

The Ups and Downs of B Mixing and Lifetimes

- Measurements

- Average B lifetime (1993-1995)
- B^+ and B^0 lifetimes (1994-2000)
- B^0 mixing (1995-...)
- B_s mixing (1996-...)

People

- Direct contributors (1993-now)

Ken Baird

Mourad Daoudi

Danning Dong

Mike Fero

Gary Gladding

Kazumi Hasuko (PhD)

Jenny Huber

Dave Jackson

John Jaros

Cheng-Ju Lin (PhD)

Ming Liu (PhD)

Inga Karliner

Nety Krishna

Steve Manly

Tom Markiewicz

Thomas Moore (PhD)

Homer Neal

Bob Panvini

Greg Punkar

Sumit Sen (PhD)

Nick Sinev

Julia Thom (PhD soon)

Tracy Usher

Stéphane Willocq

Jodi Wittlin (PhD)

Geordie Zapalac

(apologies to those who have
been left off this list)

Average B Lifetime (I)

- Back in 1993:

- ◆ Surprisingly large lifetime $\Rightarrow |V_{cb}|$ is small

- ◆ LEP exploits silicon vertex detectors

- \Rightarrow Measured average B lifetime moves a lot

- ◆ At SLD: 2 “traditional” analyses

- Impact parameter of all tracks opposite b-tagged jets

- Summed impact parameter

- \Rightarrow Exploit SLD 3-D CCD vertex detector

- to develop inclusive topological vertexing

Average B Lifetime (II)

- Desire to exploit 3-D CCD vertex detector led to the *first application of topological vertexing* by S.Manly (1994)

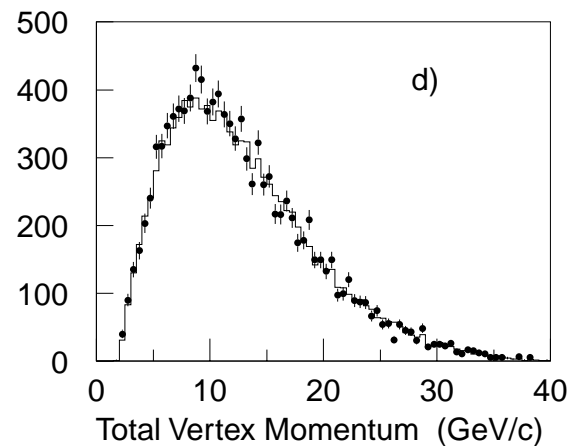
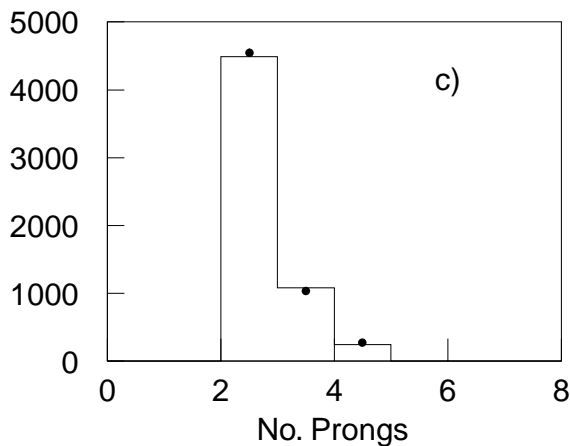
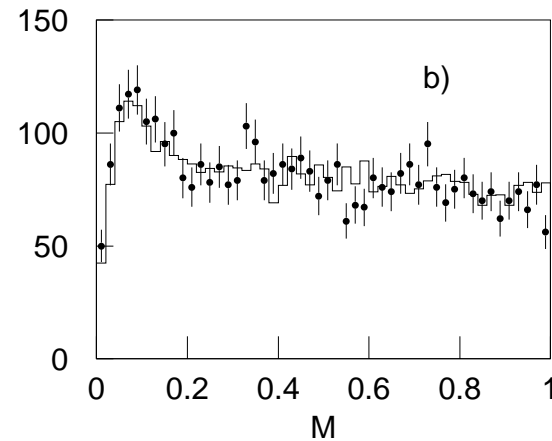
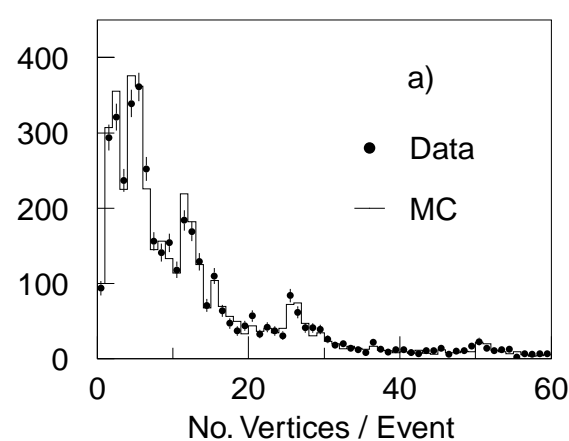
2D impact param tag

$$\varepsilon_b = 60\% \quad \Pi_b = 90\%$$

Select partition with largest Π $\text{prob}(\chi^2, \text{dof})$

1993 data: 50K evts

Select ~ 2500 decay candidates



Average B Lifetime (III)

- First results: summer 1994 (S.Manly, S.Sen, S.Willocq)

Published: PRL 75, 3624 (1995)

1993 data sample: 50K evts

Fit to inclusive vertex
decay length distribution

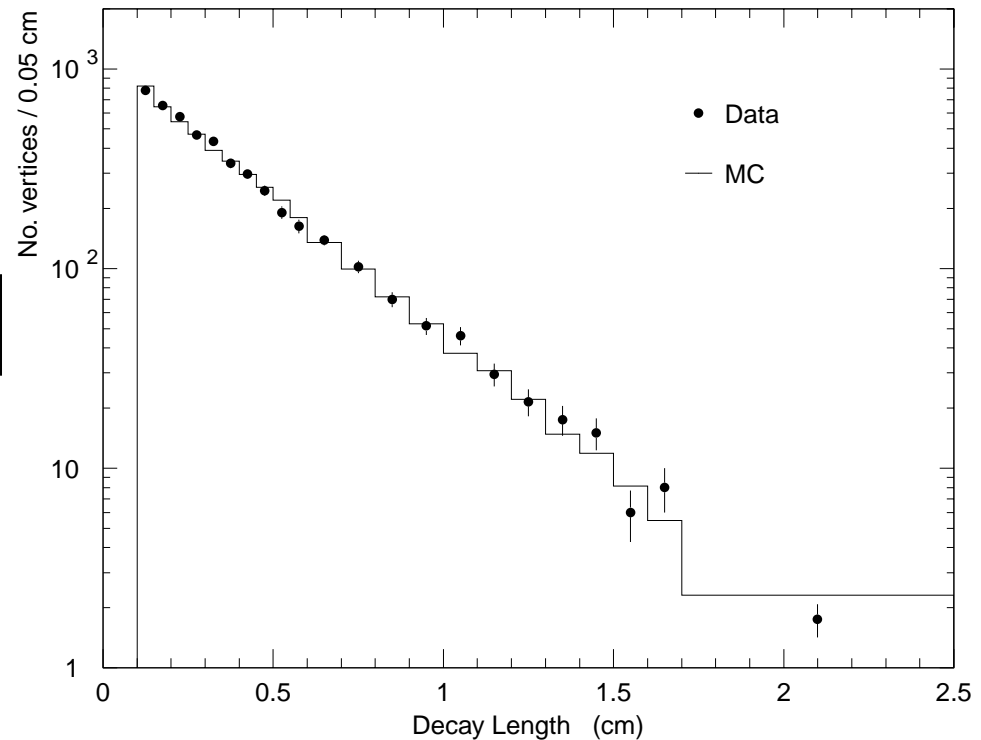
$$\tau_B = 1.564 \pm 0.030 \pm 0.037 \text{ ps}$$

More powerful than

Impact-parameter methods:

$$(\delta) \quad 1.617 \pm 0.048 \pm 0.086 \text{ ps}$$

$$(\Sigma\delta) \quad 1.627 \pm 0.054 \pm 0.132 \text{ ps}$$



Average B Lifetime (IV)

- Latest world average

$$\tau_B = 1.564 \pm 0.014 \text{ ps}$$

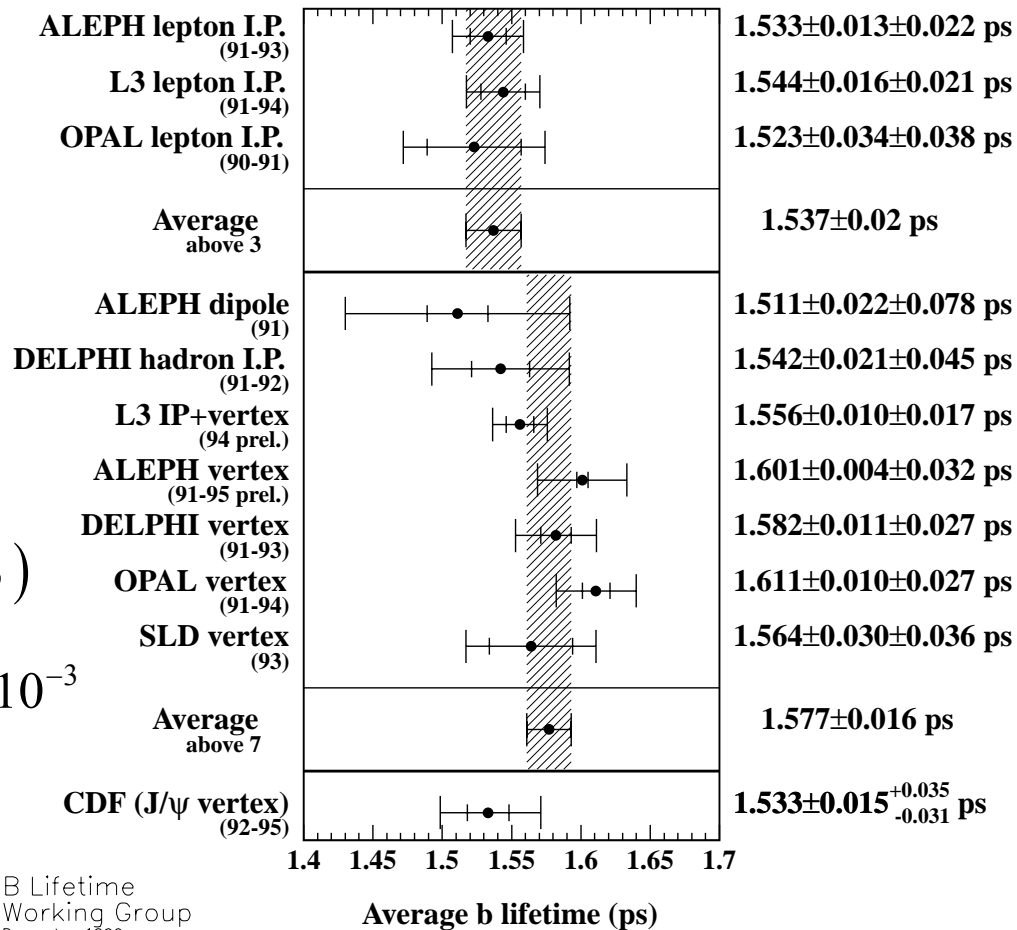
- Determination of V_{cb}

From τ_B and semileptonic branching fraction (Bigi, Shifman, Uraltsev)

$$|V_{cb}| = 0.0411 \sqrt{\frac{1.55}{0.105} \Gamma(b \rightarrow lvX) \cdot (1 + \delta)}$$

$$= [40.76 \pm 0.41(\text{exp}) \pm 2.04(\text{theo})] \times 10^{-3}$$

δ is few percent correction



B Lifetime Working Group
December 1999

B⁺ and B⁰ Lifetimes (I)

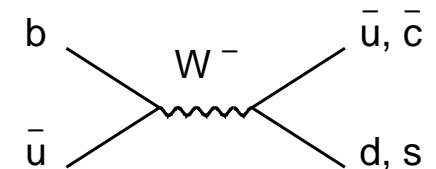
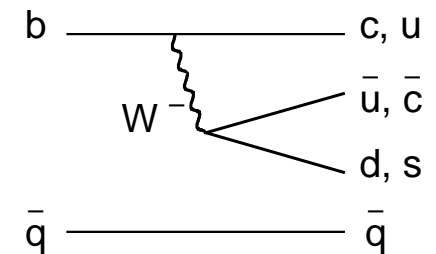
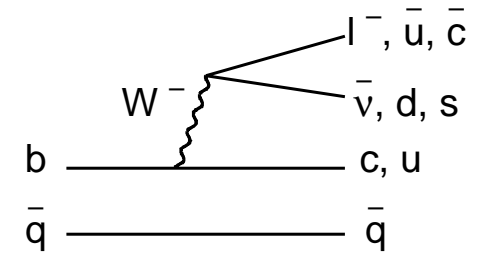
- Test b-decay transitions and dynamics (strong interaction)
- Heavy Quark Expansion predicts small differences between b-hadron types

$$\tau(B^+) / \tau(B^0) = 1 + O(5\%)$$

$$0.9 < \tau(\Lambda_b) / \tau(B^0) < 1.0$$

Bigi et al.

