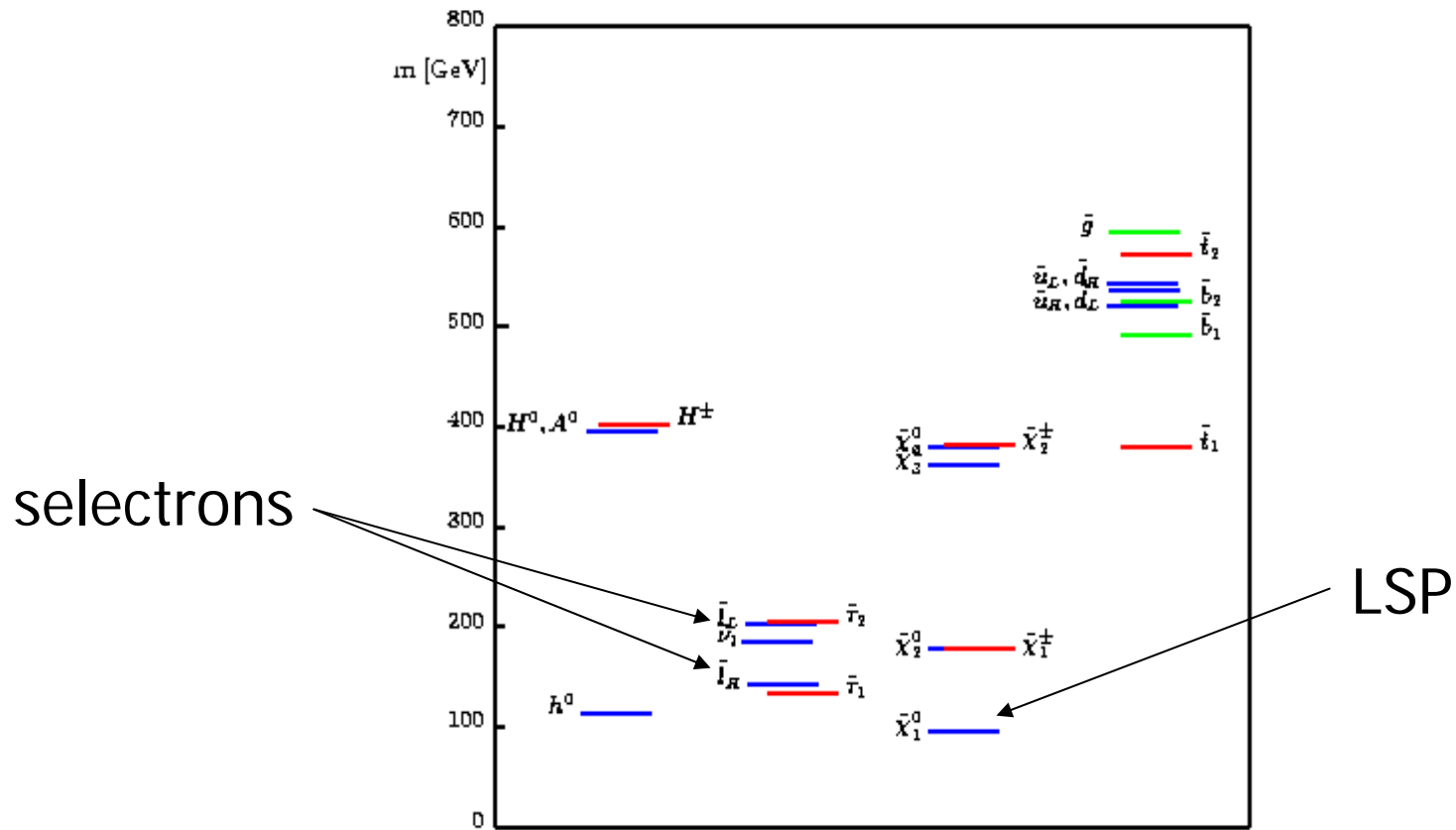
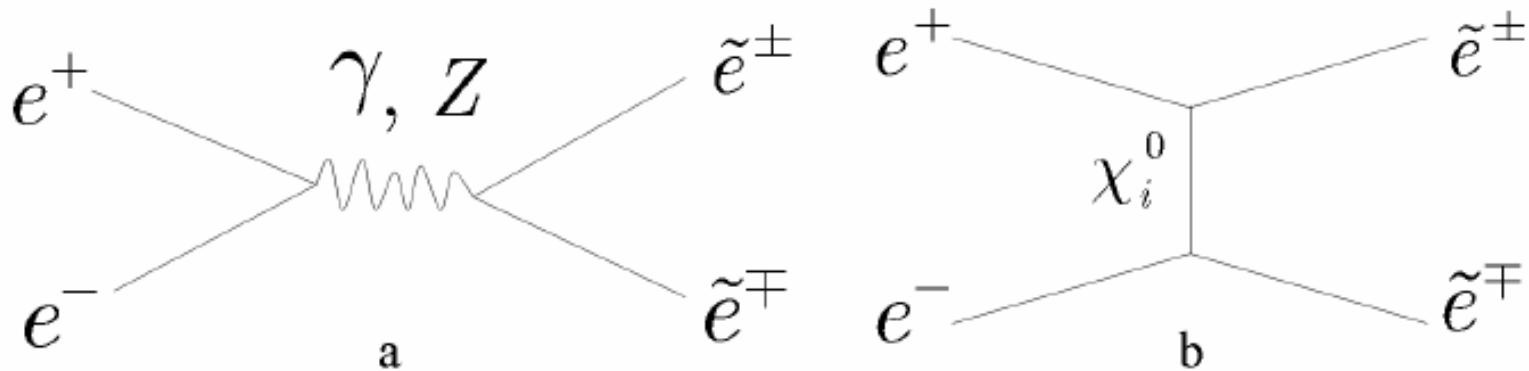
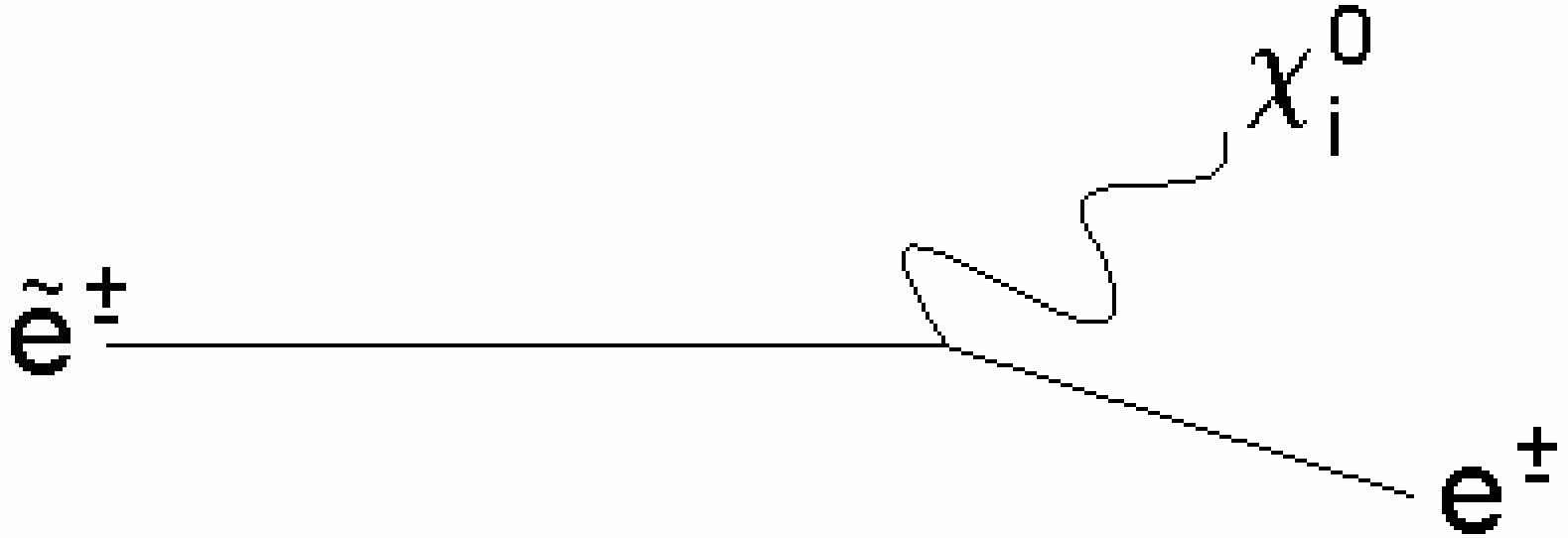


Figure 1: SPS 1 mass spectrum of ISAJET



Selectron production channels

- s-channel (central region)
- t-channel (dominates the forward region when lightest selectron and X^0_1 LSP mass are small... SPS1A satisfies these conditions)



- selectron decay \rightarrow electron + neutralino



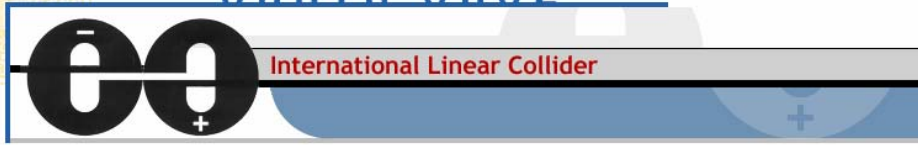
Theory

Every X^0_1 / selectron mass combination has a distinctive electron energy distribution.

The electron energy spectrum endpoint (EEEP) reveals the mass of the selectron and X^0_1 LSP.

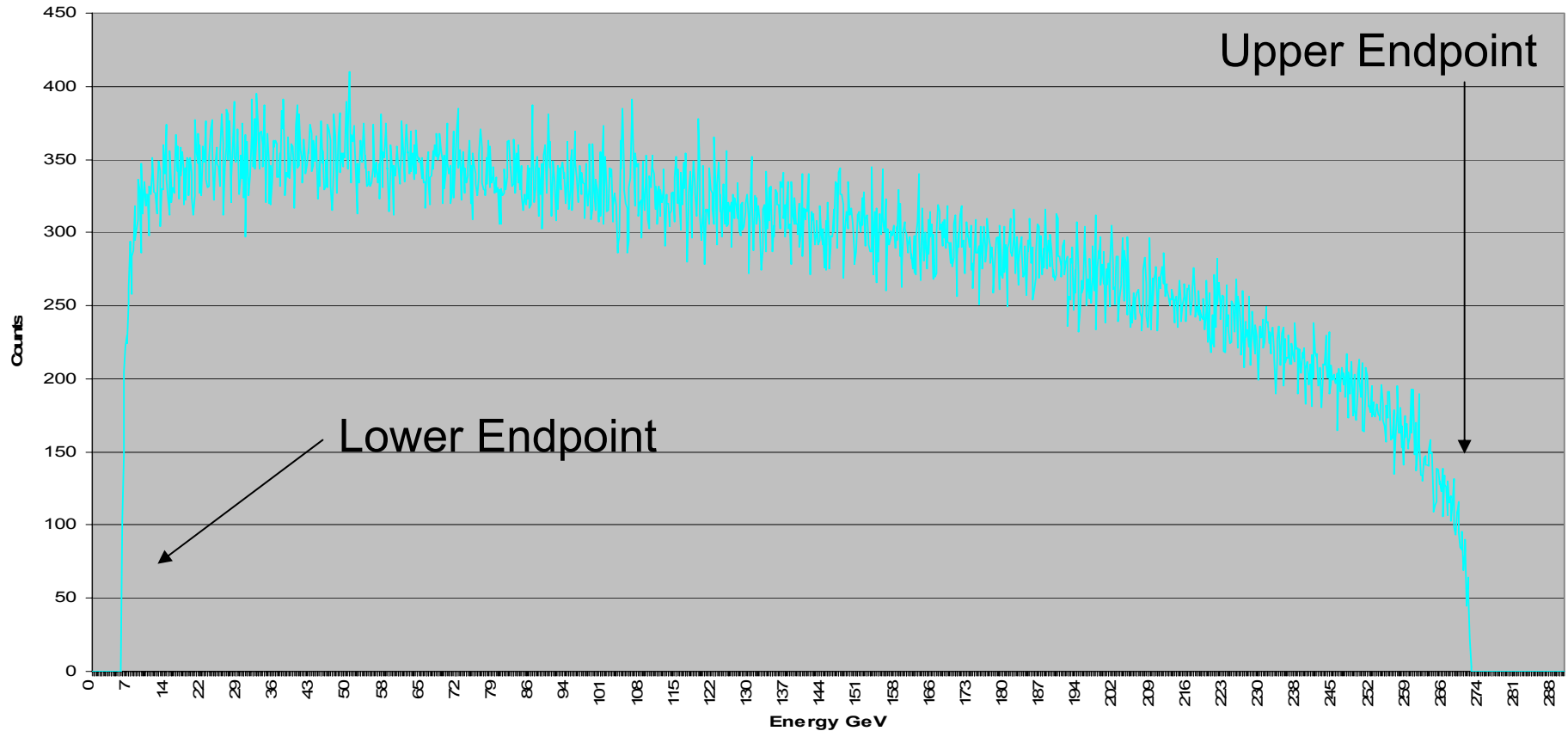
Measurement can be difficult in the presence of ISR, bremsstrahlung, and beamstrahlung. How do we do it ?

What effects, if any, do beamspread and the detectors' resolution have on determining the EEEP?



Energy Distribution

Electron energy distribution with beam/bremm/ISR (.16%). No detector effects or beam energy spread.



- sample electron energy distribution $M_{\text{selectron}} = 143.112$ (SPS1A)

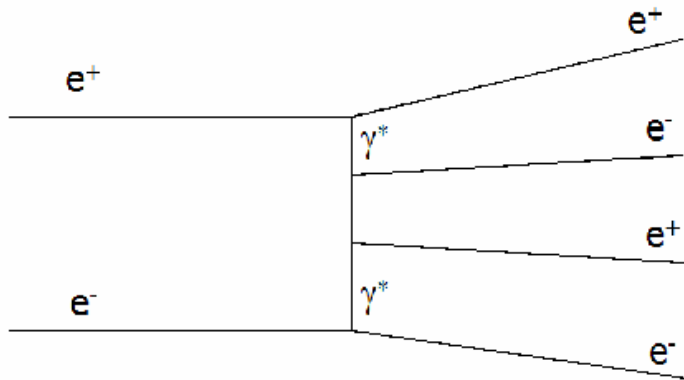


Gerbode, Mooser, Holguin

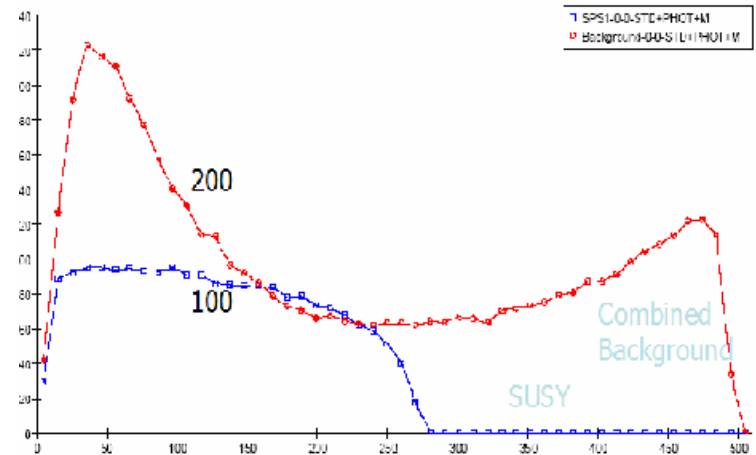
Standard Model Cuts

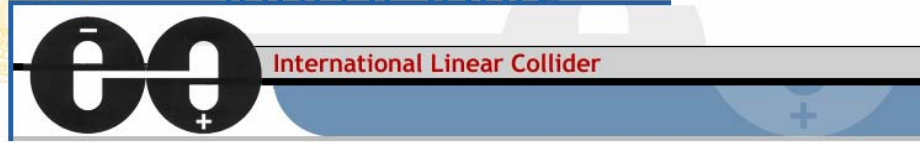
Previous work done in 2003-2004 developed cuts to remove standard model, SUSY like, events.