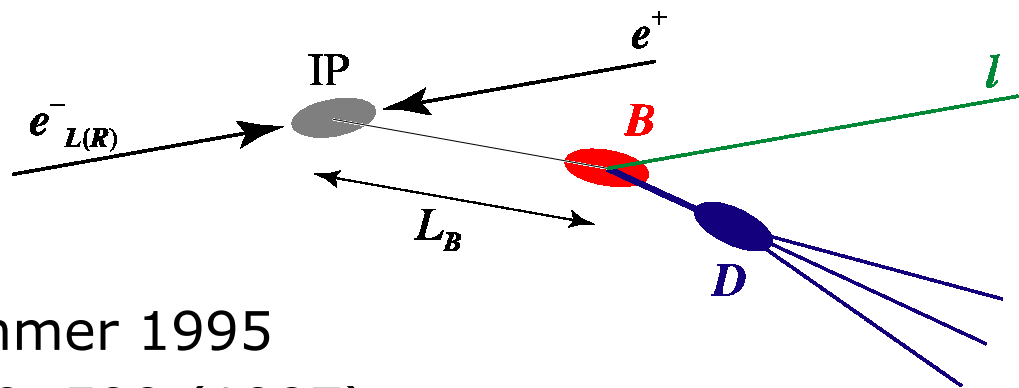
(somewhat contested by Neubert)



B⁺ and B⁰ Lifetimes (II)

- Refined *methods all based on vertexing* (1994):

1. Lepton+D (G.Gladding, I.Karliner, T.Usher)



First results: summer 1995

Published: PRL 79, 590 (1997)

1993-95 data sample: 150K evts

$$\tau(B^+) = 1.61 \pm 0.13 \pm 0.07 \text{ ps}$$

$$\tau(B^0) = 1.56 \pm 0.14 \pm 0.10 \text{ ps}$$

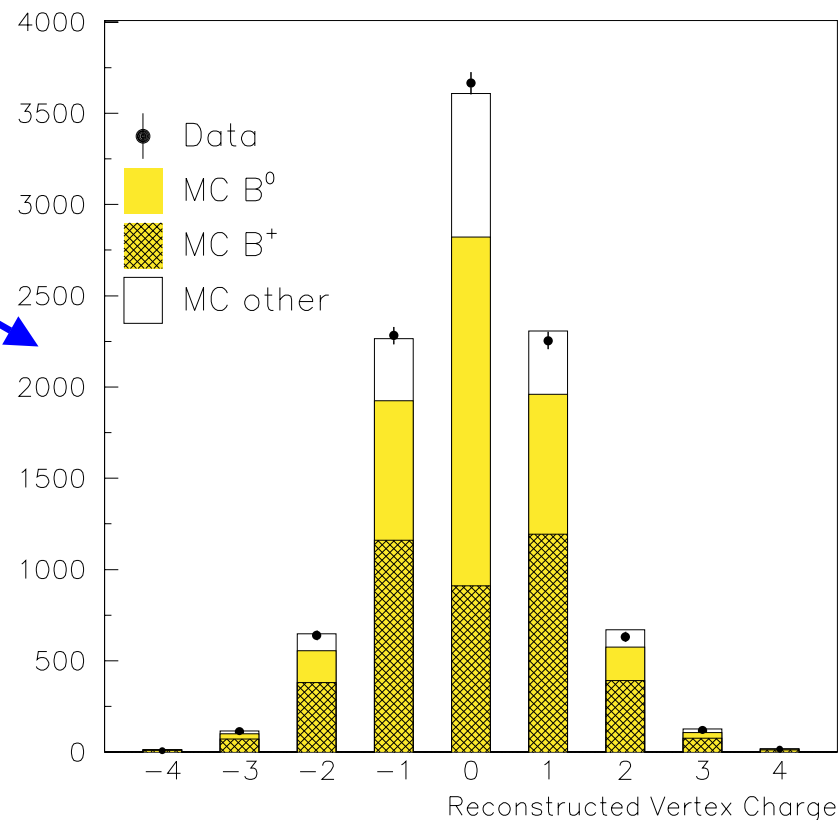
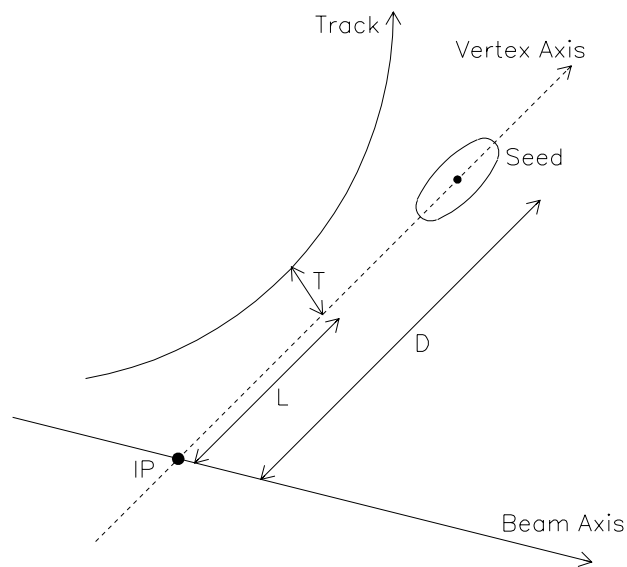
$$\tau(B^+) / \tau(B^0) = 1.03 \pm 0.15 \pm 0.09$$

B⁺ and B⁰ Lifetimes (III)

2. Inclusive topological vertexing (D.Jackson)

first development and implementation of ZVTOP

- Select *seed* vtx with high track overlap density
- Attach tracks with $L/D > 0.3$ and $T < 0.1$ cm
- Lower quality tracks also attached to improve vtx charge



B⁺ and B⁰ Lifetimes (IV)

First results: summer 1995

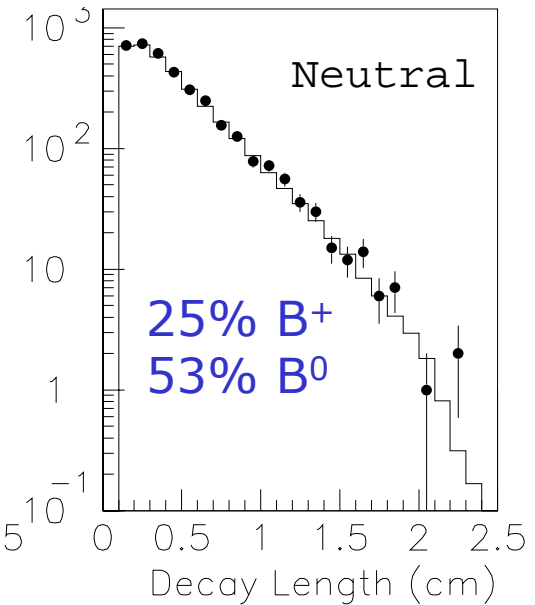
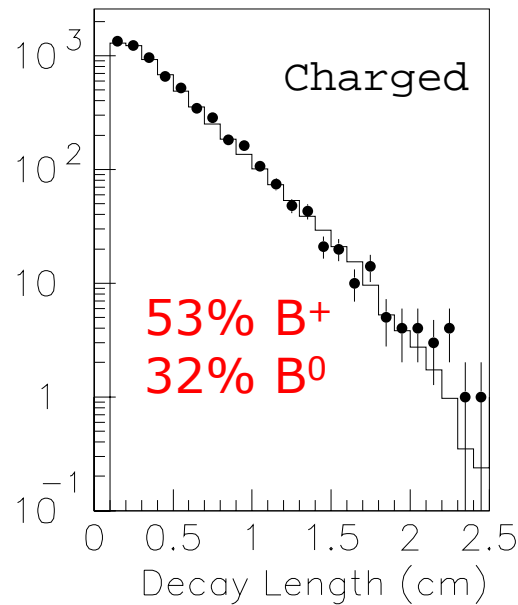
Published: PRL 79, 590 (1997)

1993-95 data sample: 150K evts

Topological analysis

9719 candidate B decays

B purity = 98%



$$\tau(B^+) = 1.67 \pm 0.07 \pm 0.06 \text{ ps}$$

$$\tau(B^0) = 1.66 \pm 0.08 \pm 0.08 \text{ ps}$$

$$\tau(B^+) / \tau(B^0) = 1.01 \pm 0.09 \pm 0.05$$

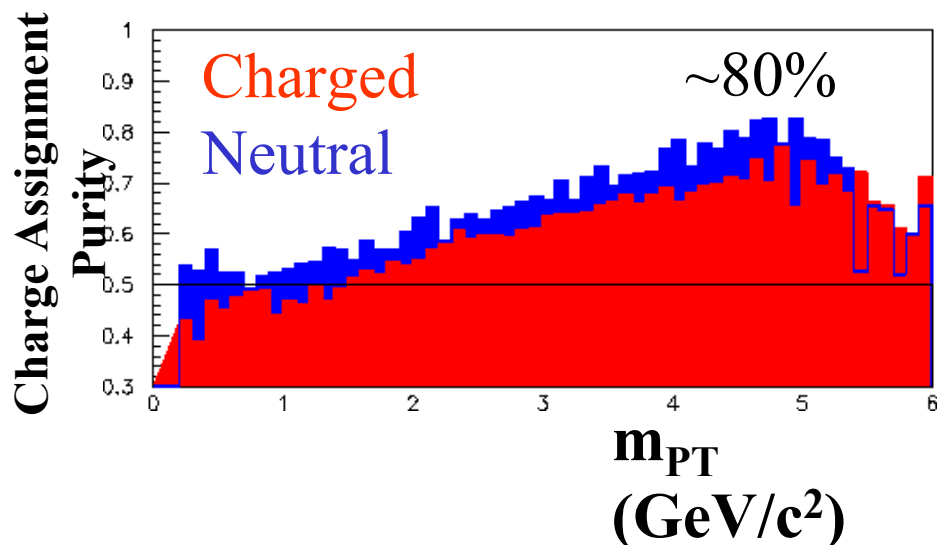
B⁺ and B⁰ Lifetimes (V)

Latest prelim results: summer 1999 (K.Baird, D.Jackson)

[SLAC-PUB-8206]

1997-98 data sample: 350K evts

→ Use additional information to determine probability that the charge assignment is correct: vertex mass, P_{e^-} , Q_{jet}



$$\tau(B^+) = 1.613 \pm 0.023 \text{ ps}$$

$$\tau(B^0) = 1.565 \pm 0.024 \text{ ps}$$

$$\tau(B^+) / \tau(B^0) = 1.030 \pm 0.028$$

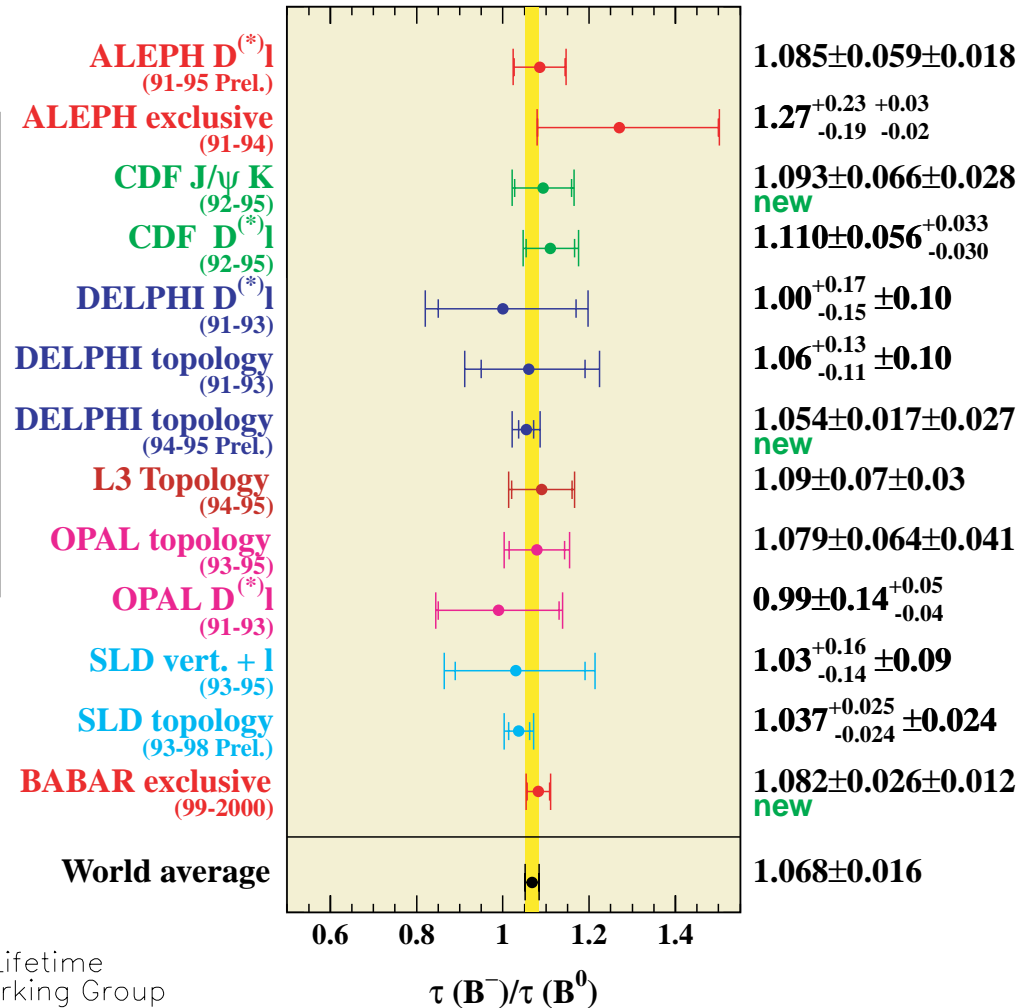
B⁺ and B⁰ Lifetimes (VI)

- For 1993 – 1998 Data:

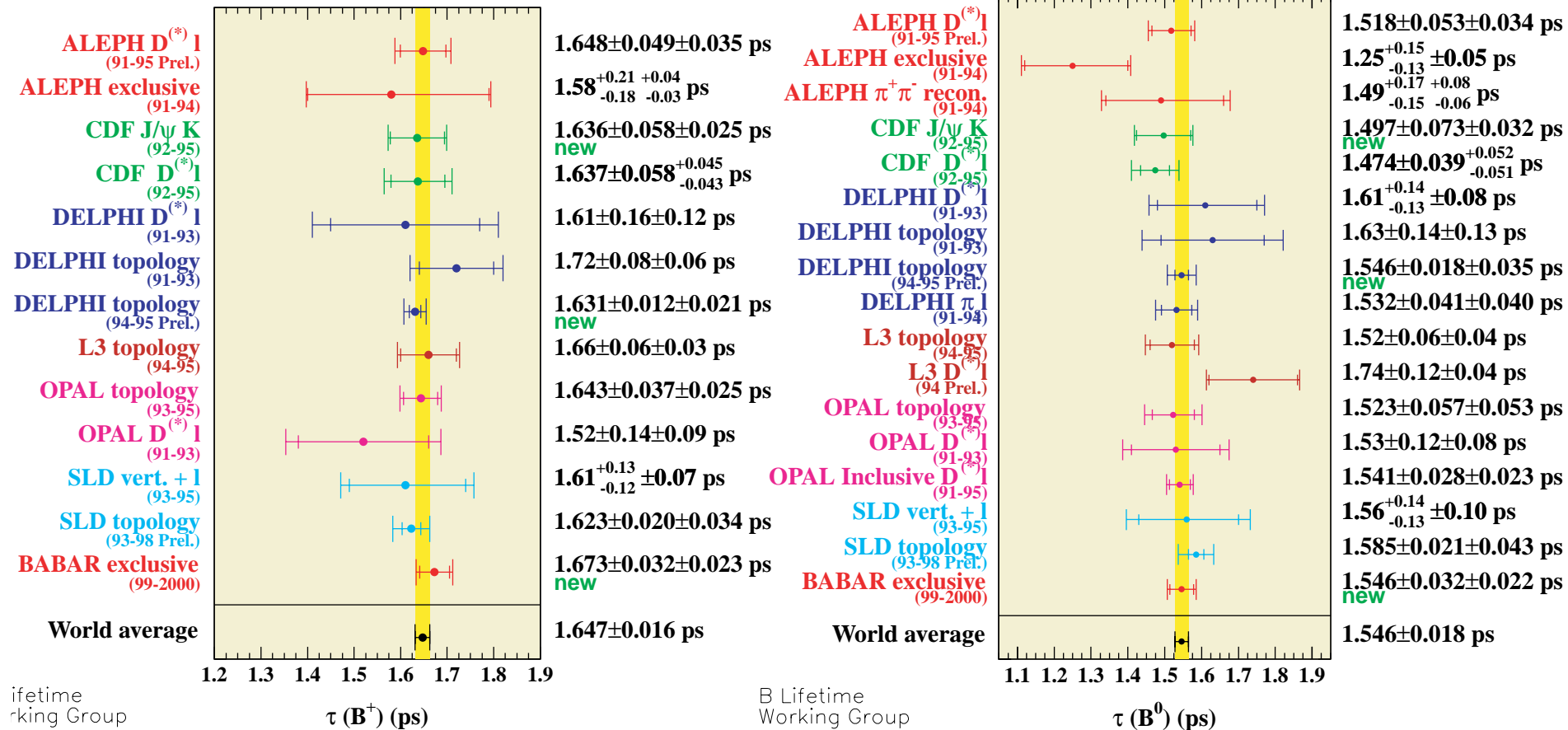
(Preliminary)

$\tau_{B^+} = 1.623 \pm 0.020 \pm 0.034 \text{ ps}$
 $\tau_{B^0} = 1.565 \pm 0.021 \pm 0.043 \text{ ps}$
 $\tau_{B^+}/\tau_{B^0} = 1.037^{+0.025}_{-0.024} \pm 0.024$

**Latest world average
 shows clear evidence for
 difference between
 B⁺ and B⁰ lifetimes**

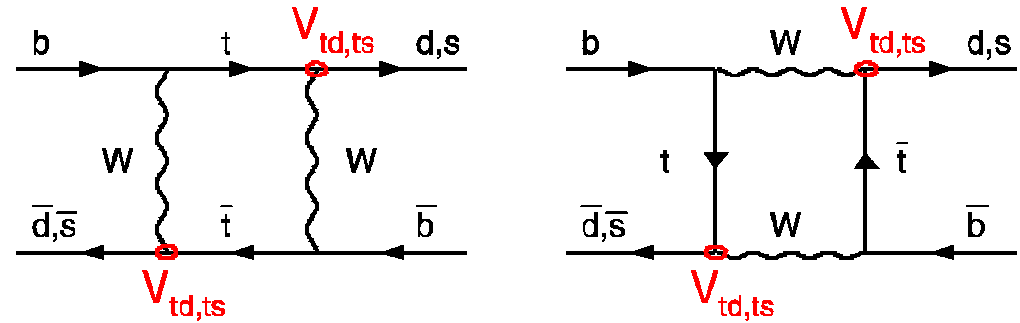


B⁺ and B⁰ Lifetimes (VII)



B⁰ Mixing (I)

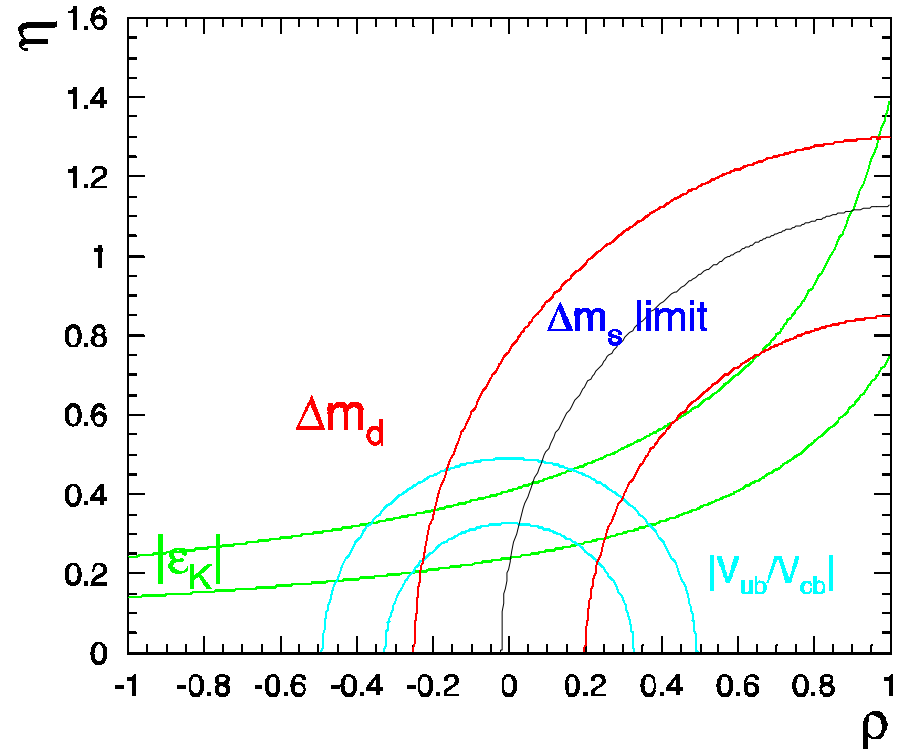
- B⁰ ↔ B⁰ transitions occur via second order weak interactions



- Time-dependent oscillations with frequency $\Delta m_d \propto |V_{td}|^2$

$$\Delta m_d = \frac{G_F^2}{6\pi^2} m_{B_d} m_t^2 F\left(\frac{m_t^2}{m_W^2}\right) \times B_{B_d} f_{B_d}^2 \eta_{QCD} |V_{tb}^* V_{td}|^2$$

⇒ Measure $|V_{td}|$ and constrain CP violation in SM



B⁰ Mixing (II)

- **First results: summer 1996** (M.Fero, D.Jackson, M.Liu, S.Manly, T.Moore, SW)
SLAC-PUBS: 7228, 7229, 7230
1993-95 data sample