Explored eee backgrounds in central region



Explored forward region

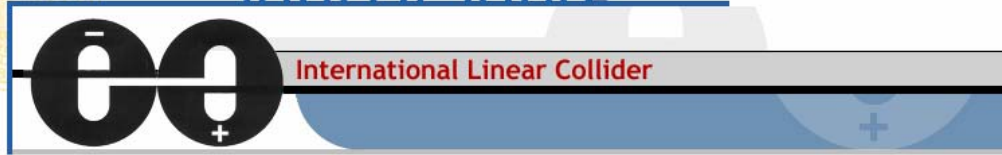




The Cuts

- **Fiducial Cut:** Exactly one final state positron/electron pair is observed, and each of the pairs has a transverse momentum of at least 5GeV. Otherwise the event is discarded.
- **Tagging Cut:** If a final state fermion is found in the tagging region, the event is discarded.
- **Photon Cut:** Cuts events if there is a photon in the tagging region with energy of 20GeV or more, and cuts events with photon in forward or central region with energy of 5GeV or more.
- **Transverse Momentum Cut:** Cuts events where vector sum of transverse momentum for + - e e pair is less than $2 * 250\text{GeV} * \sin(20 \text{ mrad})$.
- **HP Cut:** Removes low-mass, t -channel-dominated $e e \nu \nu$ backgrounds while preserving high-mass SUSY signal

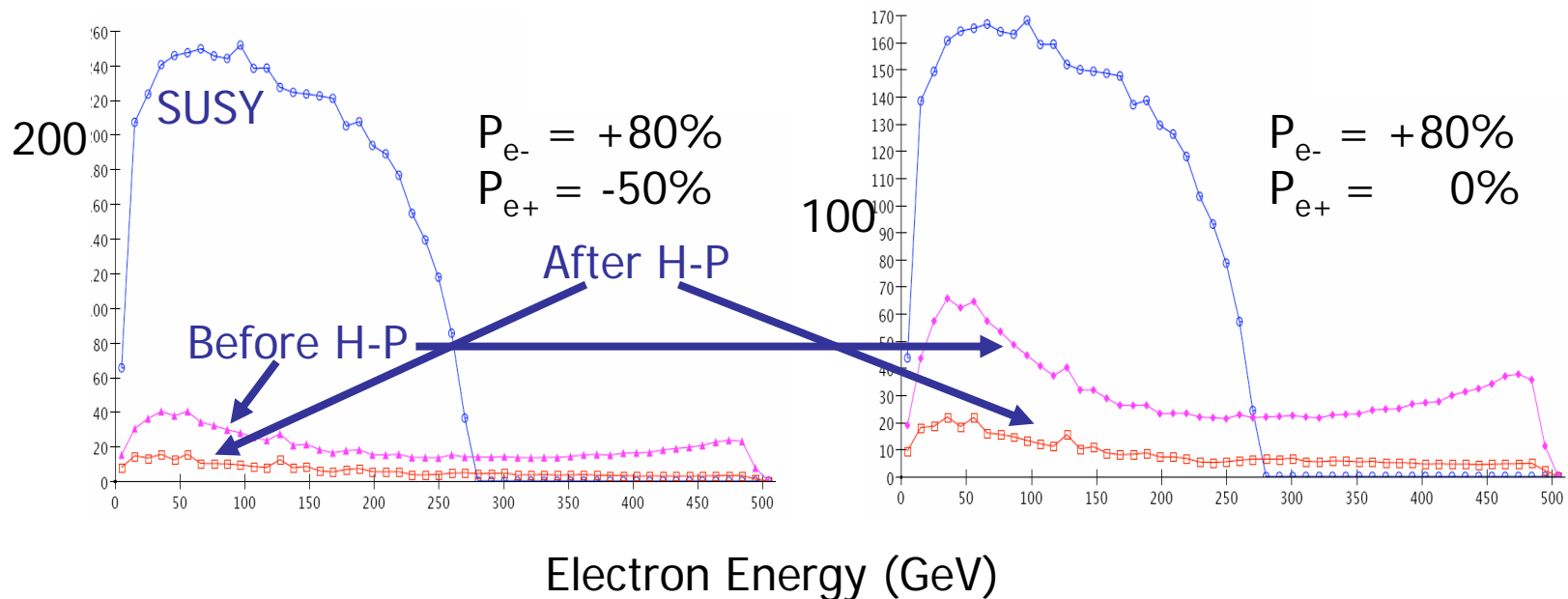
$$|\vec{p}_{e^-} + \vec{p}_{e^+}| < 225$$

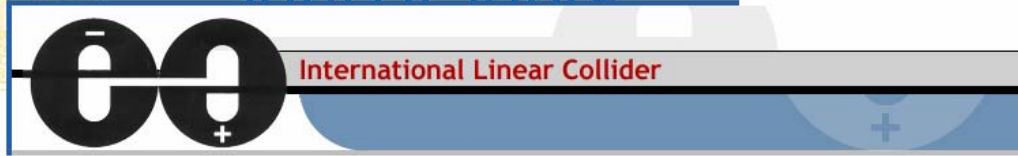


Use of Beam Polarization

Also: can extinguish main background ($e\bar{e}\nu\nu$) with RH electron and LH positron polarization

For fixed integrated luminosity, the signal is higher and the background lower with positron polarization.





Results of Event Selection Study

Selectron production can be detected over the full tracking volume

Developed two additional helpful cuts: looking for photons radiated in $eeee$ processes and cutting on momentum imbalance ('H-P').

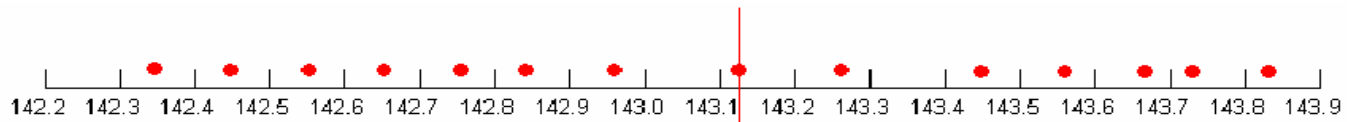
M_{\min} cutoff needs to be extended down below 4 Gev for $ee\nu\nu$ generation

Now on to finding the selectron mass...



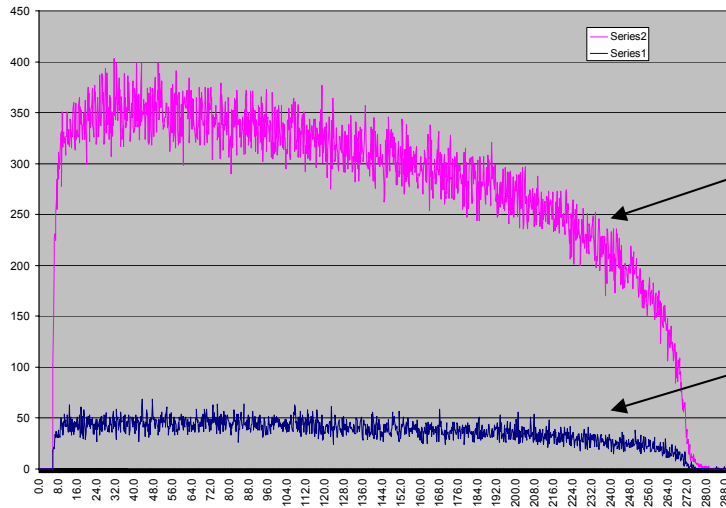
The one-dimensional **CHI-Squared Method** for determining the right-handed selectron mass

- 1) Keep the X^0_1 mass constant at 95.473 GeV
- 2) Vary the selectron mass and create corresponding Monte Carlo template data. Files are generated at high luminosity (800 fb⁻¹) and simulate beam/brem and ISR.



- 3) Generate a data set at SPS1A with expected LC luminosity(115 fb⁻¹).

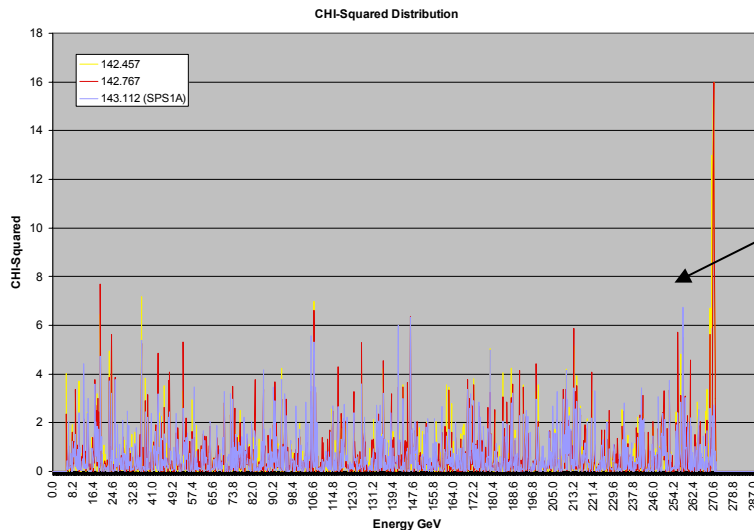
4) Run everything through JAS, perform Cuts, histogram the energy



High luminosity MC template

Realistic luminosity data

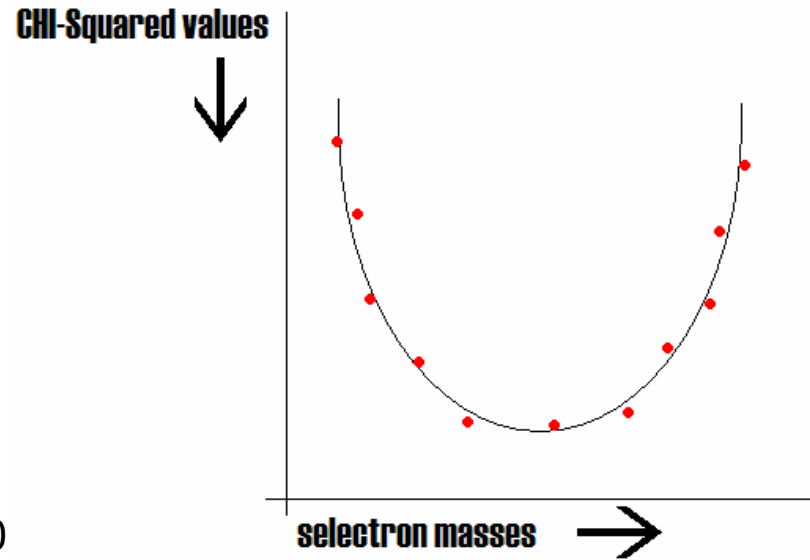
5) Perform a CHI-Squared comparison between the data set and each of the template sets' (selectron mass assumptions) histograms. Obtain a Chi-Square value for each.



MC CHI-Square spectrum for three MC templates

6) Plot CHI-Squared vs. selectron mass and fit to a parabola-like curve (quartic).

7) The minimum of the curve is the fitted selectron mass corresponding to this data set.



8) Wash, rinse and repeat the process 120

9) Calculate the average fitted mass and RMS error.

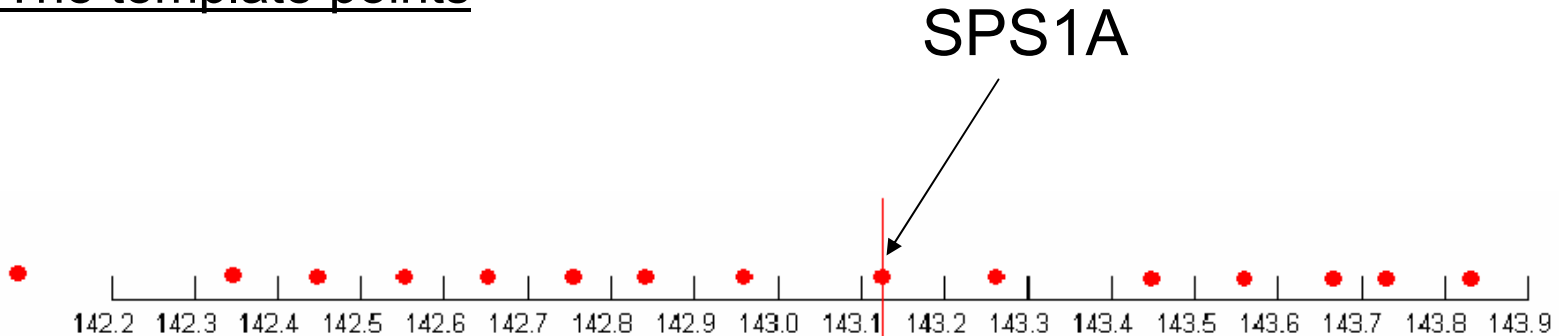
10) Bin the data, fit to Gaussian, and find the Gaussian fitted mass and Gaussian error.

* Cuts developed by Gerbode, Holguin, and Mooser remove practically all backgrounds, therefore standard model processes are not included in this study.



Step 2 - The template points

143.823
 143.718
 143.680
 143.571
 143.440
 143.279
 143.112
 142.974
 142.836
 142.767
 142.663
 142.560
 142.457
 142.353
 142.015



SUSY parameters are changed in a way that changes the selectron mass while holding the neutralino mass constant.

Initially 24 were created, but only the innermost 15 were necessary for quality resolution and fits.