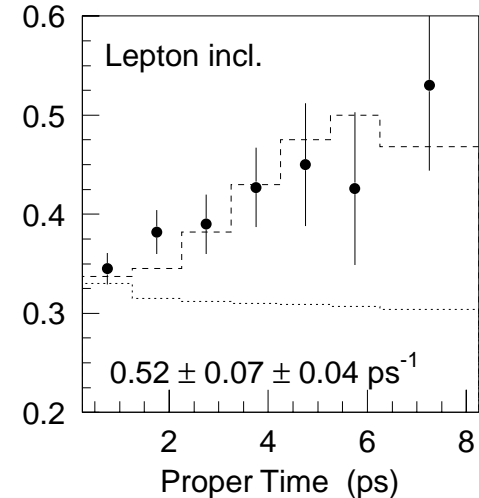
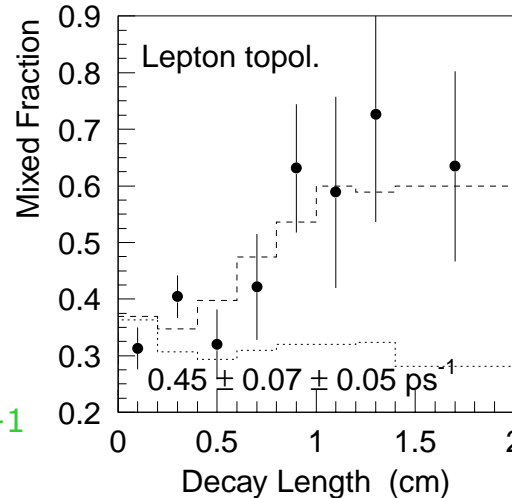
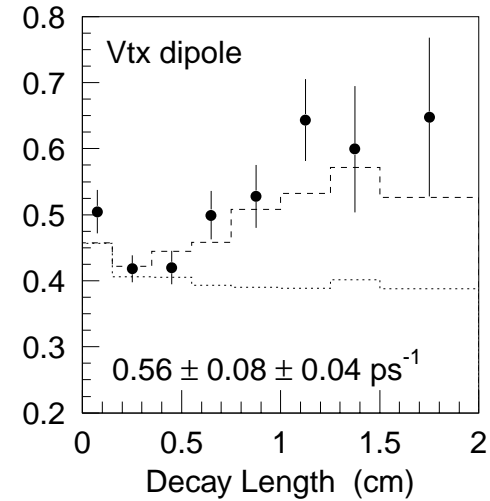
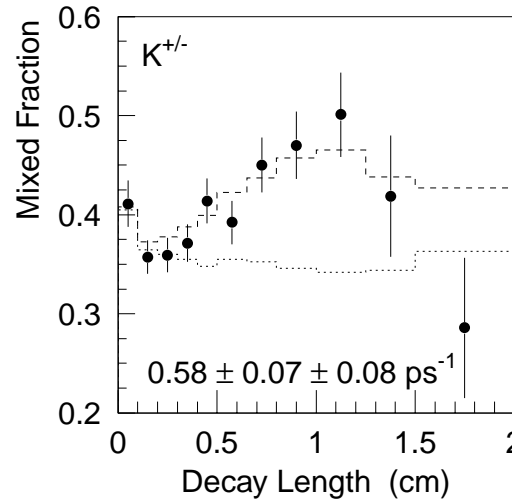
- Adapt lepton+D and topological lifetime analyses
- Tag initial and final B⁰ / \bar{B}^0 flavor

- NEW:** lepton+tracks analysis
initial state tag (Pol+Qjet)
kaon tag
charge dipole tag

SLD avg:

$$\Delta m_d = 0.531 \pm 0.043 \pm 0.034 \text{ ps}^{-1}$$

SLD Preliminary



B⁰ Mixing (III)

- Latest results: summer 2001

1996-98 data sample

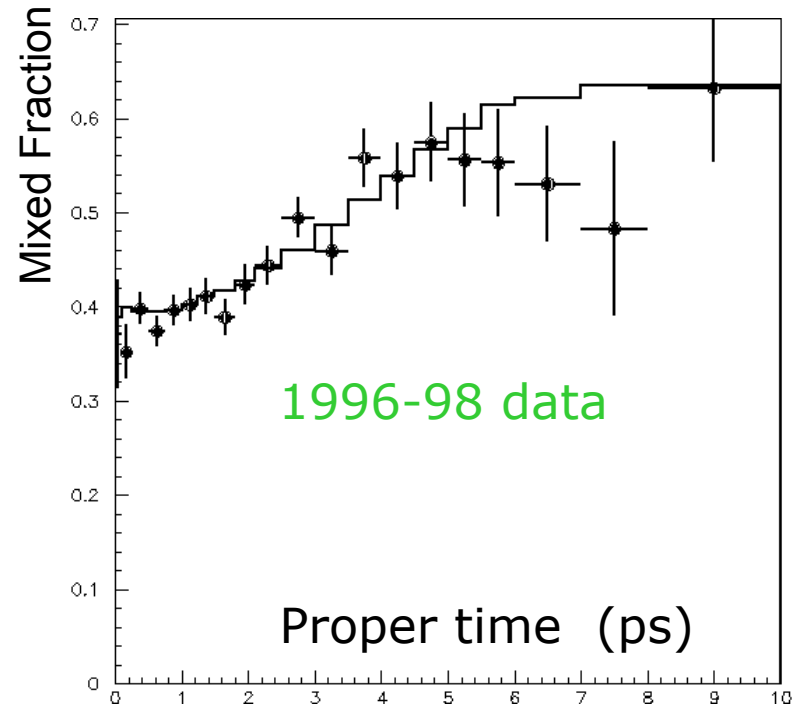
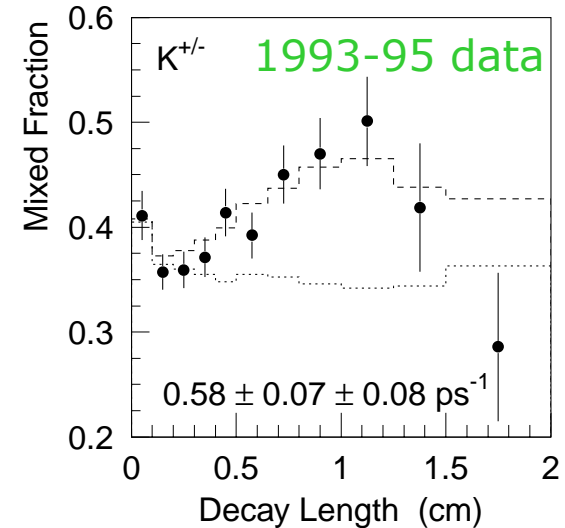
- Revamped **kaon tag analysis** (J.Wittlin)
unbinned likelihood
multi-var initial state tag
VXD-only tracks for b tag
and neutral b-hadron selection

K tag:

$$\Delta m_d = 0.503 \pm 0.028 \pm 0.020 \text{ ps}^{-1}$$

B⁰ K tag RSF = 0.797 ± 0.022

⇒ Much reduced K tag systematics



B⁰ Mixing (IV)

- Summer 2001 world avg:

$$\Delta m_d = 0.489 \pm 0.008 \text{ ps}^{-1}$$

Precise measurement but...

Extraction of $|V_{td}|$ from Δm_d

is affected by a $\sim 20\%$

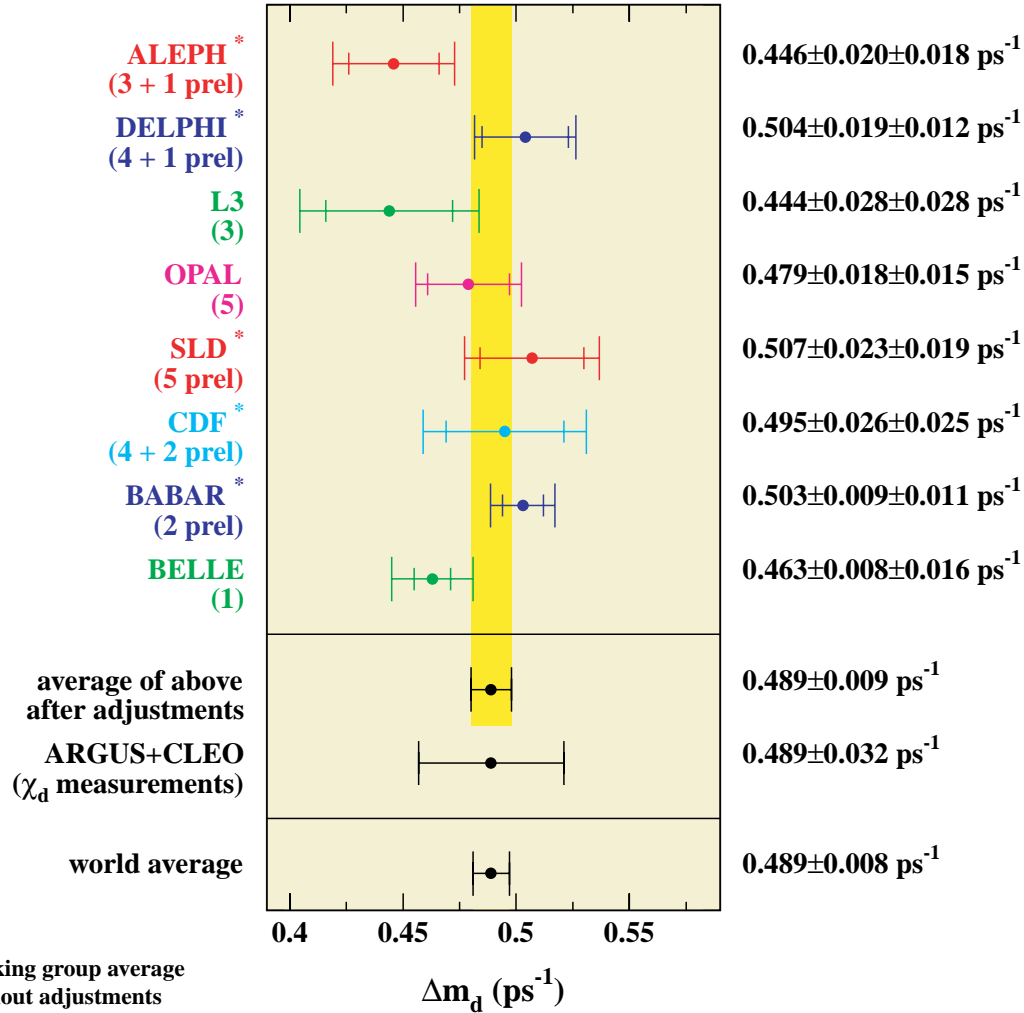
uncertainty in $\sqrt{B_{B_d} f_{B_d}}$

⇒ Study B_s mixing to measure

$$\frac{\Delta m_s}{\Delta m_d} = \frac{m_{B_s} f_{B_s}^2 B_{B_s}}{m_{B_d} f_{B_d}^2 B_{B_d}} \cdot \left| \frac{V_{ts}}{V_{td}} \right|^2$$

$$= \frac{m_{B_s}}{m_{B_d}} \cdot (1.16 \pm 0.05)^2 \cdot \left| \frac{V_{ts}}{V_{td}} \right|^2$$

* working group average without adjustments



B_s Mixing (I)

Significance for B_s mixing signal:

$$S = \sqrt{\frac{N}{2}} f_{B_s} (1-2w) e^{-\frac{1}{2}(\Delta m_s \sigma_t)^2}$$

statistics

B_s purity

mistag

resolution

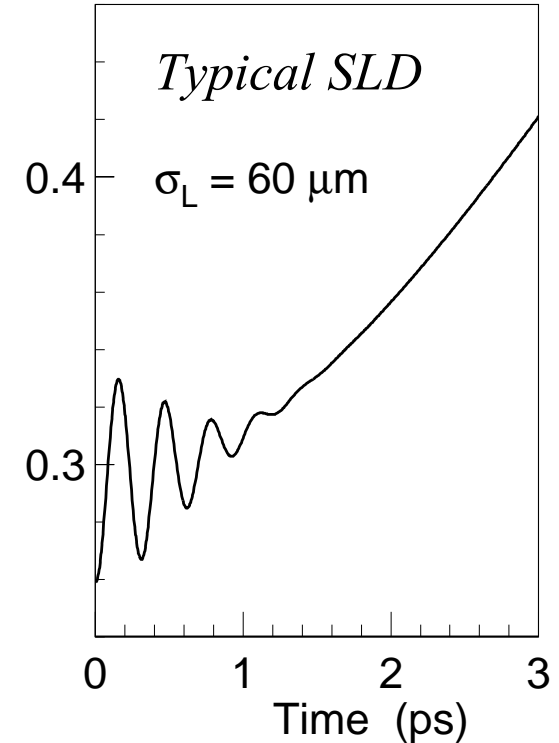
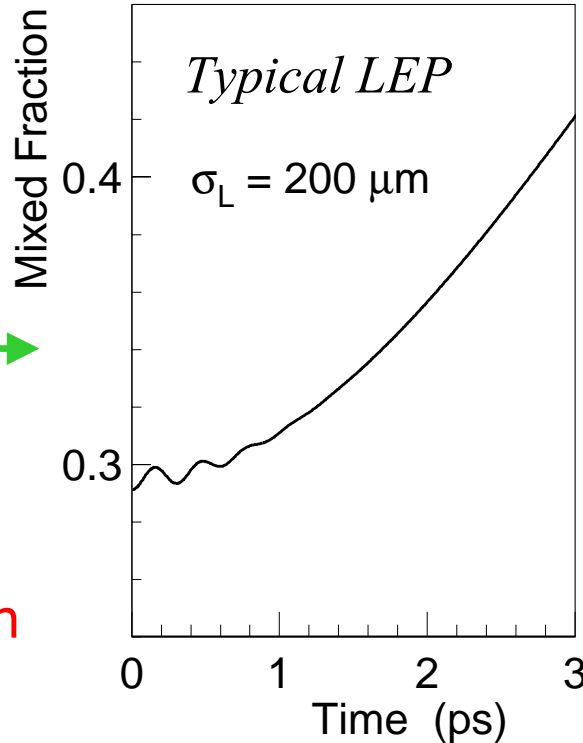
Small IP + CCD VXD
+ Polarization + PID
ALL IMPORTANT

$$\Delta m_s = 20 \text{ ps}^{-1}$$

$$f(B_s) = 0.18$$

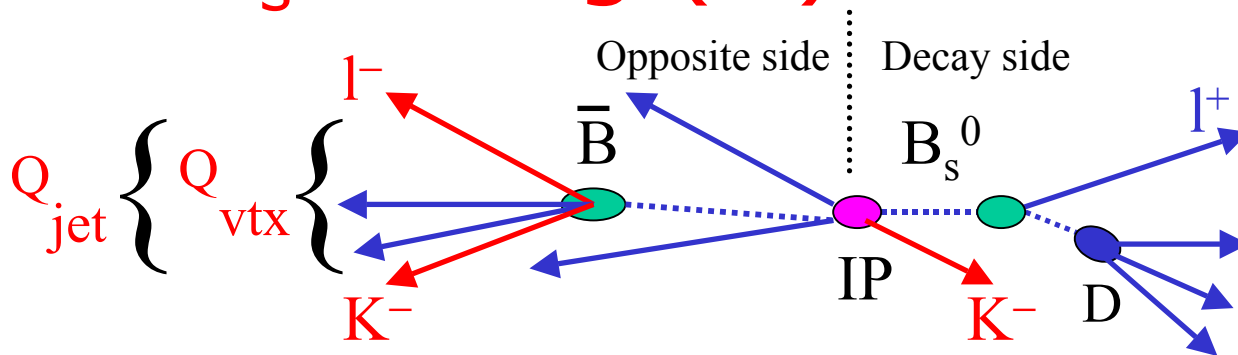
$$w = 0.25$$

$$\sigma_p / p = 0.10$$



Decay length resolution
is critical

B_s Mixing (II): Initial State Tag



❖ Polarized F-B Asymmetry ($w = 0.28$)

❖ Opposite Side Tags

Lepton charge $b \rightarrow l^-$

Jet Charge $\sum_{\text{tracks}} Q_i |p_i \cdot T|^\kappa$

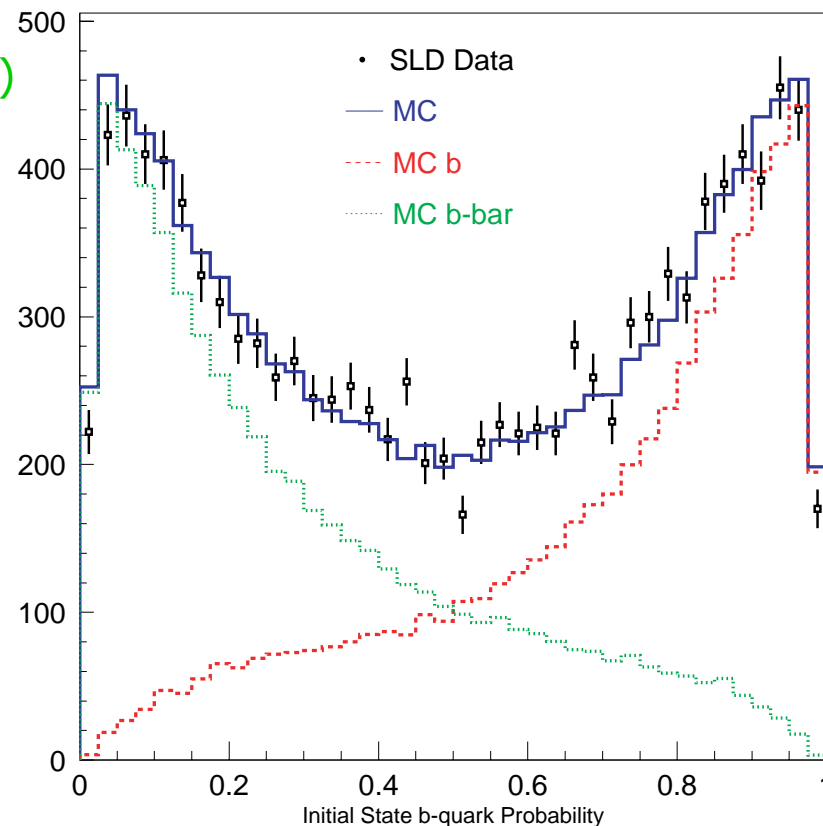
Secondary vtx charge Q_{vtx}

Kaon charge $b \rightarrow c \rightarrow s$ (i.e. K⁻)

Dipole charge

→ Combined with NN (T.Moore)

Overall mistag rate $w \approx 0.22-0.25$



B_s Mixing (III)

- Total of *3 different analyses* at SLD using 400K hadronic Z decays (1996-98 data) Differing in proper time recon and B⁰ \bar{B}^0 decay flavor tag

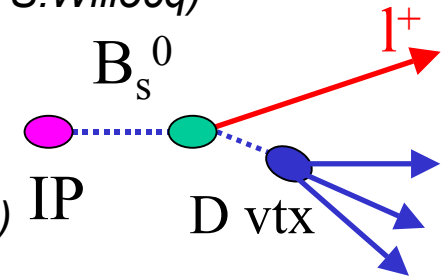
1) Inclusive

Fully inclusive: secondary & tertiary topological vtx

Charge Dipole: 11462 decays (D.Jackson, J.Thom, S.Willocq)

Semileptonic decays: lepton + topological D vtx

Lepton+D: 2087 decays (H.Neal, T.Usher, K.Hasuko)

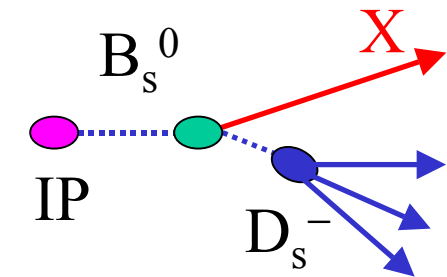


2) Semi-exclusive

Partial reconstruction: B_s → D_s⁻ X
with full reconstruction of D_s decay

$$D_s^- \rightarrow \phi\pi^-, K^{*0}K^-$$

D_s+tracks: 361 decays (C.Lin)



Efficiency ↑
Purity ↓

B_s Mixing with D_s^- + tracks

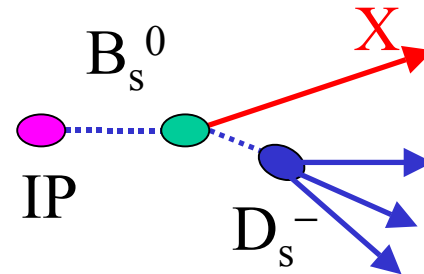
Partial reconstruction of $B_s \rightarrow D_s^- X$

full reconstruction of D_s decay

$$D_s^- \rightarrow \phi\pi^-, K^{*0}K^-$$

particle ID with Cherenkov

Ring Imaging Detector (CRID)



Neural Network D_s selection yields

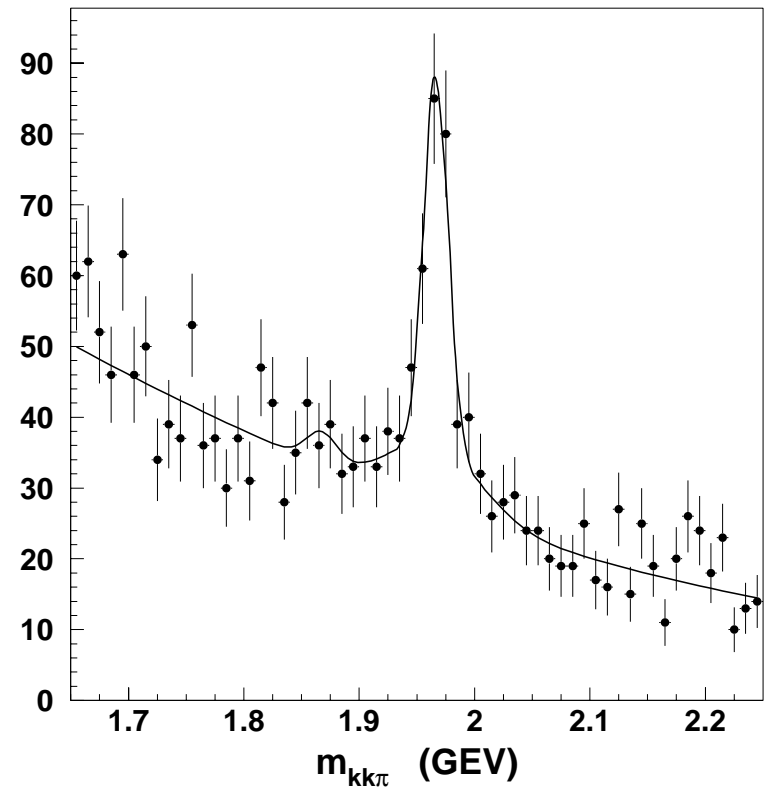
280 $D_s^- \rightarrow \phi\pi^-$ candidates

81 $D_s^- \rightarrow K^{*0}K^-$ candidates

Both $B_s \rightarrow D_s^- l^+ X$ (39 events) and

$B_s \rightarrow D_s^-$ hadrons

are included in the analysis



D_s + tracks analysis (II)

Performance of the analysis:

superb decay length resolution

$\sigma_L = 50 \mu\text{m}$ (60%) & $151 \mu\text{m}$

$\sigma_p / p = 0.08$ (60%) & 0.19

high B_s purity

$f(B_s) = 38\%$ overall

for D_s signal:

$f(B_s) = 65\%$ neutral sample (D_s + hadrons)

90% neutral sample (D_s + lepton)

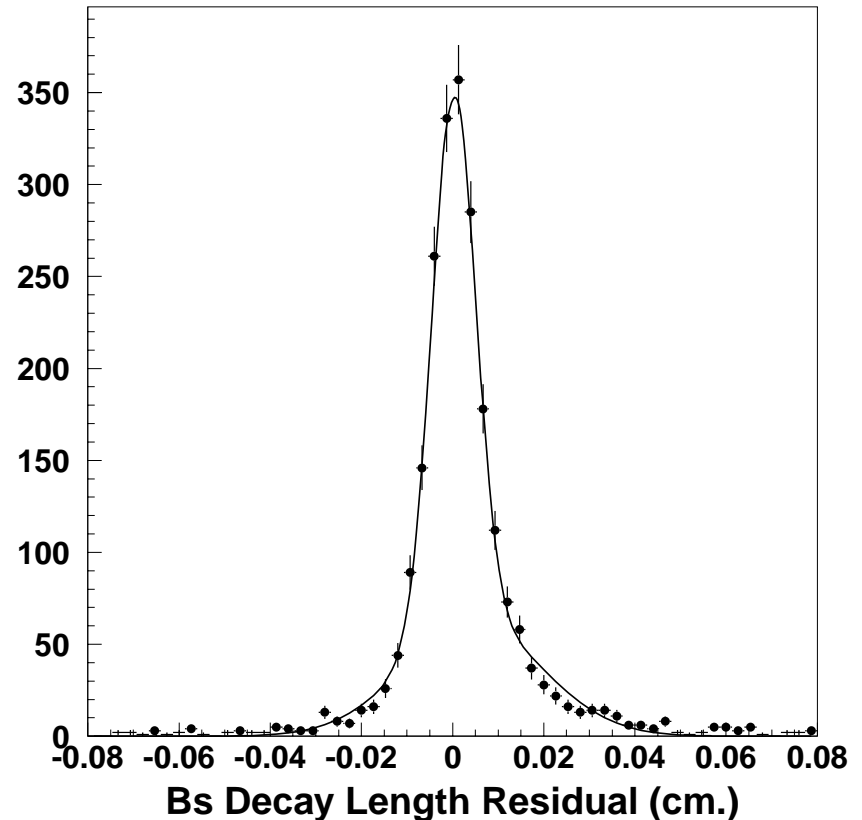
good tagging

initial state mistag = 22%

for D_s signal:

final state mistag = 13% (D_s + hadrons)

final state mistag = 5% (D_s + lepton)