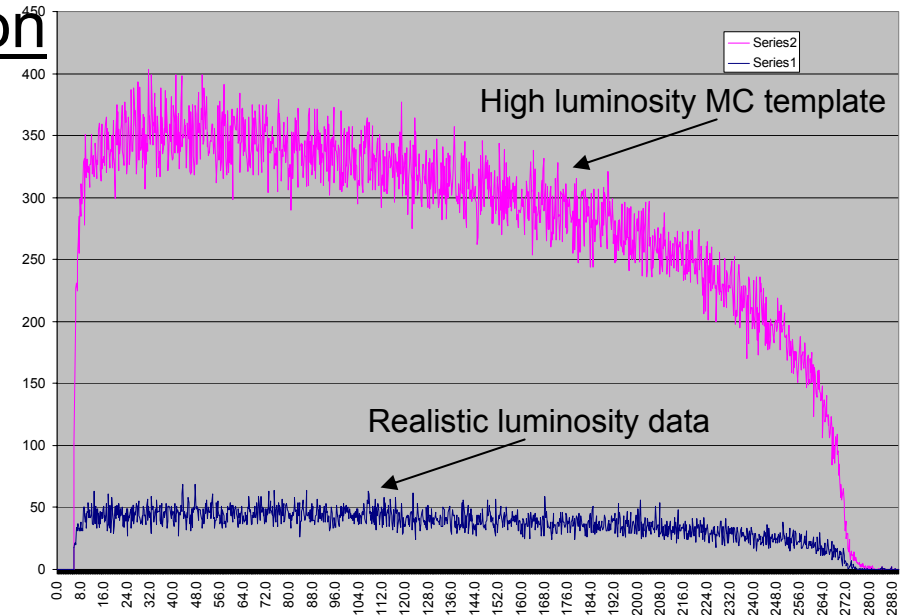
Step 5 - CHI-Squared equation

Energy binning - .2 GeV

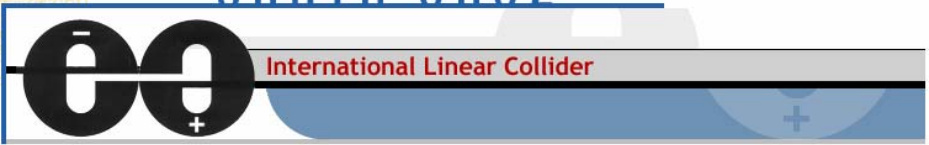
m_i = bin content of template

n_i = bin content of data

$w^2 = \sum m_i / \sum n_i$ (weighting factor)