D_s +tracks Amplitude Fit

95% CL sensitivity 3.3 ps^{-1}

(was 1.4 ps^{-1} last year)

Excluded regions

at 95% CL:

$$\Delta m_s < 0.48 \text{ ps}^{-1}$$

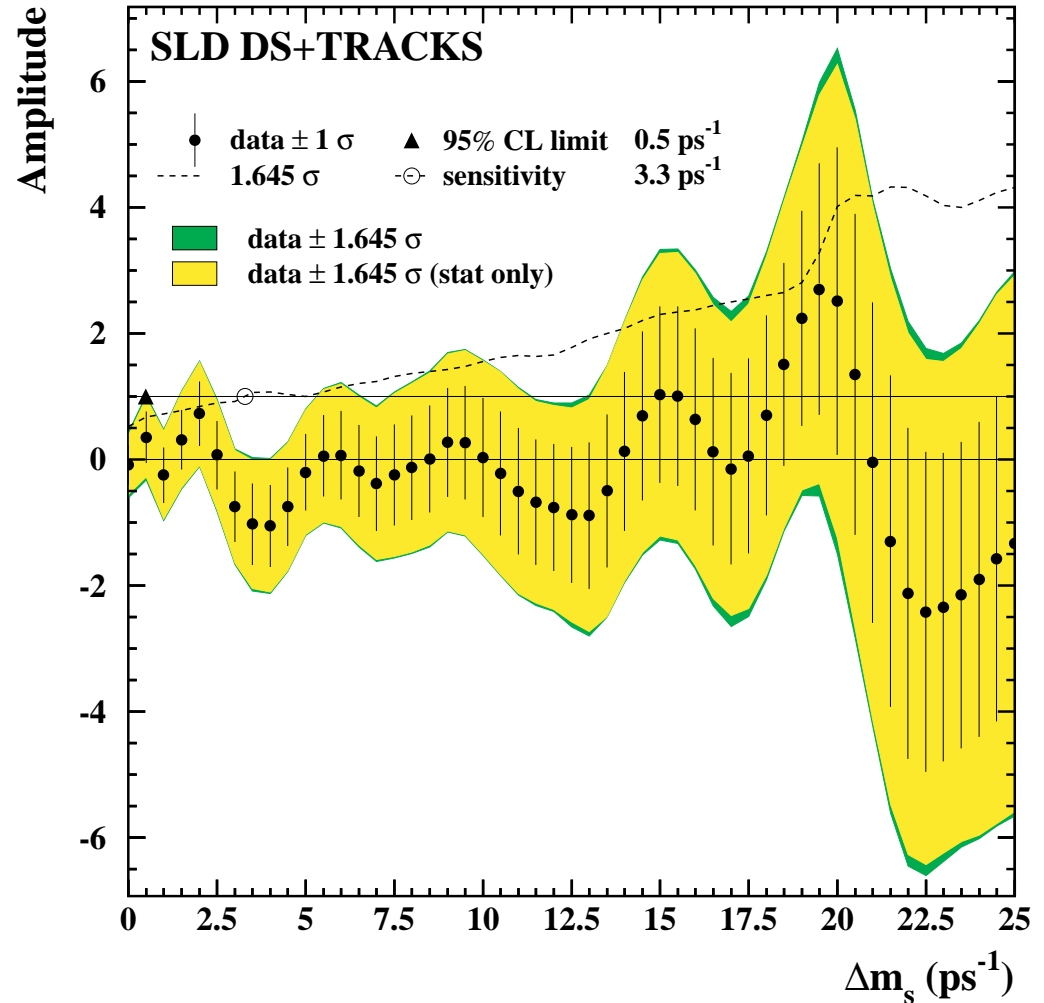
$$0.5 < \Delta m_s < 1.4 \text{ ps}^{-1}$$

$$2.5 < \Delta m_s < 5.3 \text{ ps}^{-1}$$

TO DO:

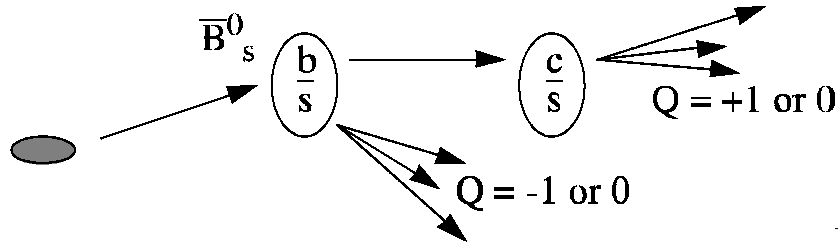
Finalize systematics

Finish paper



Charge Dipole Analysis

- FULLY inclusive reconstruction



Reconstruct sec. and tert. vertices

Tag flavor with “charge dipole”

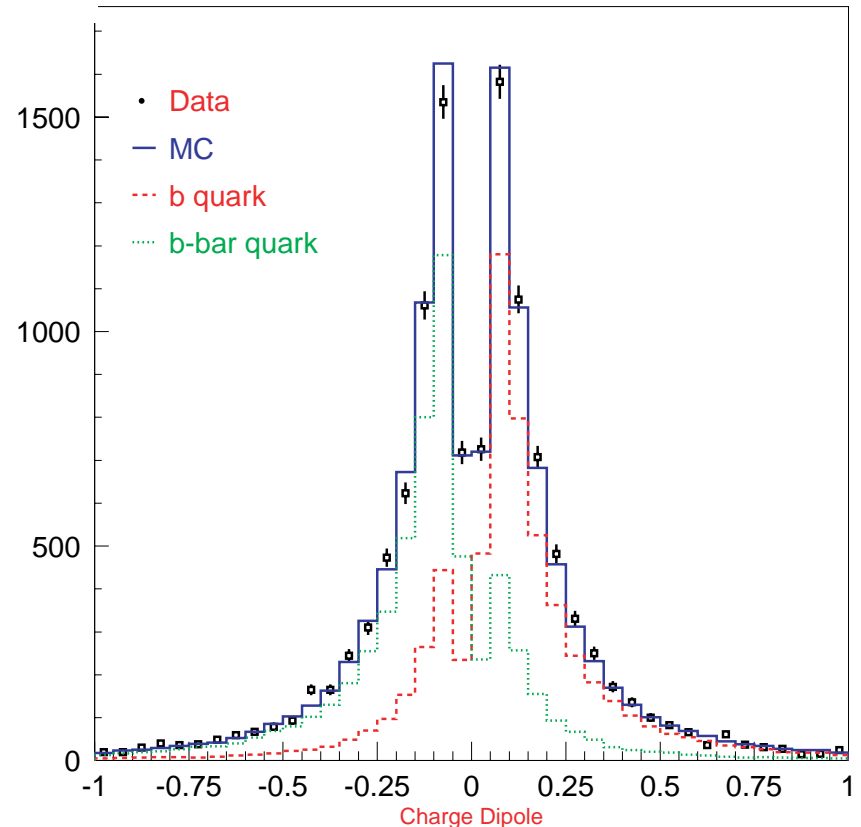
$$\delta q = \text{sign}(Q_D - Q_B) * \text{Distance}_{B \text{ to } D}$$

New event selection: higher eff. &

higher B_s purity

Select 11462 neutral decays

Final state mistag = 22%



Amplitude fit results

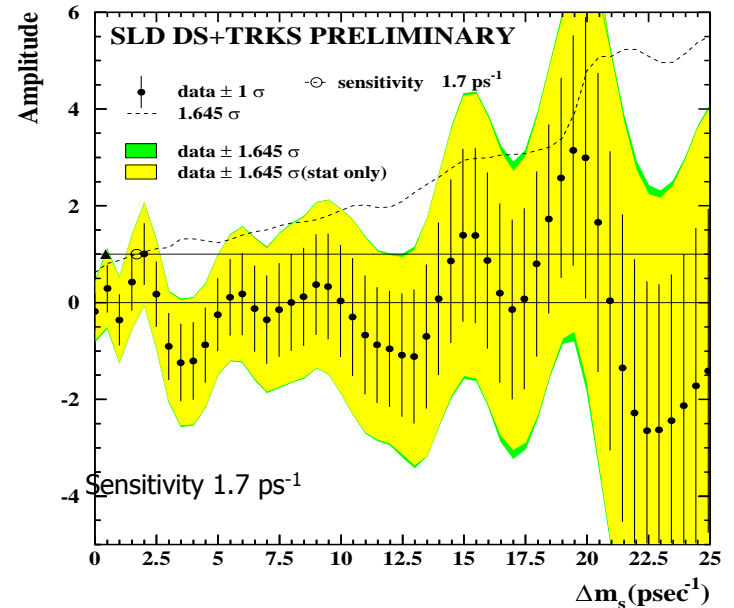
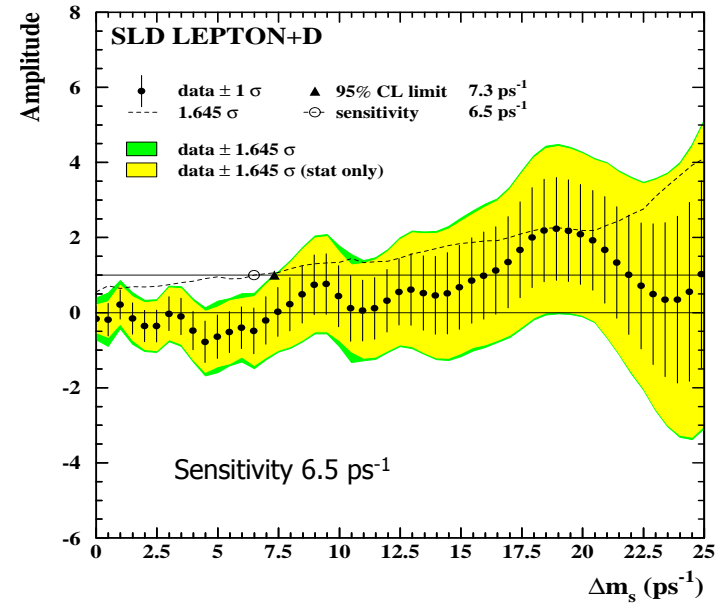
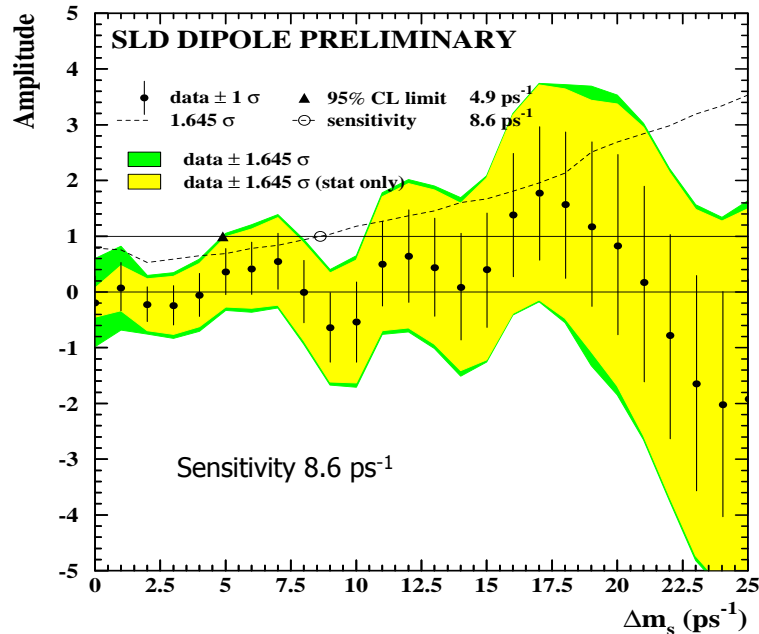
Oscillation amplitude A at fixed Δm_s

$$P_{\text{mix,unmixed}} = \frac{1}{2} \Gamma e^{-\Gamma t} (1 \mp A \cos \Delta m_s t)$$