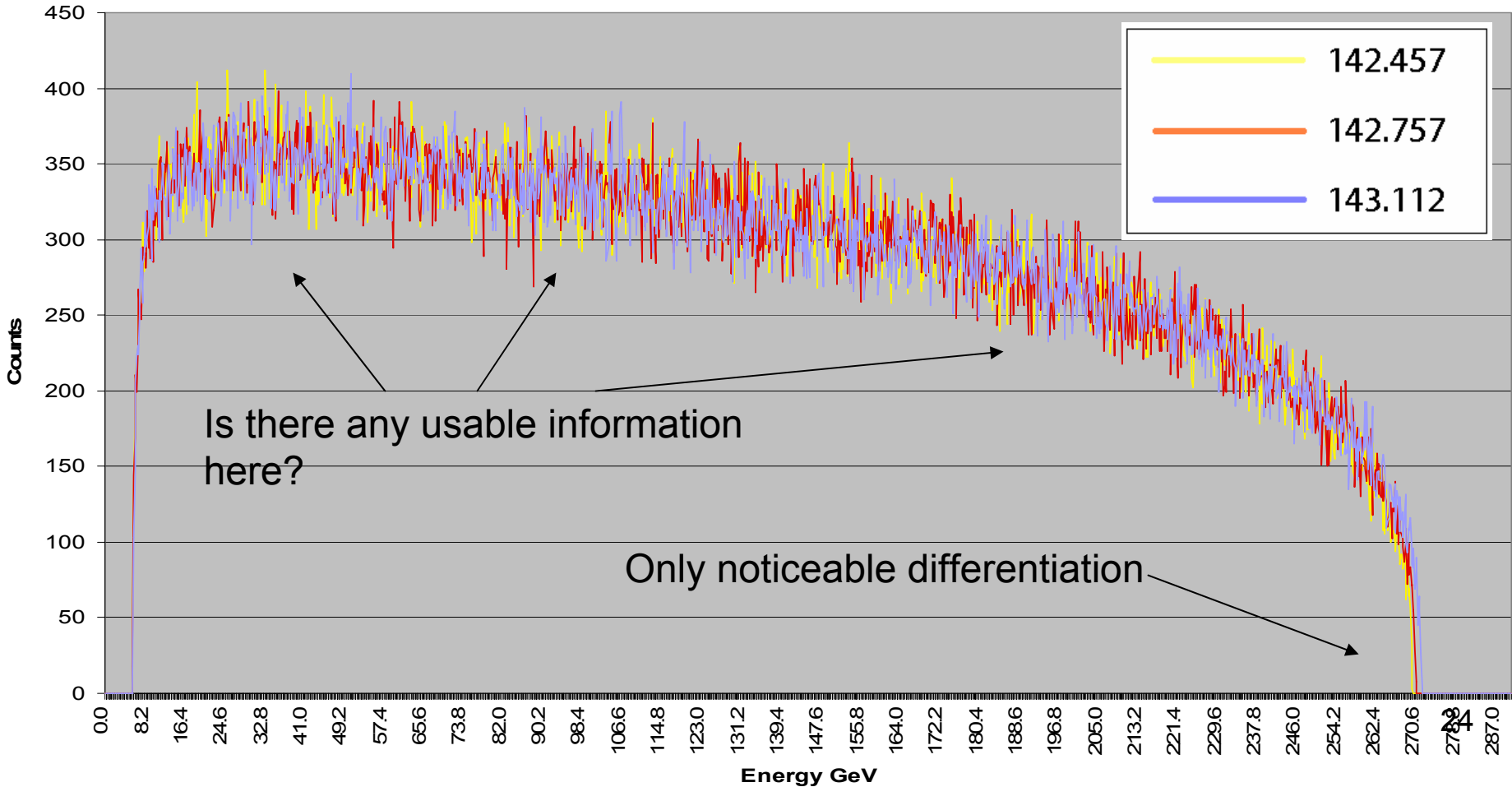


$$\text{CHI-Squared} = \sum \frac{(w * n_i - m_i / w)^2}{(n_i * w^2 + m_i)}$$



Steps 5,6 – Understanding the distribution endpoints

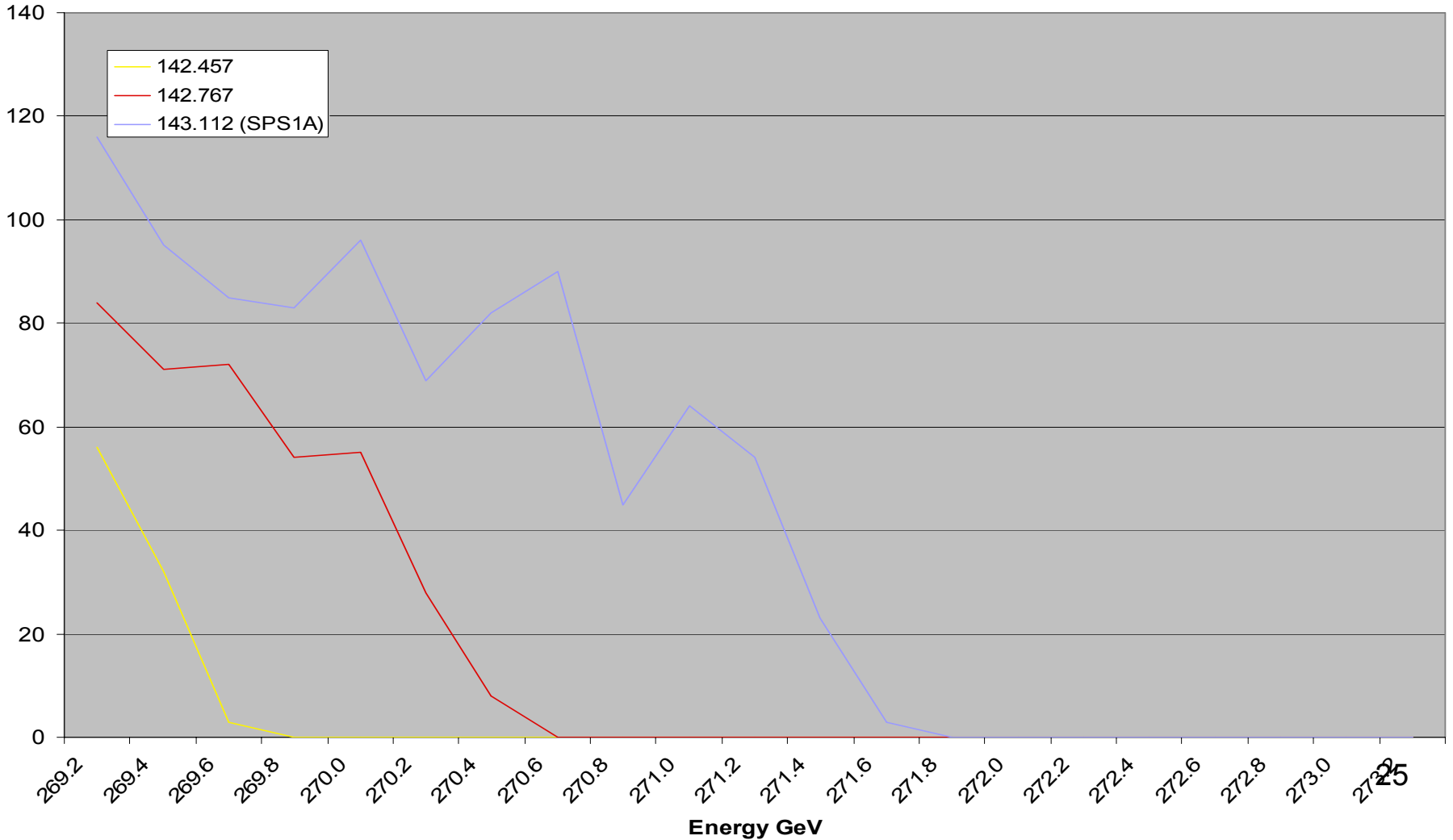
Electron Energy Distribution





Upper Endpoint

Energy Distribution

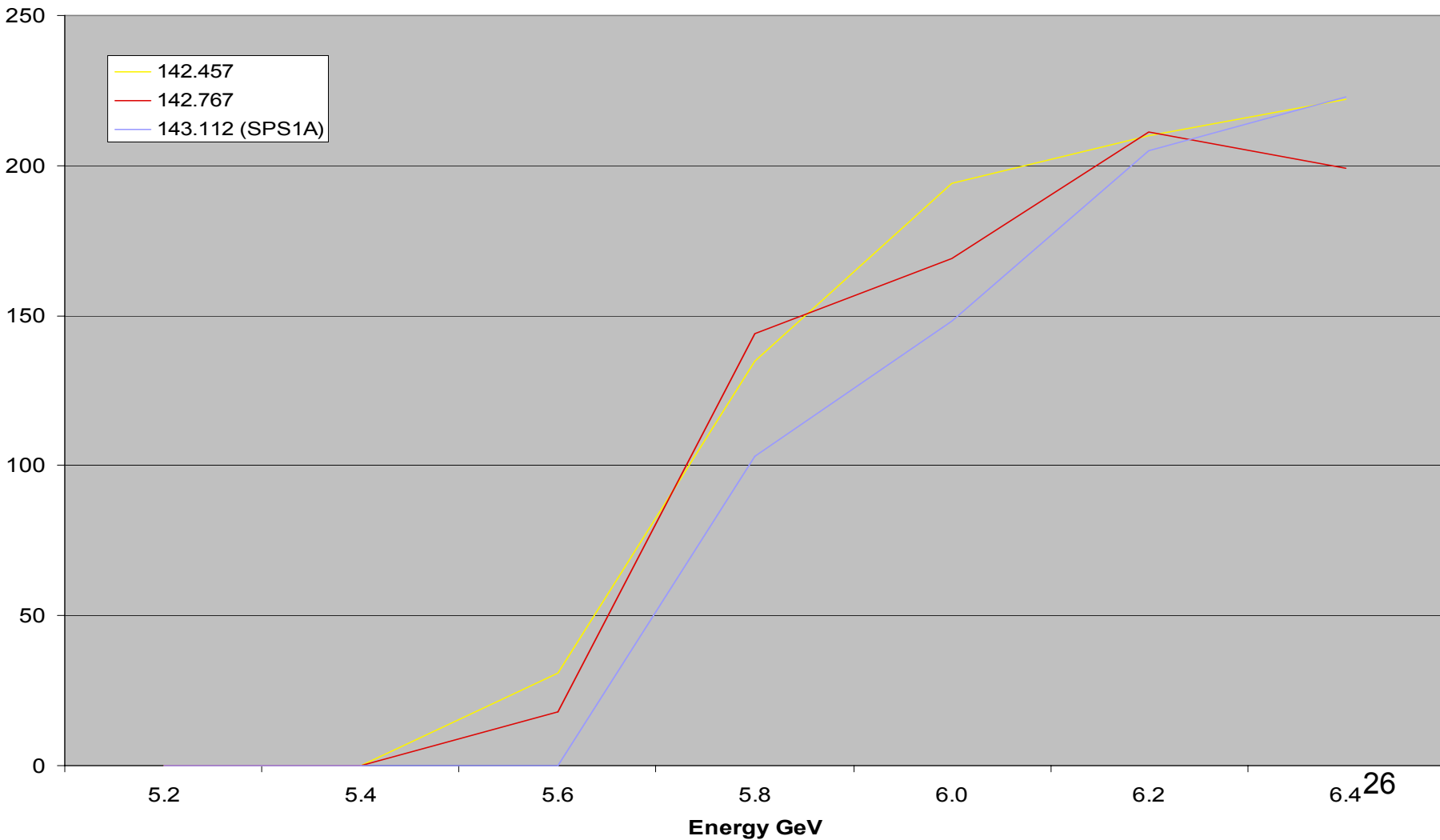




International Linear Collider

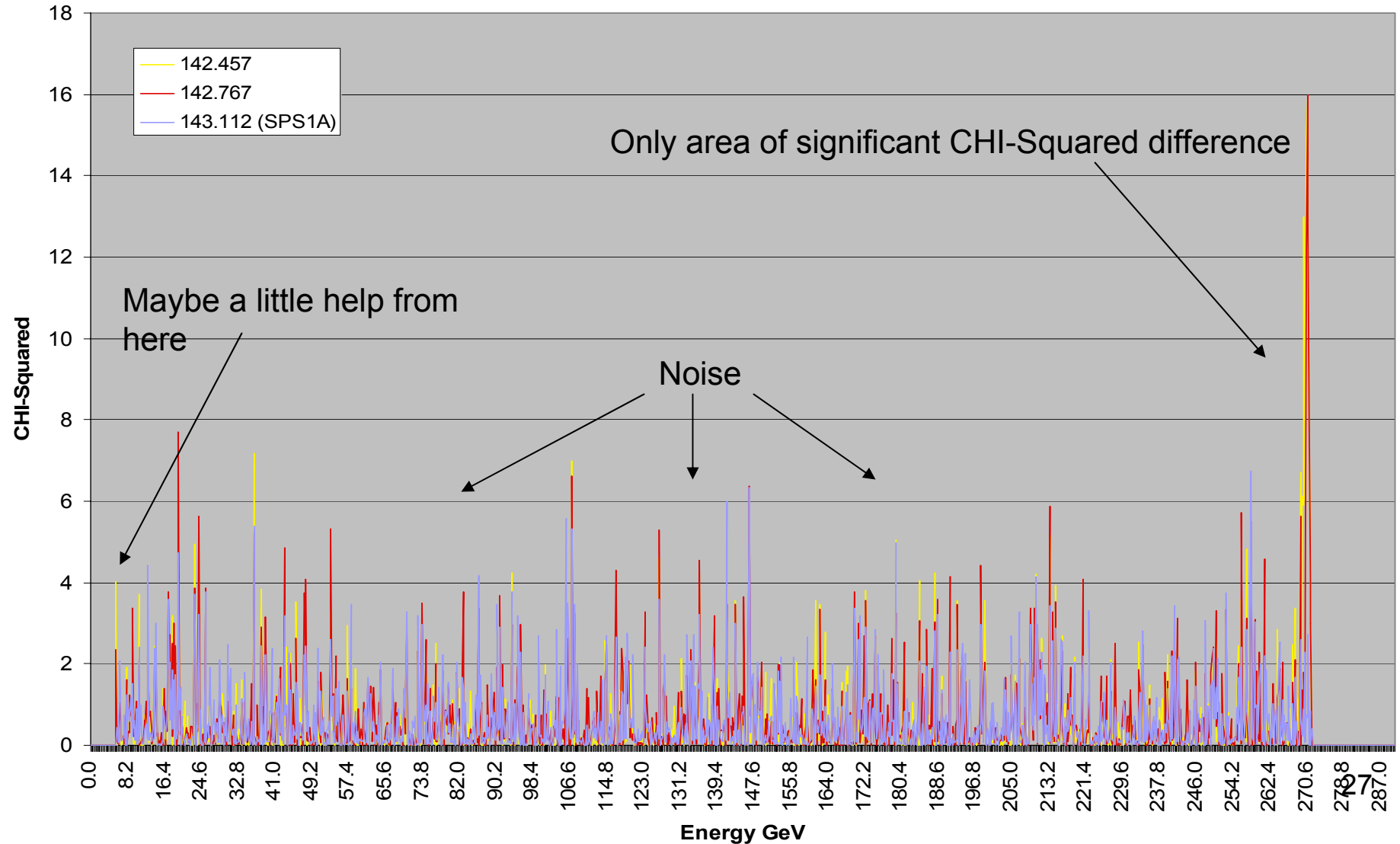
Energy Distribution

Lower Endpoint



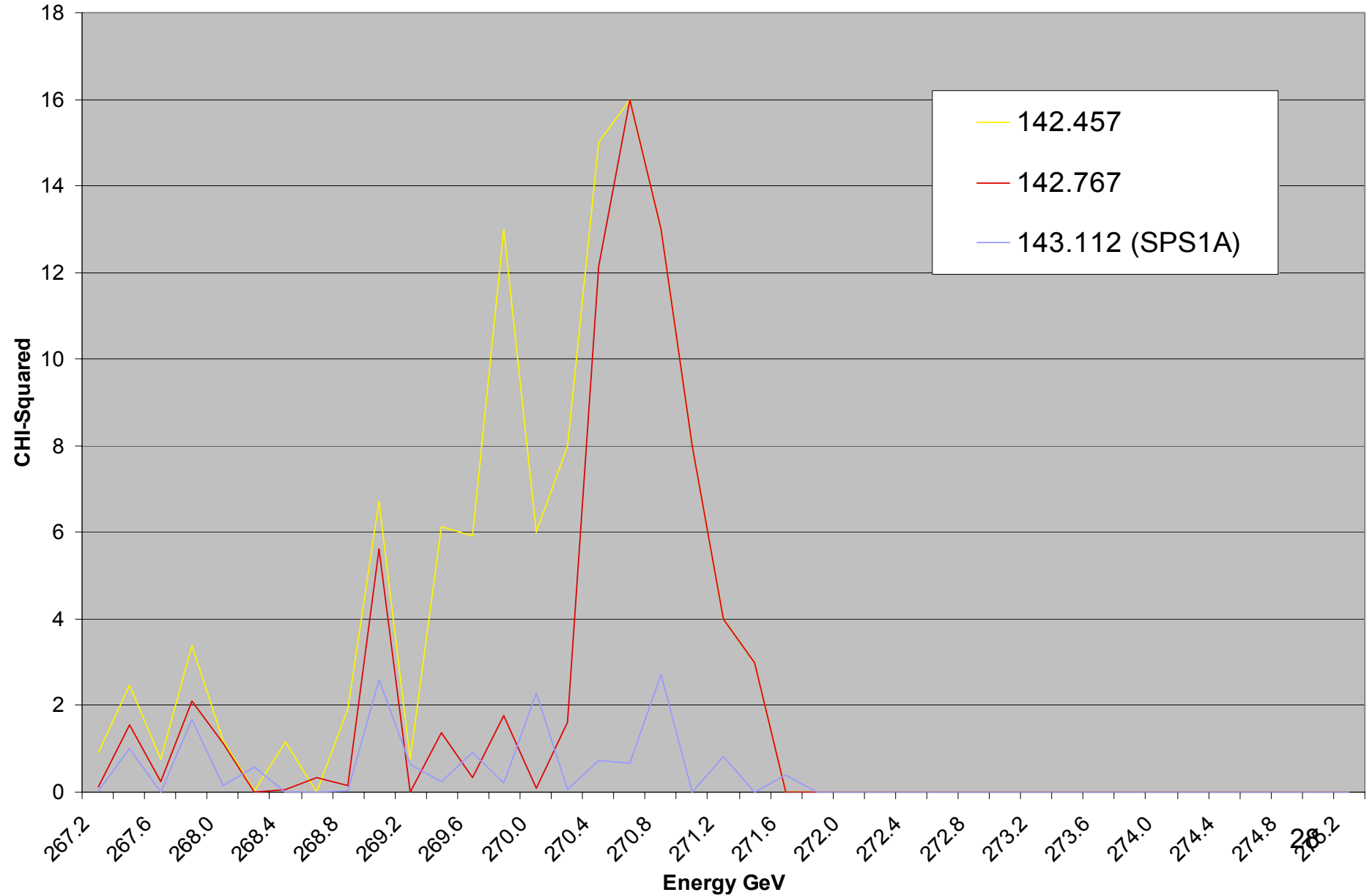
Plot CHI-Squared vs. energy spectrum and see where the differentiation comes from

CHI-Squared Distribution



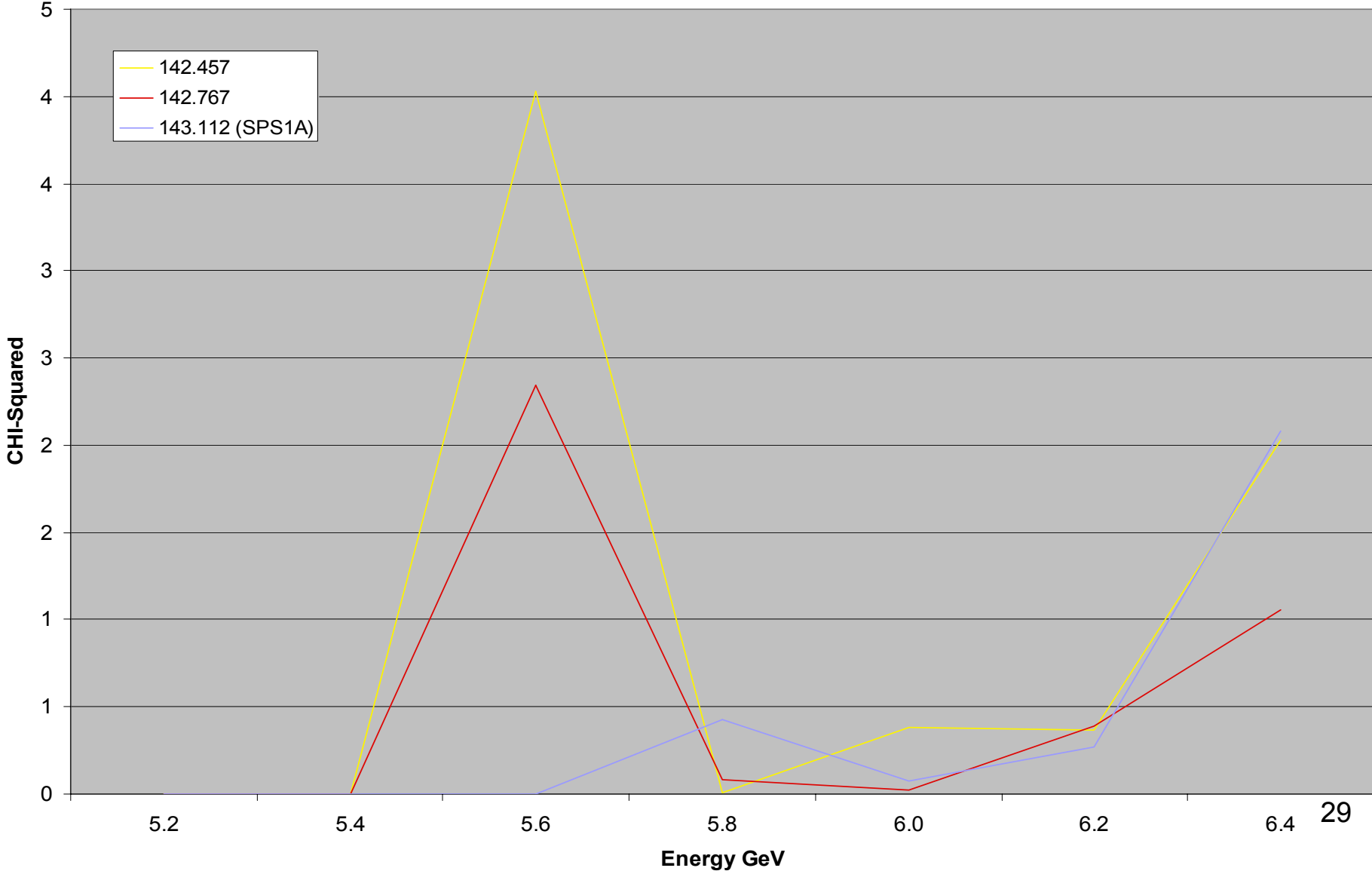
Zooming into the endpoints (upper)...

CHI-Squared Distribution



Zooming into the endpoints (lower)...

CHI-Squared Distribution



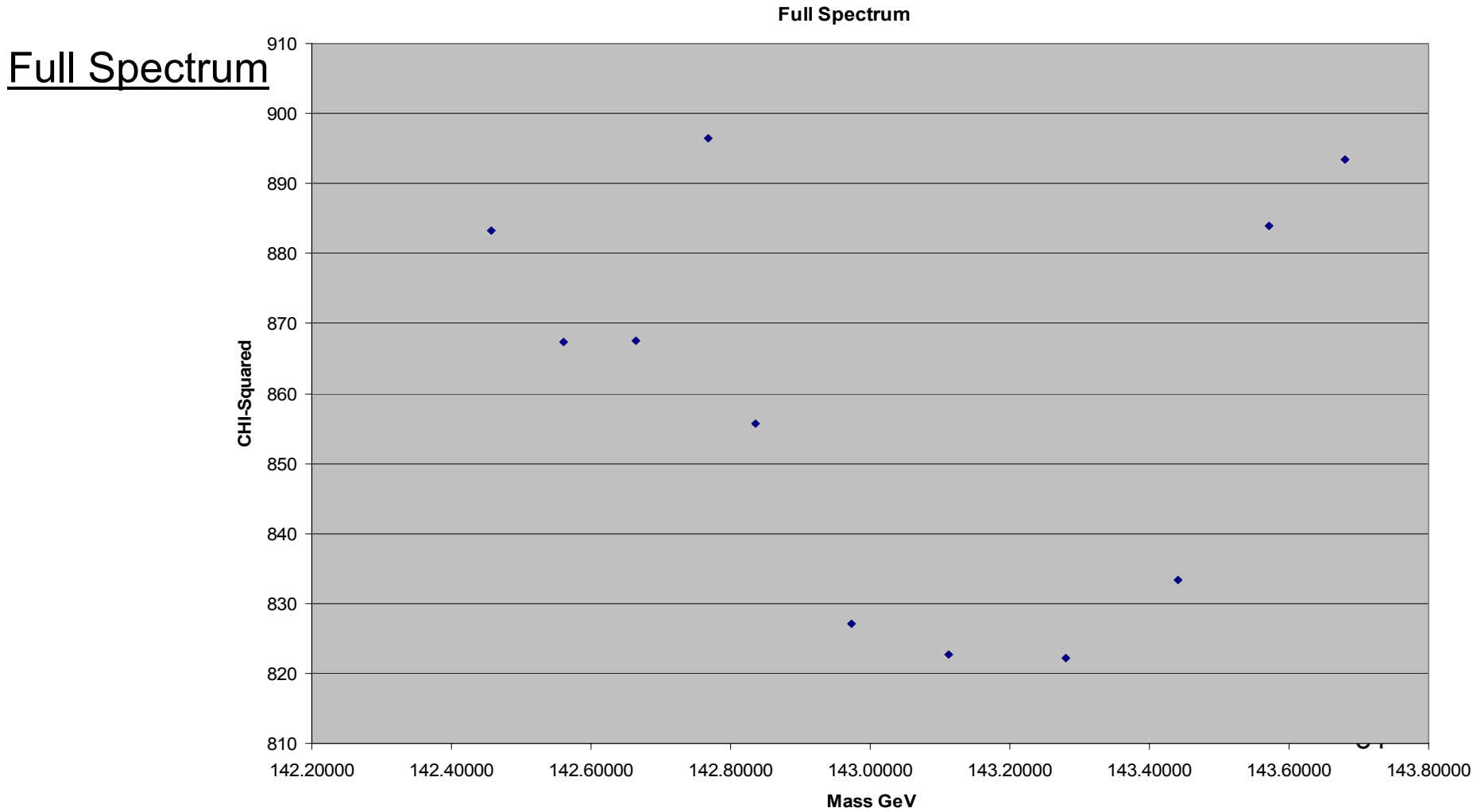


Isolating the endpoint

- Differentiation is small but measurable.
- The noise “off – endpoint”, is enough to compromise the differentiation.
- Ignore the middle. Carefully chose the energy range in which CHI-Squared will be calculated.
- Endpoint ranges used in this study are
 - 5.2 - 6.4 GeV (lower)
 - 269.2 - 273.2 GeV (upper) (no detector smearing)
 - 267.8 - 274.6 GeV (upper) (smearred .16% beamsread)
 - 267.2 - 275.2 GeV (upper) (smearred 1.0% beamsread)
- A truly small part of the spectrum, 4%.
- Isolation essential to obtain the resolution that we have.



So what happens when we use the end-point only technique?

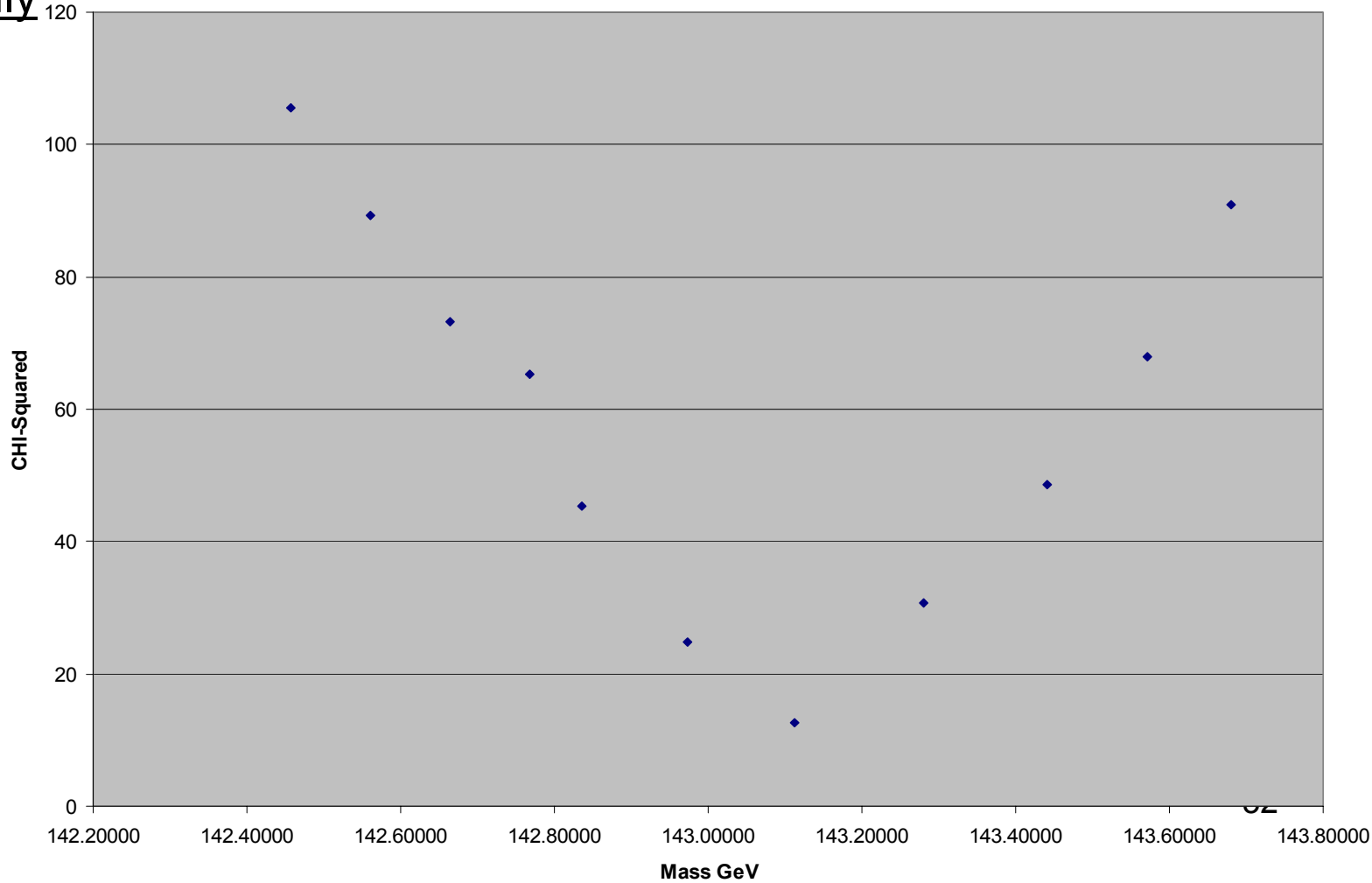




The difference is night and day !

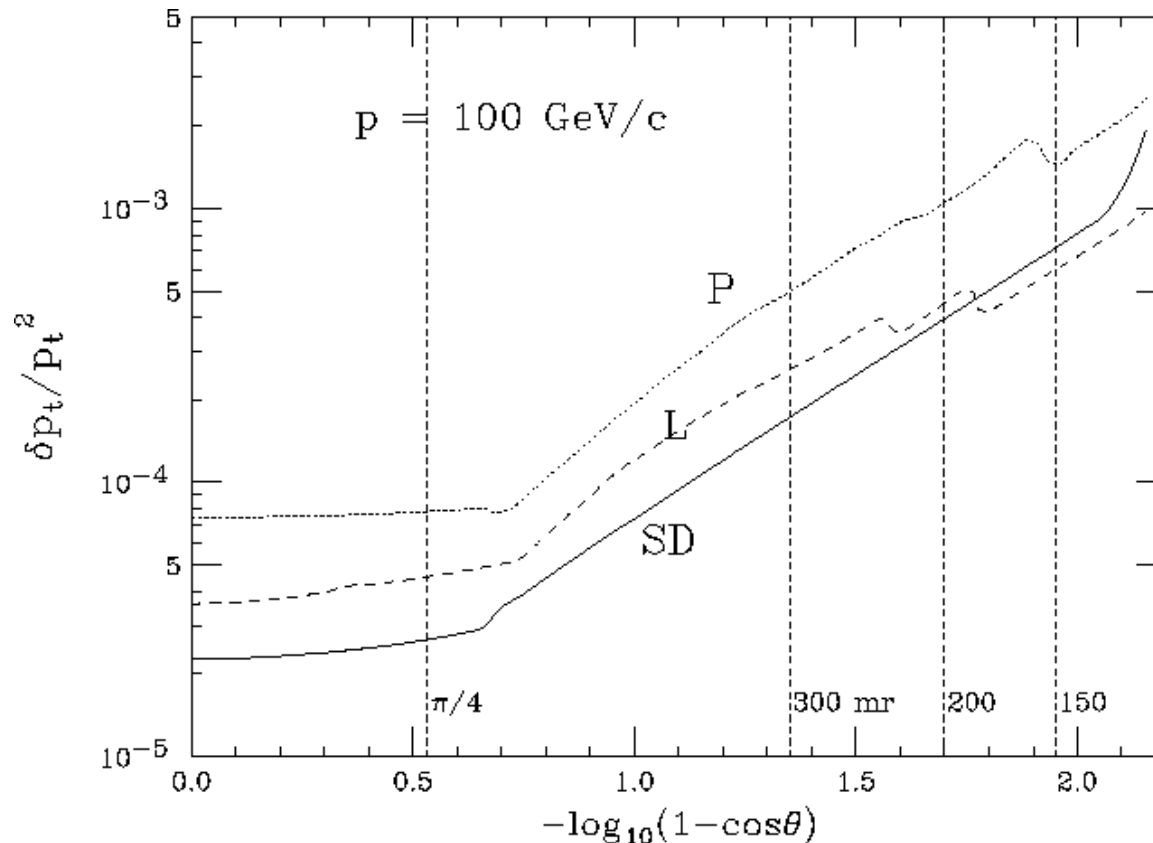
Endpoint Only

Endpoints Only





Okay, so now that we can deal with a perfect machine (no beamspread or smearing), what happens when we include these factors?