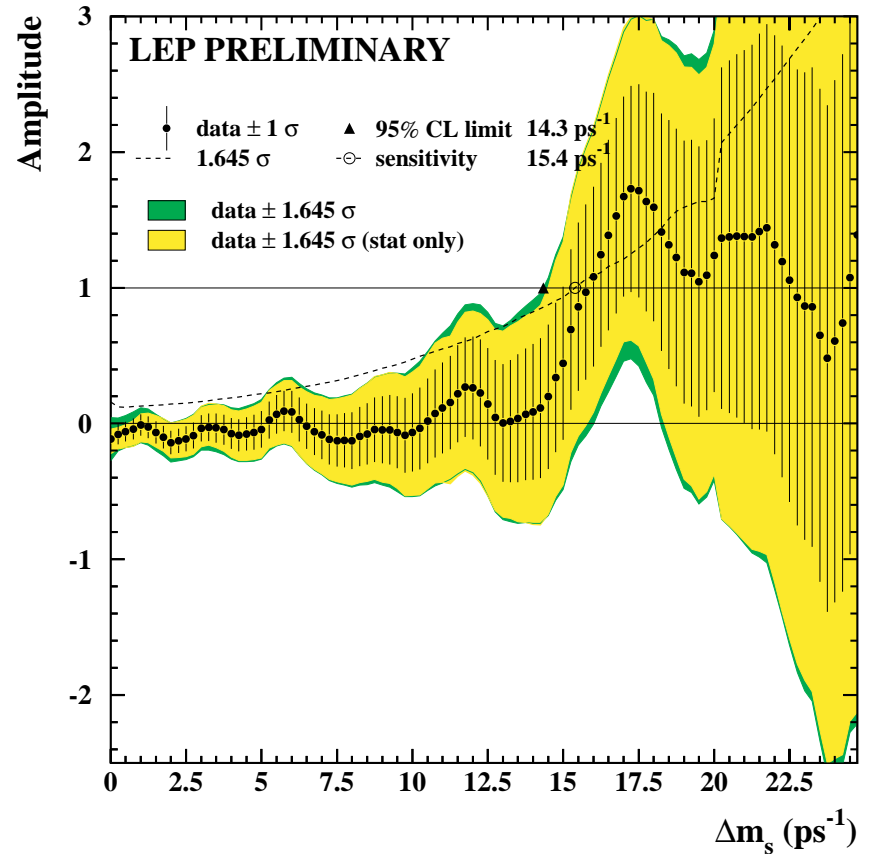
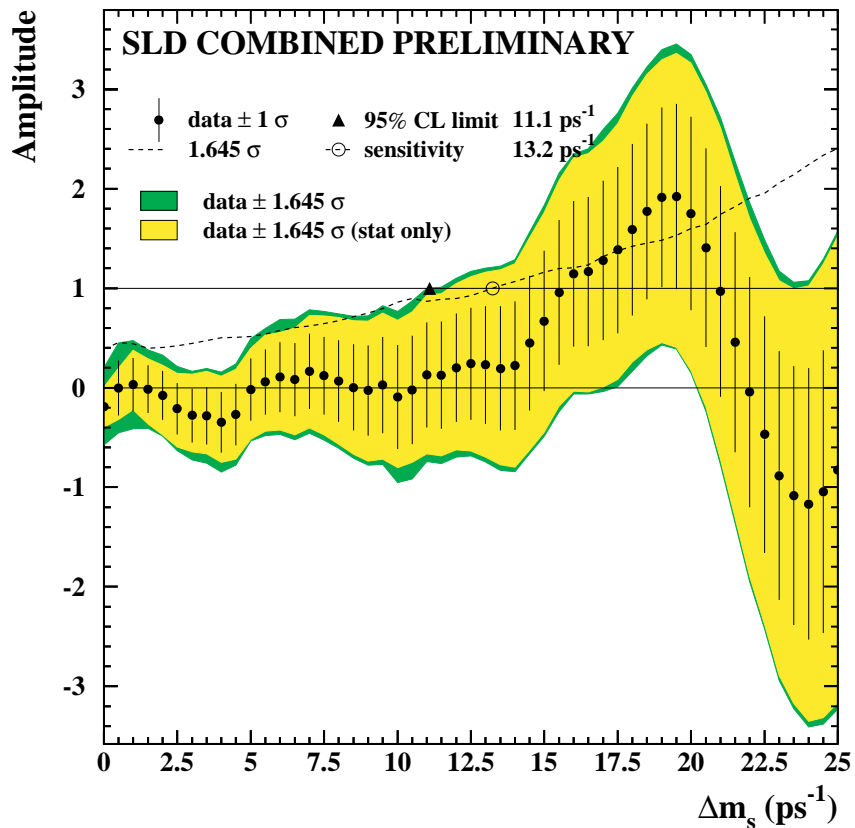
Expect $A = 1$ for freq = true Δm_s

$A = 0$ for freq \neq true Δm_s

Sensitivity: Δm_s value with $1.645 \sigma_A = 1$



B_s Oscillation Amplitude: SLD and LEP



SLD 400K Z⁰: Sensitivity = 13.2 ps⁻¹

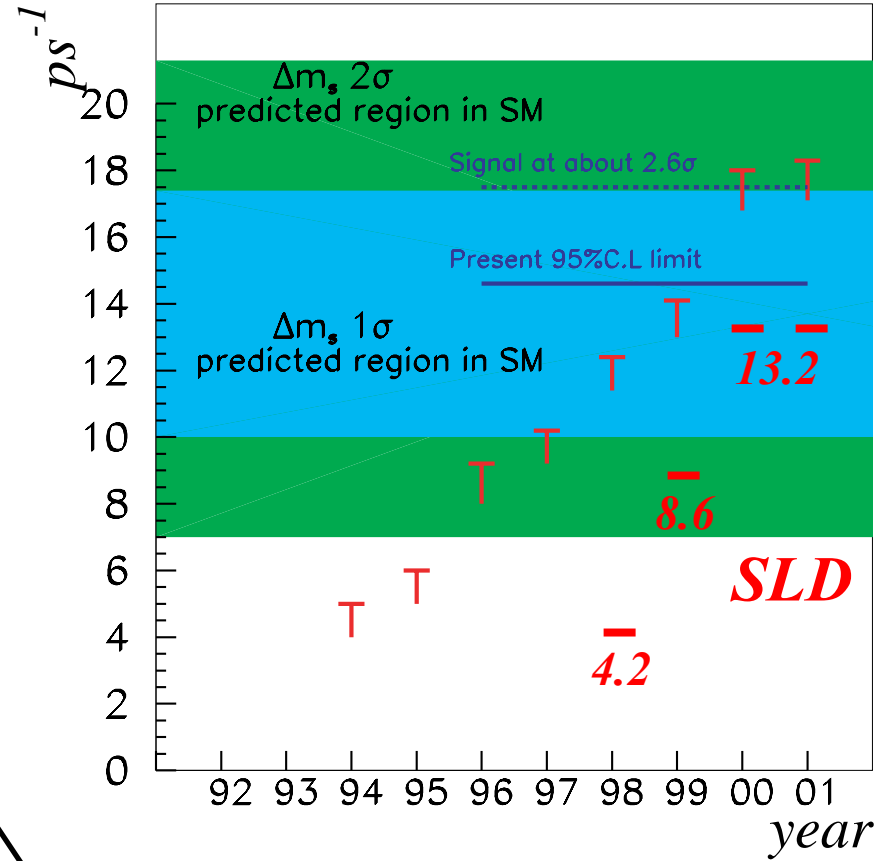
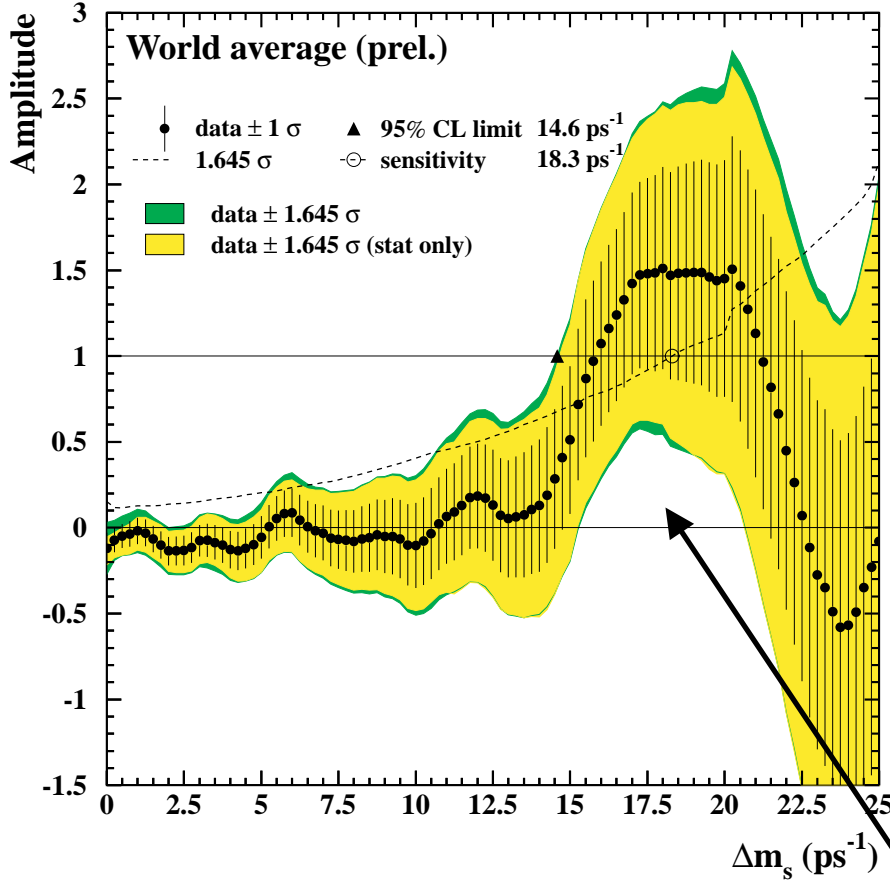
LEP 12M Z⁰: Sensitivity = 15.4 ps⁻¹