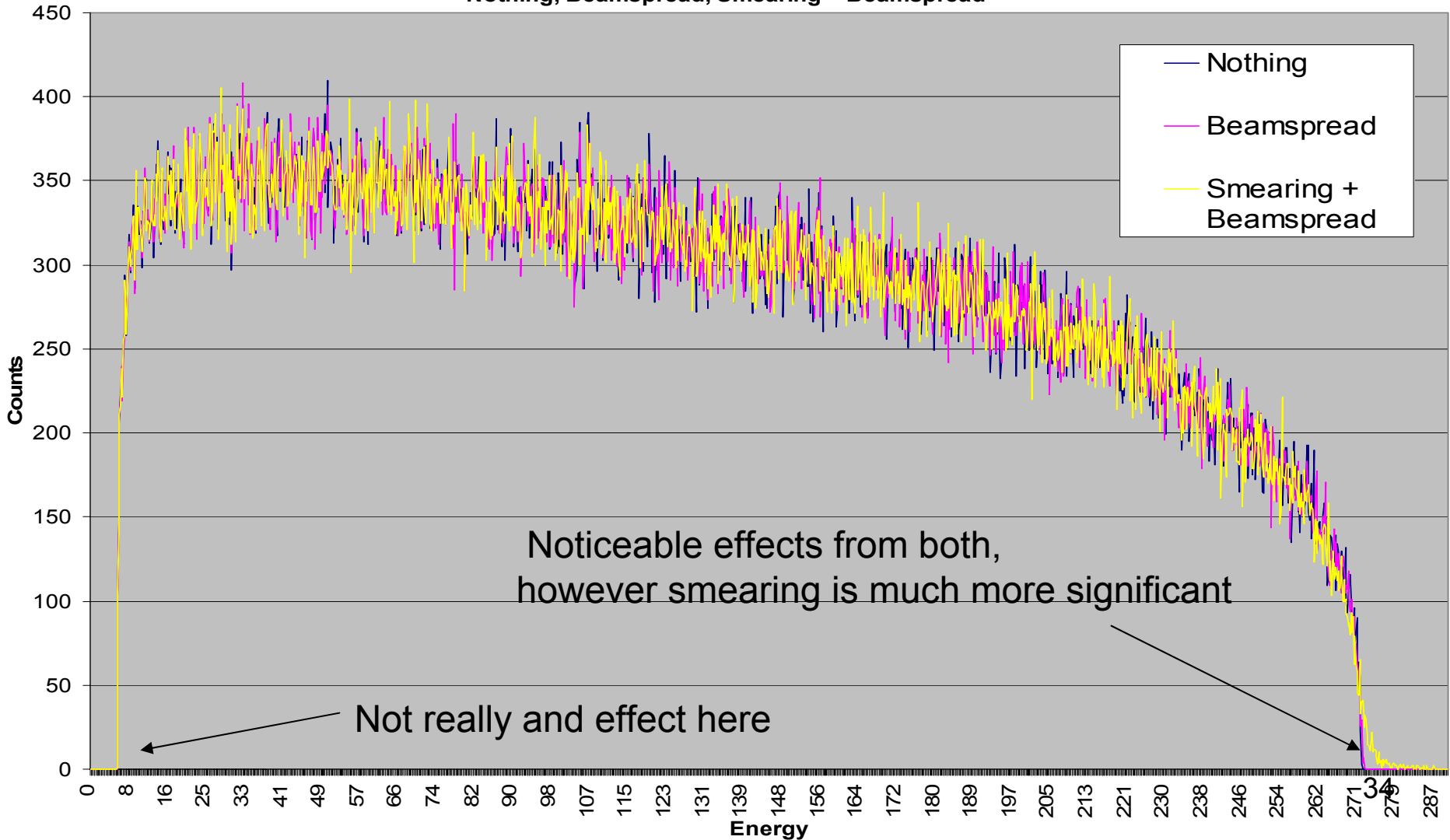
International Linear Collider

SPS1A template (high statistics)
set

Mass of right selectron = 143.112

Beamspread = .16%

Nothing, Beamspread, Smearing + Beamspread

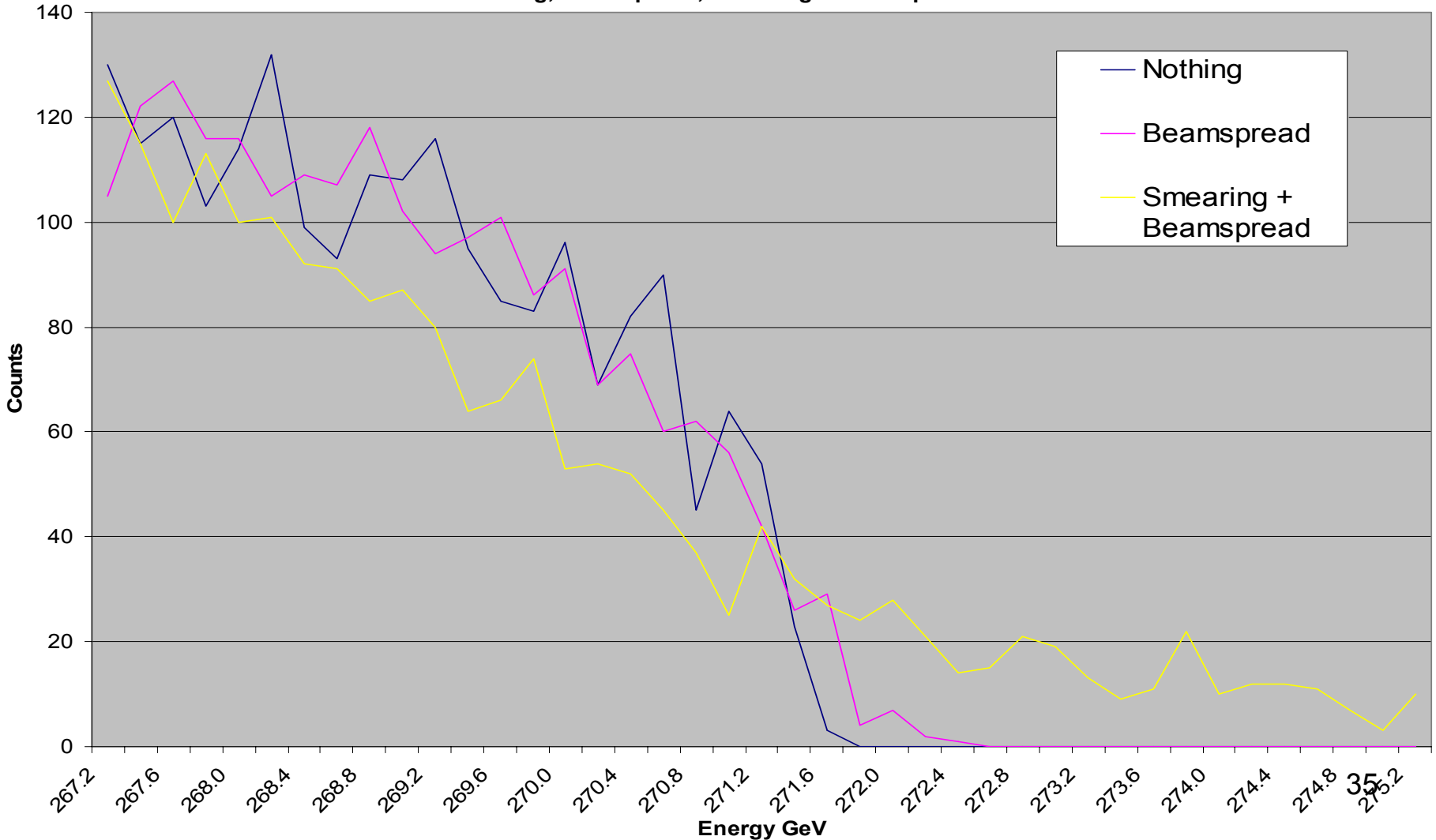




Upper endpoint

significant effects, especially with smearing

Nothing, Beamsread, Smearing + Beamsread

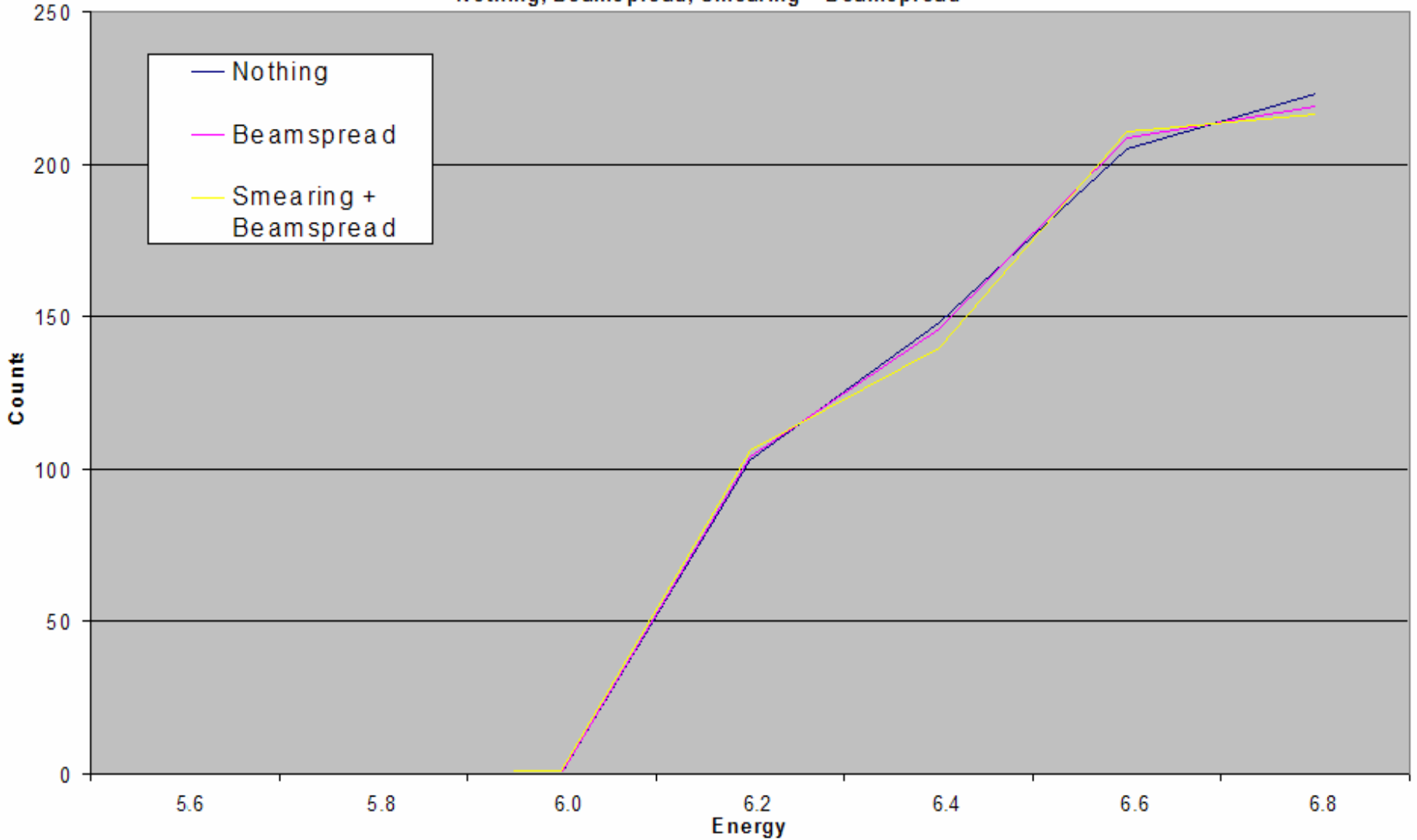




International Linear Collider

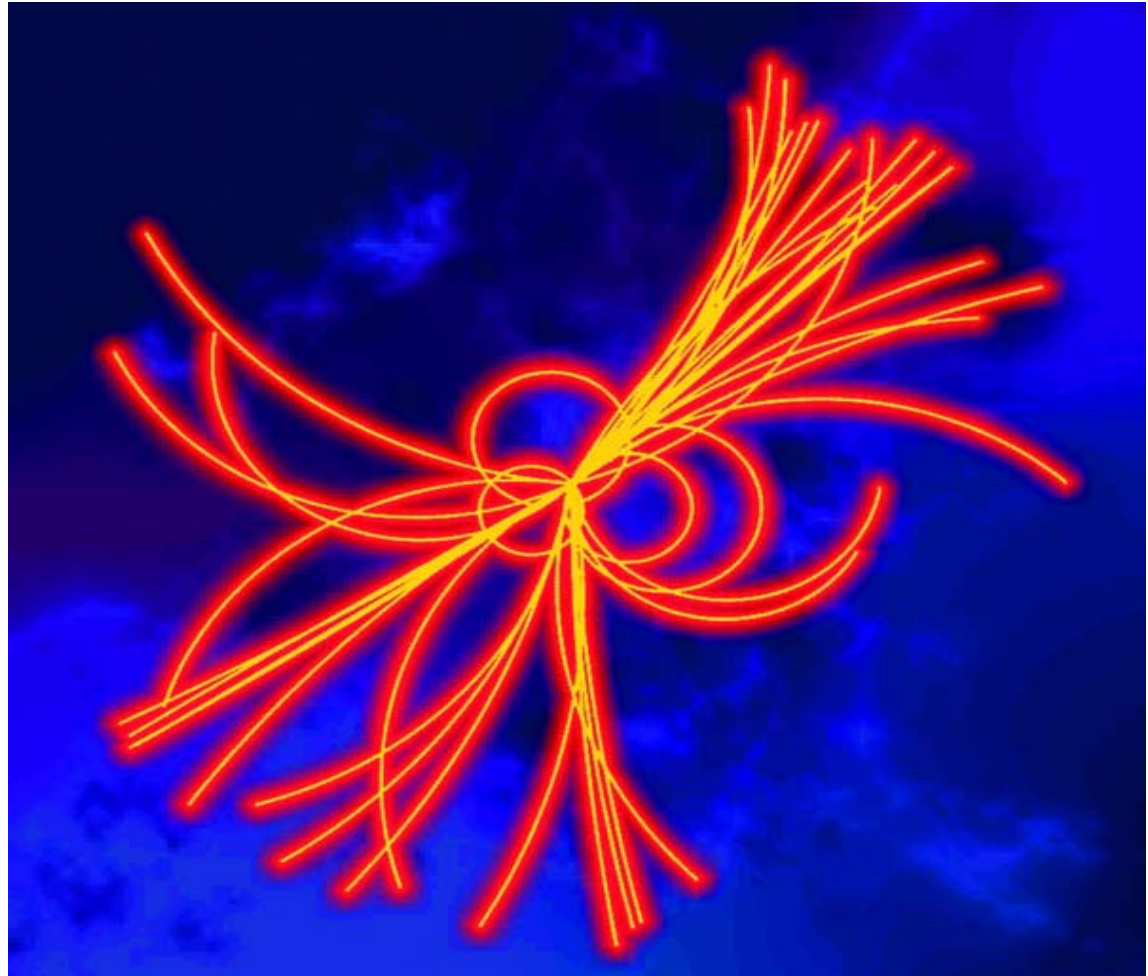
Lower endpoint
no significant effects

Nothing, Beams pread, Smearing + Beamspread





Now lets look at the CHI-Square vs. energy spectrum with detector smearing and .16% beamsread.



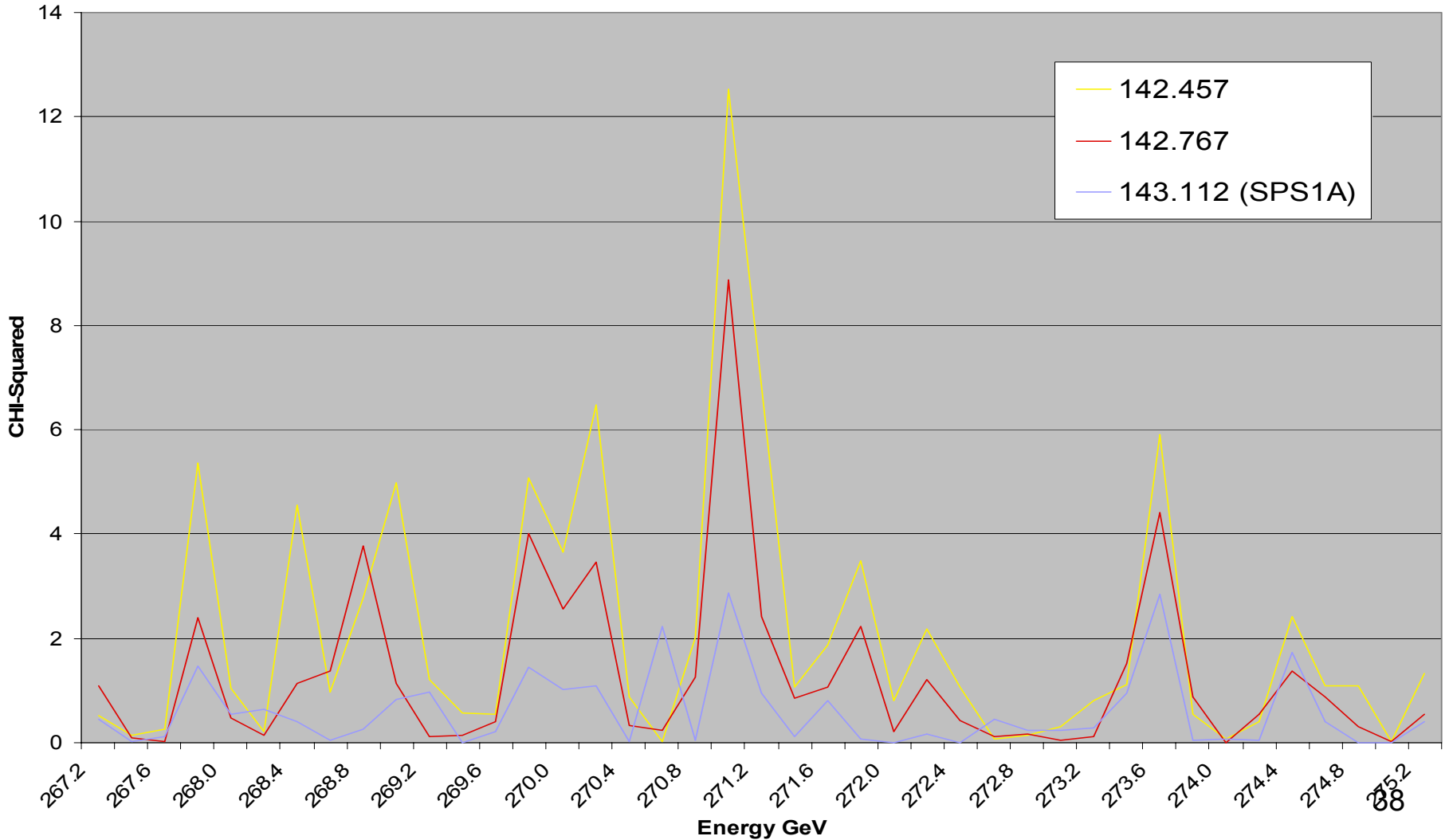


International Linear Collider

Upper endpoint

CHI-squared

CHI-Squared Distribution

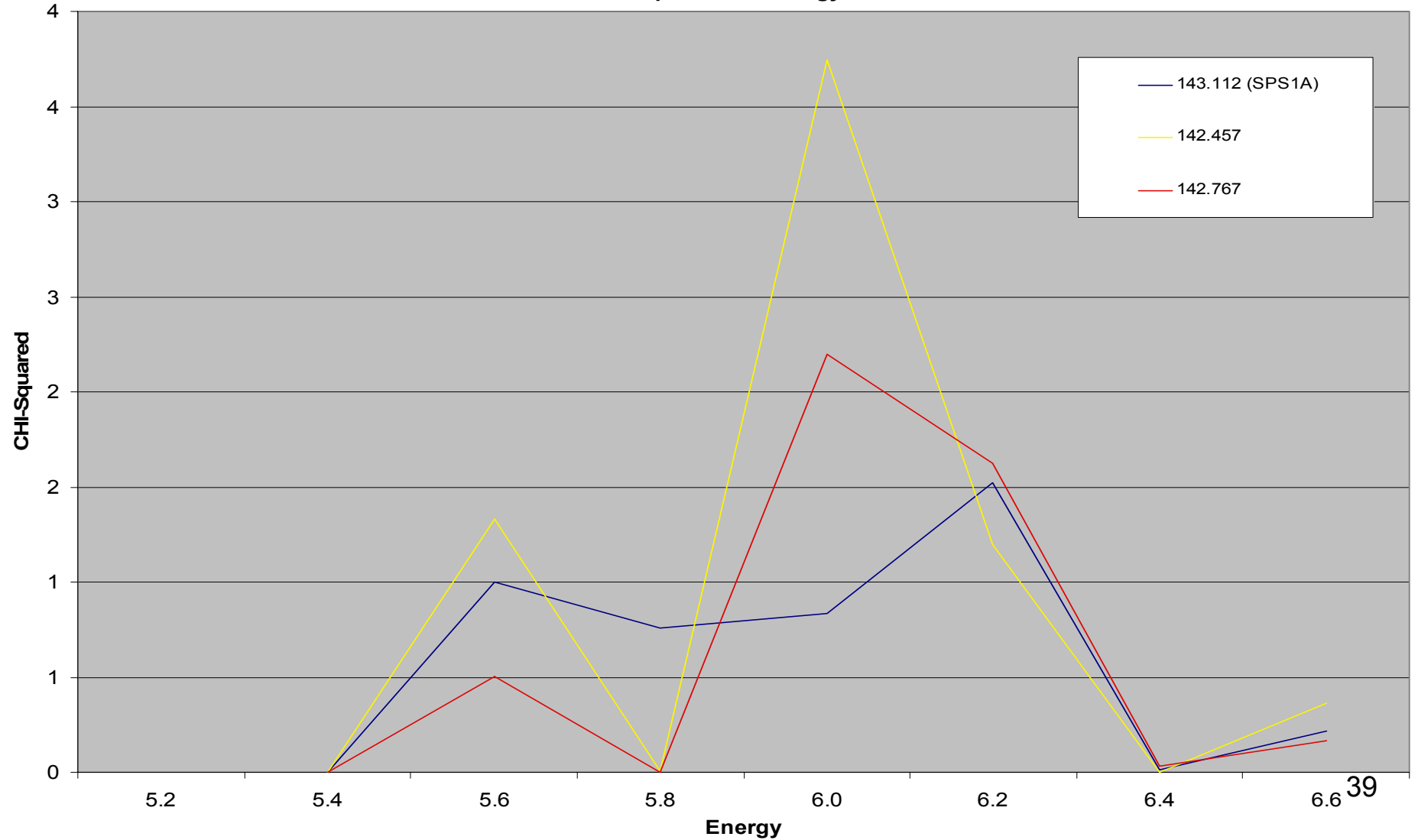




Lower Endpoint

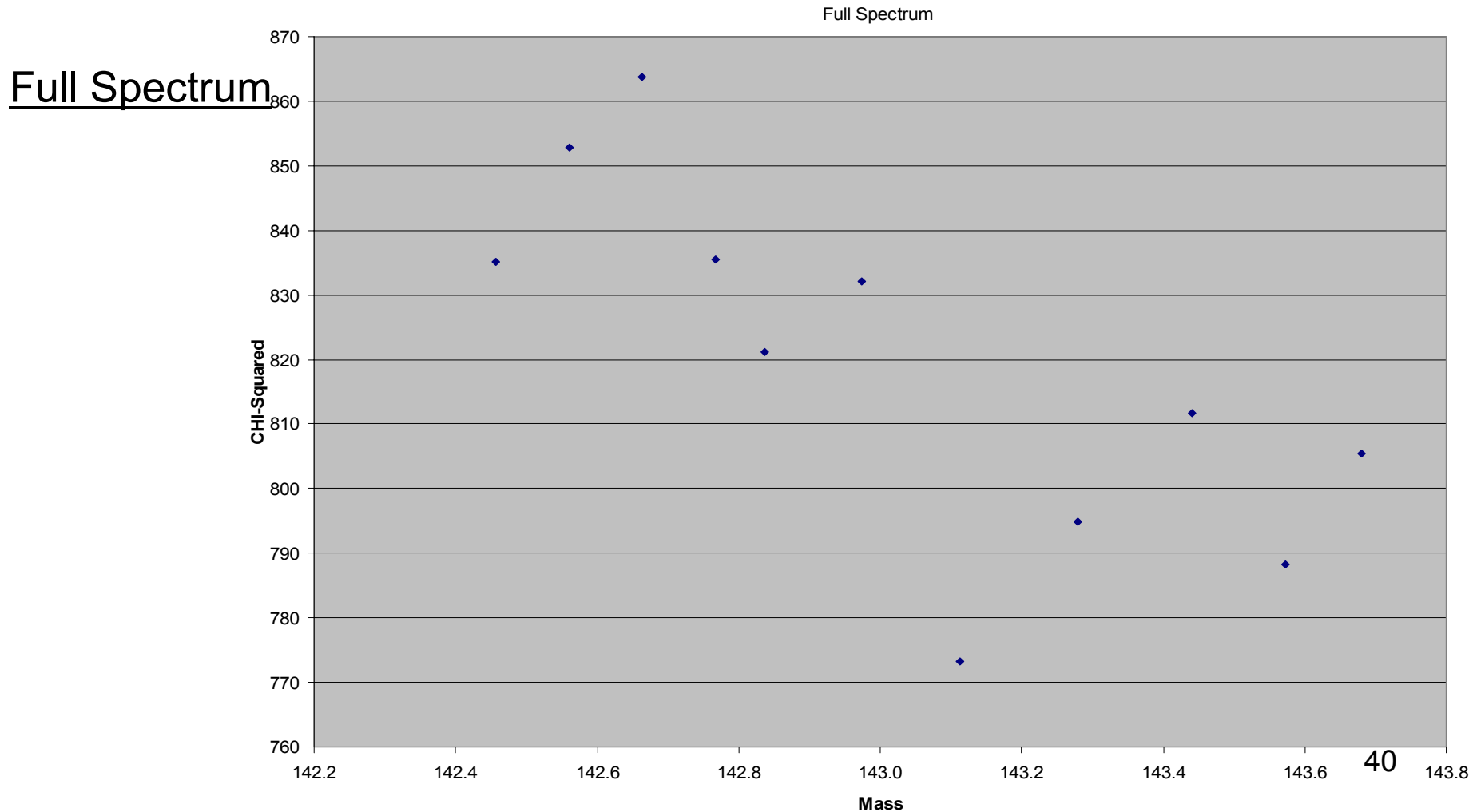
CHI-squared

CHI-Squared vs. Energy





Testing the endpoint isolation technique again.... (smear)

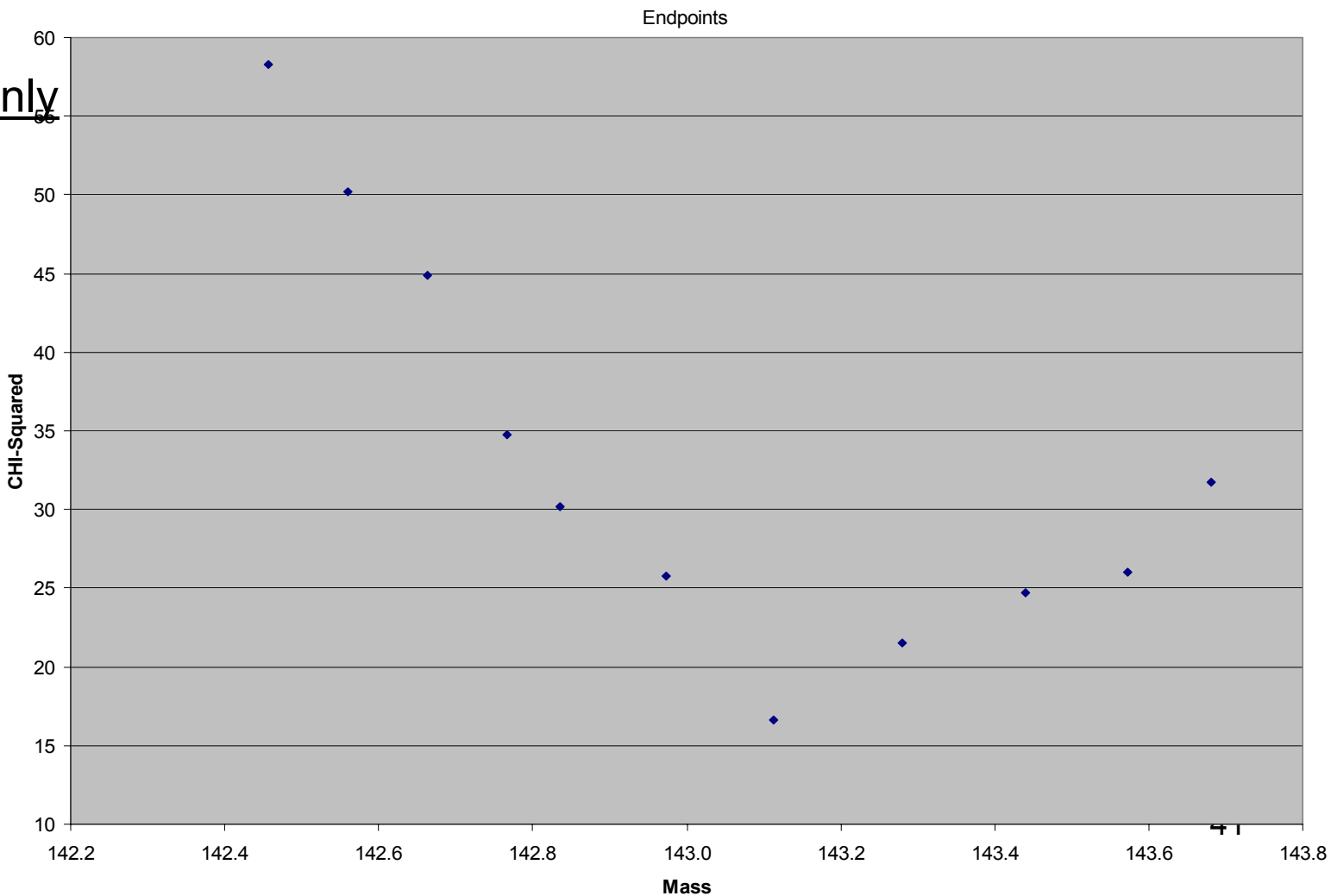




International Linear Collider

Holy COW !!!!!!!!!!!!!!!

Endpoints Only



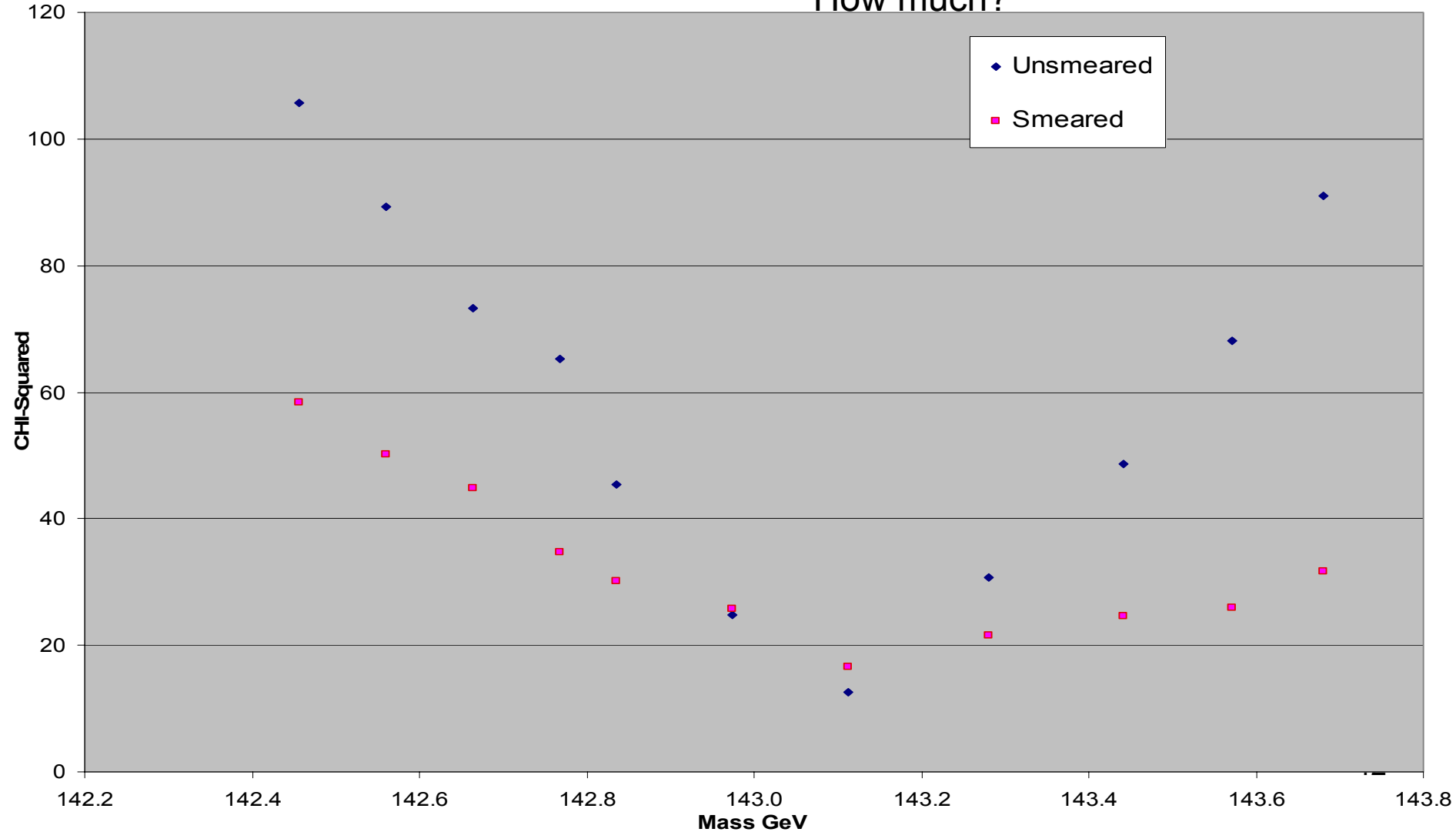


International Linear Collider

Clearly smearing has some negative effects on the CHI -Squared resolution.

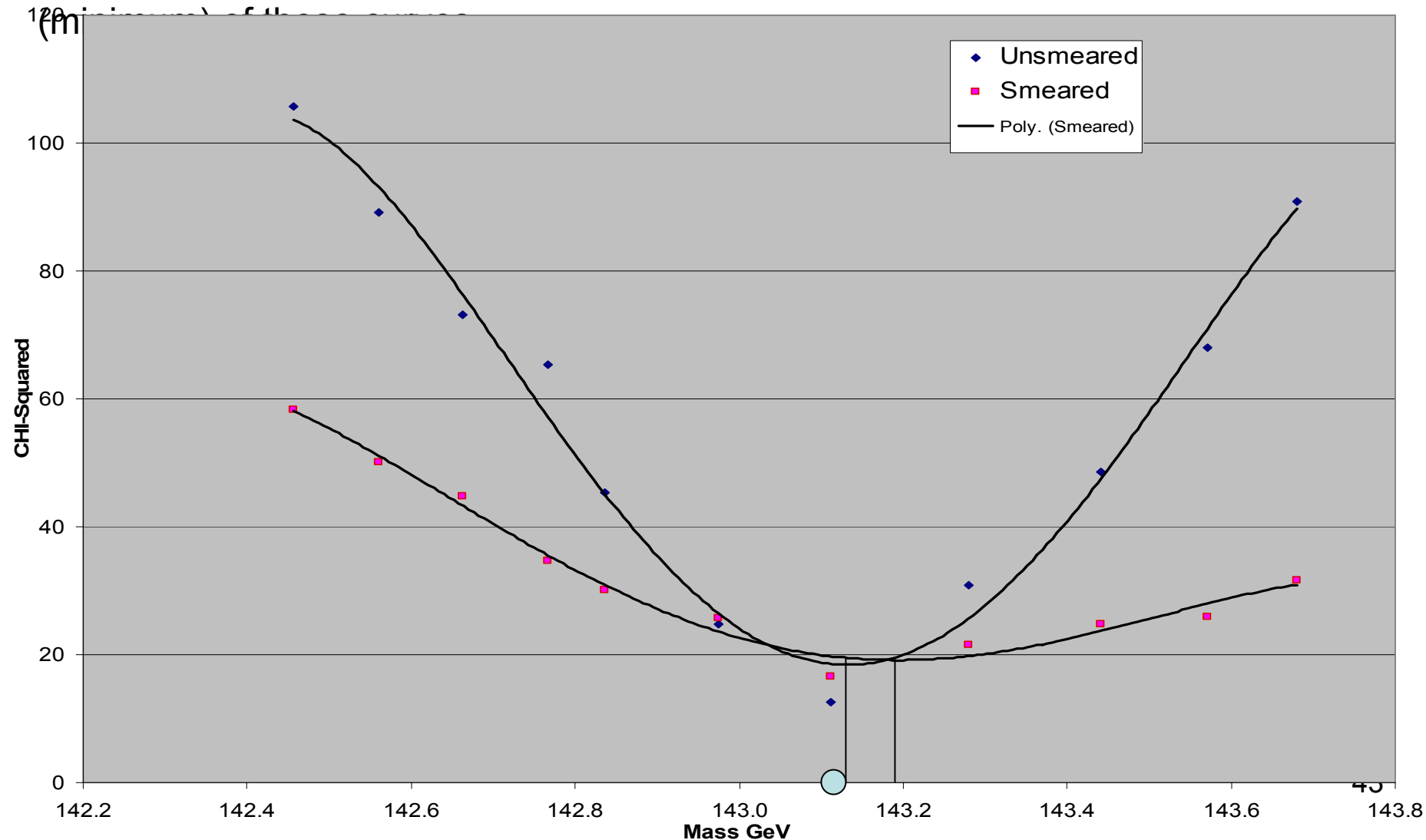
Smeared vs. Unsmeared

How much?



Comparing steepness of CHI-Square curves is a comparison of resolution. If a curve is shallow, it is an indicator that resolution will not be as good as one that is steep. We can fit a quartic to this distribution and compare the fitted masses

Smeared vs. Unsmeared





Calculating the resolution/error

This CHI-Squared fitting process is repeated 120 times and the fitted mass is the minimum of these curves. The resolution/error is the RMS of these masses.

Results are cross checked by binning and fitting to
a

Gaussian. The error is the width, and is in agreement with the RMS.