Excluded at 95% C.L.:

$$\Delta m_s < 11.1 \text{ ps}^{-1}$$

$$\Delta m_s < 14.3 \text{ ps}^{-1}$$

B_s Oscillation Amplitude: SLD, LEP, CDF



WORLD Sensitivity = 18.3 ps^{-1}

Excluded at 95% C.L.:

$$\Delta m_s < 14.6 \text{ ps}^{-1}$$

World sensitivity as a function of t

Prob of stat fluctuation $\sim 3\%$

21

Individual B_s Oscillation Amplitude Measurements

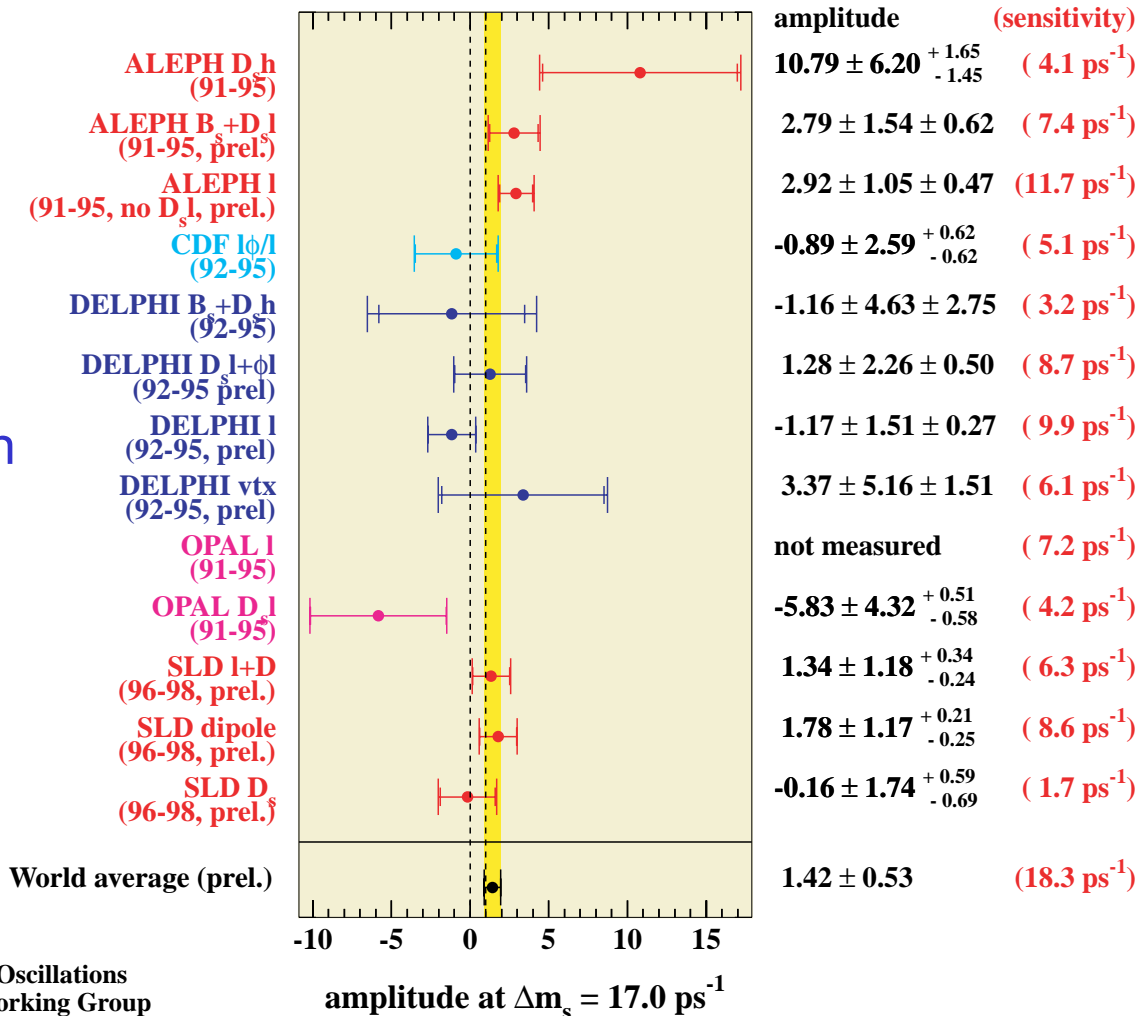
Compare measured amplitude at

$$\Delta m_s = 17.0 \text{ ps}^{-1}$$

Most sensitive

(smallest σ_A):

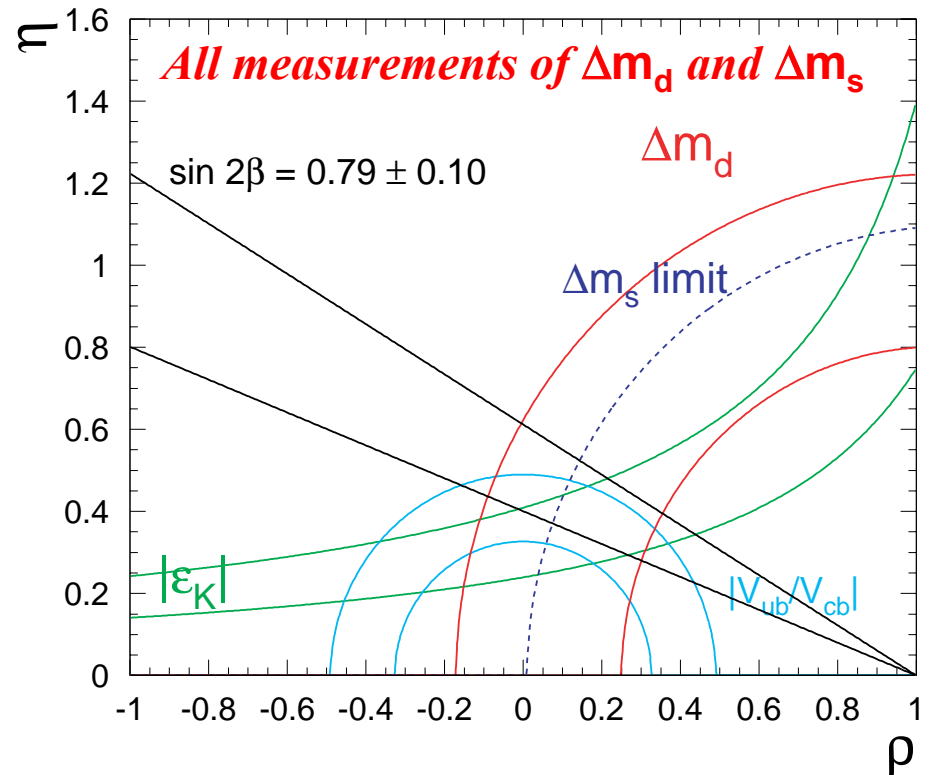
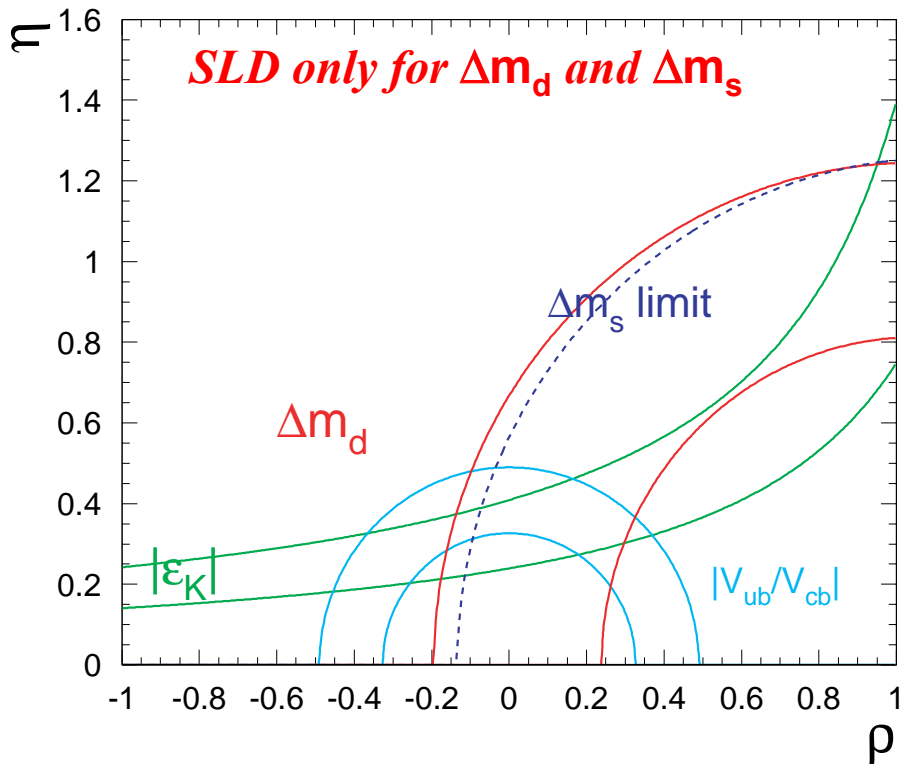
1. ALEPH inclusive lepton
2. SLD charge dipole
3. SLD lepton + D



Impact on Unitarity Triangle

Contributions from V_{cb} , V_{ub} , Δm_d , Δm_s , ϵ_K and $\sin 2\beta$

+ theory input for hadronic matrix elements (lattice QCD)



B_s mixing results eliminate $\rho < 0$ and imply CP phase $\gamma < 90^\circ$

Last-Ever(!) B_s Mixing Projection

Are we done yet? No... stay tuned!

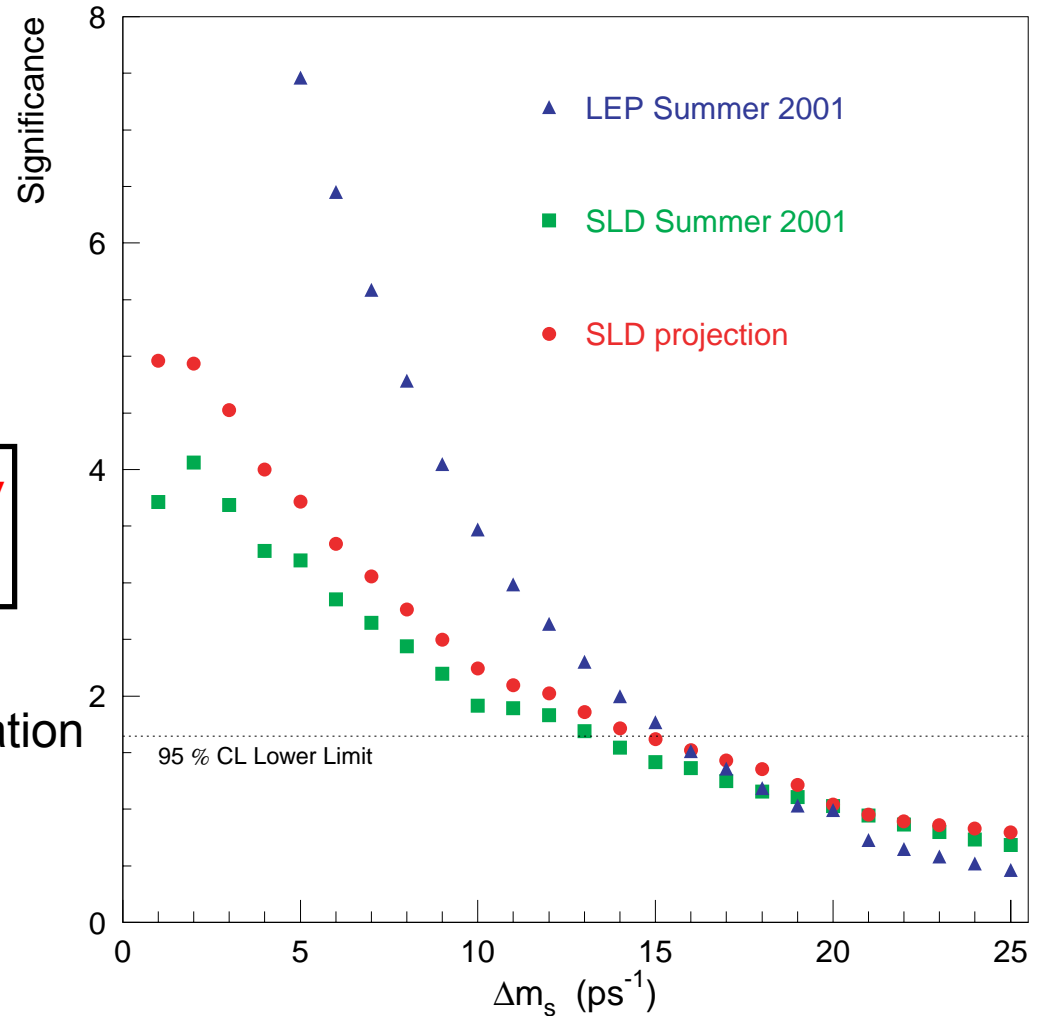
Final projection includes:

- latest version of lepton+D analysis
- (nearly) final D_s +tracks

→ **Expect final sensitivity of 15-16 ps^{-1}**

Plan to submit results for publication within 6 months

B_s mixing significance



Summary

- SLD pioneered topological vertexing for average B lifetime, B^+ and B^0 lifetime measurements
 - SLC/SLD strengths extremely well-suited to studies of time-dependent B^0 , and particularly, B_s mixing
- Beautifully illustrates power of small IP, CCD VXD, polarization and PID for B Physics
- It's been fun and rewarding!