Points of Interest

12 Scenarios are investigated.

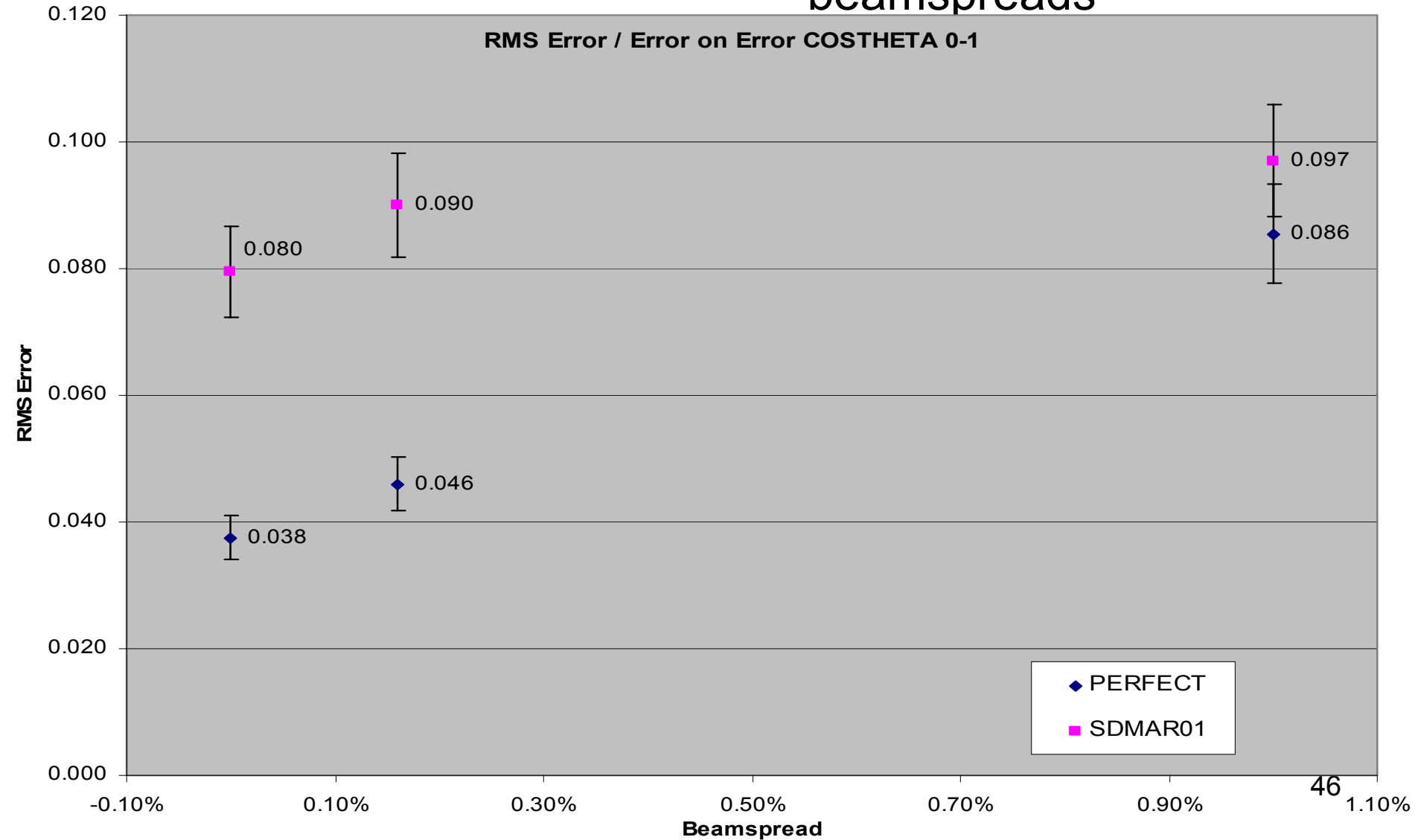
- a perfect detector (unsmearred) and sdmar01
- $\cos(\theta)$ 0 –1 (full region) , 0–.8 (only central region)
- beamspreads of 0% , .16% , 1%



International Linear Collider

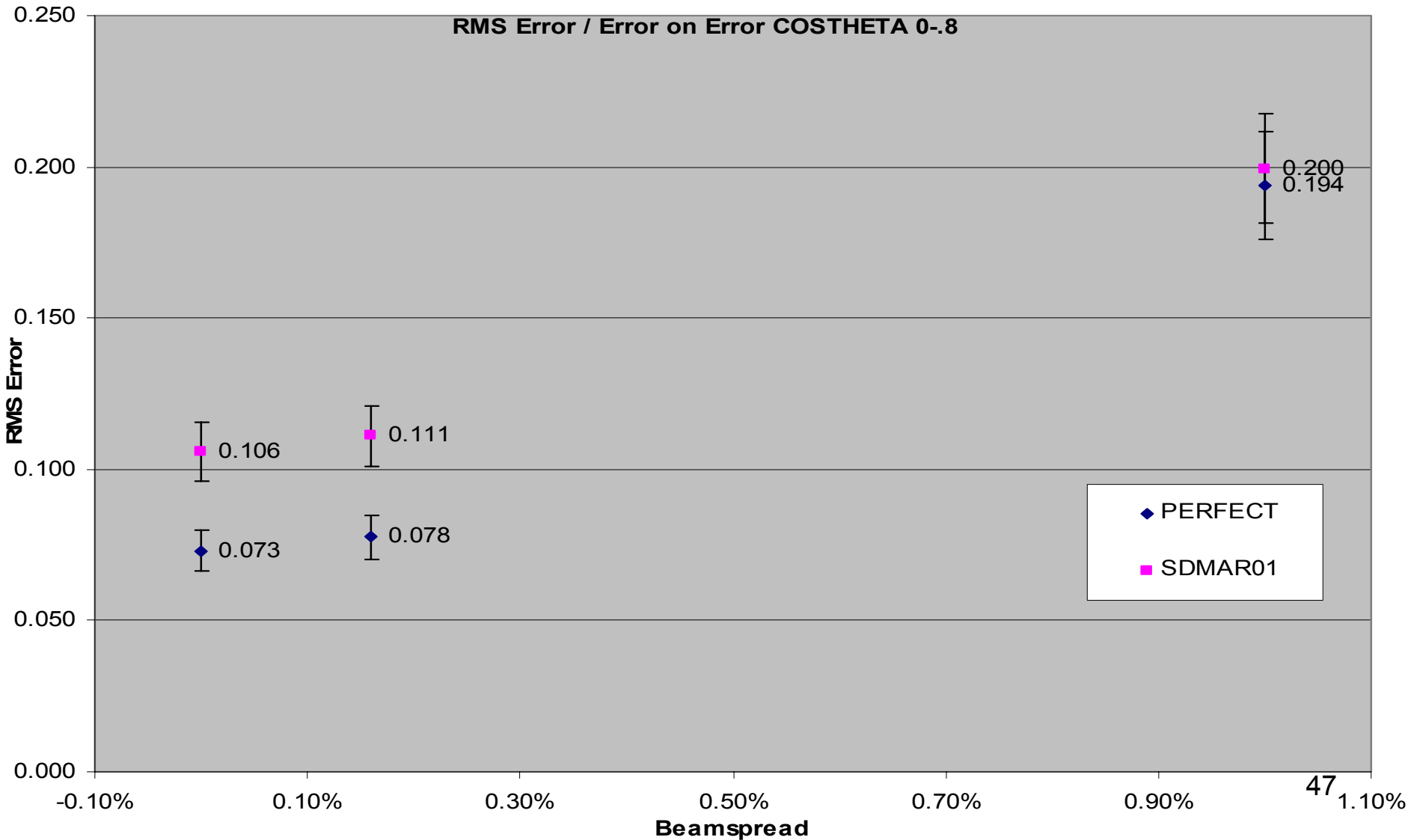
Resolution improves nearly 2* from from SDMAR01 to PERFECT for realistic beamspreads

RMS Error / Error on Error COSTHETA 0-1





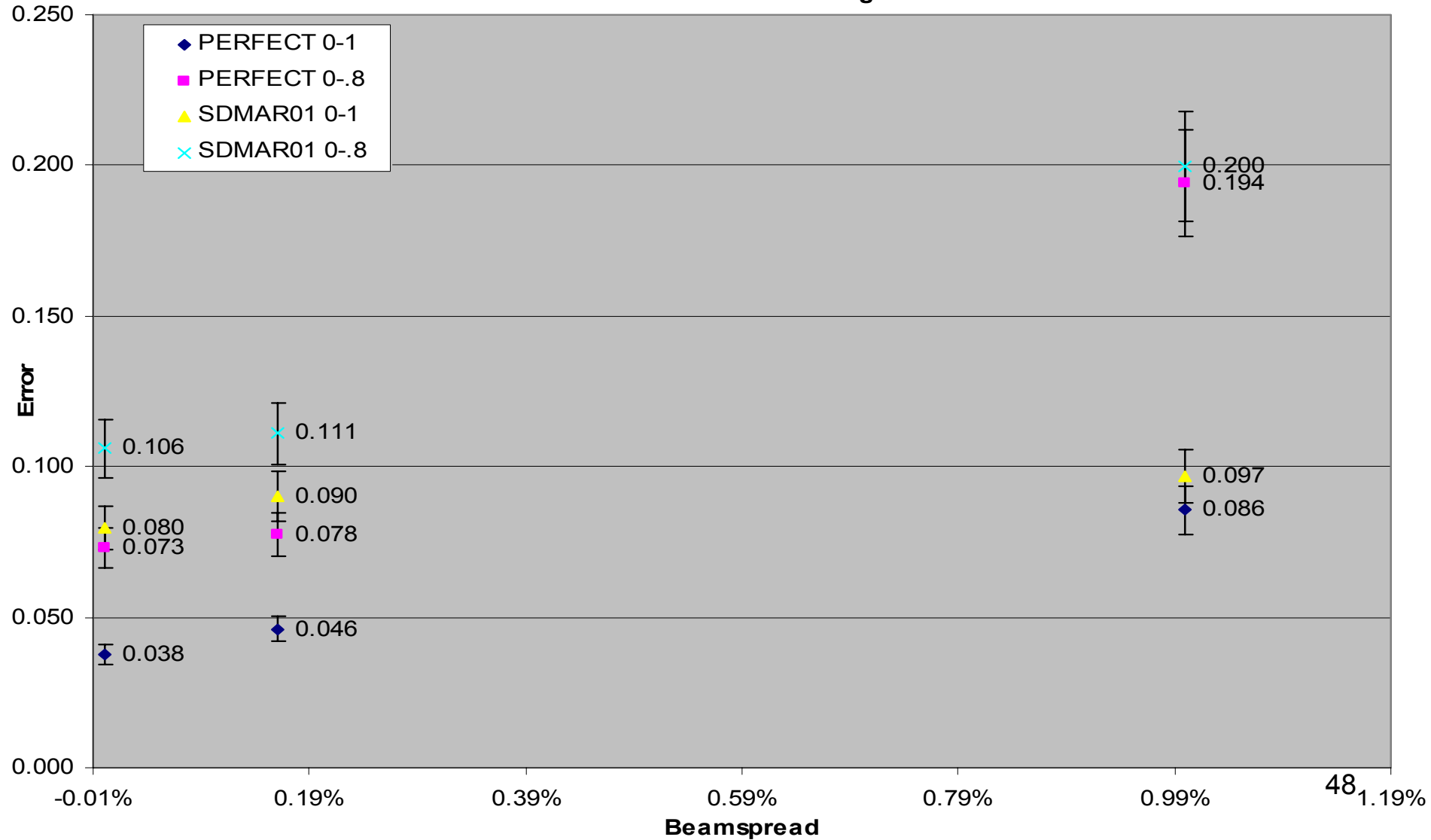
Fit error degrades when investigating only the central region.





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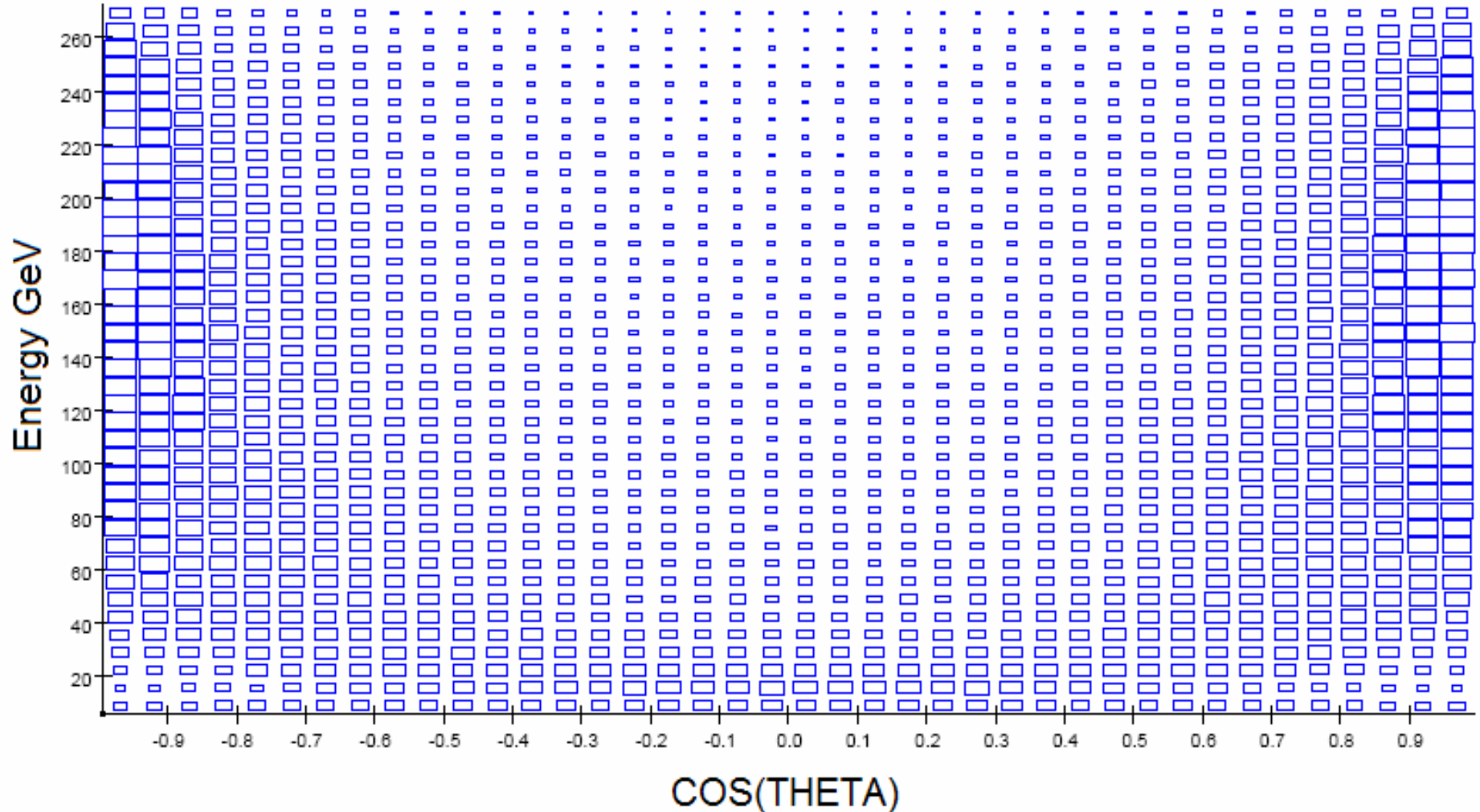
Error for COSTHETA Ranges





The significant resolution improvement in the full-region over just central is explained by the significant amount of statistics to be gained from using the forward direction at the upper endpoint.

SUSY: PARTICLE COSTHETA VS ENERGY (cuts)





Conclusions

- Selectron detection over $\cos(\theta)$ 0–1 range improves error $\cos(\theta)$ 0–.8 for all beamsread conditions.
- SDMAR01 detector design is **NOT** optimal for resolving selectron mass at low (realistic) beamsreads. The differences are significant over the full range and measurable over the central region.
- .16% Beamsread has small effect compared to smearing
- Previous studies (not by us) show no negative detector effects in central region at 1% beamsread. Our results confirm this.



Outlook

- New detector simulations are currently being produced and analyzed.
- Future studies will be a 2-dimensional bowl fit which predicts resolutions of both the right handed selectron and the \tilde{X}^0_1 LSP.