

Lessons Learned <sup>by me, anyway</sup> from

VX alone Tracking

Or: How I Learned to Stop Worrying  
and love Short-Lever-Arm Tracking.

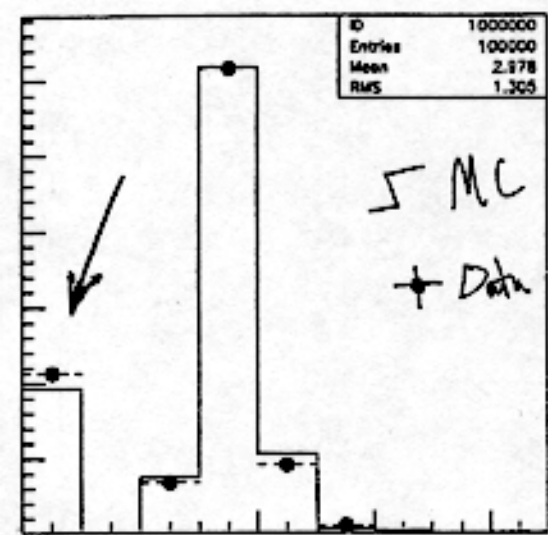
Aaron Chau, Stanford University  
(representing the tracking group)

Why use vertex-only vectors?

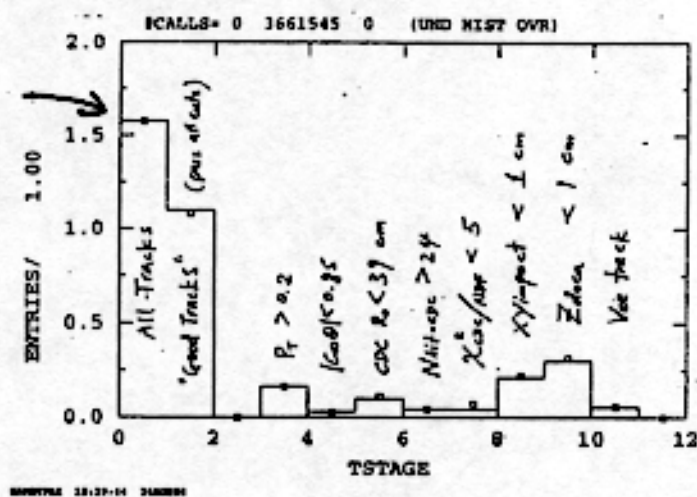
Recover unlinked tracks.

- Better B/D charge reconstruction
- Better IP  $\rightarrow$  B  $\rightarrow$  D topology reconstruction
- Perhaps Better Kinematics (especially with Levi's PHVXOV  $\leftrightarrow$  PHCHRG linking)

$\rightarrow$  May fix Data/MC tracking  $\epsilon$  mismatch:  
(due mainly to linking  $\epsilon$ ?)



$N_{\text{vhit}}$  in VXD3,  
for all PHCHRG tracks



Inefficiencies may be due to Tk Quality Cuts.  
The biggest quality cut is requiring vx03 hits on the track.

$\rightarrow$  Precursor to LCD tracking study

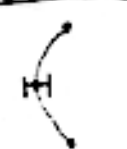
1. Some geometry
2. MC Studies of Charge measurement
3. Data/MC Comparison
4. Vertexing

# Some Geometry

Measure curvature  $K = \frac{1}{R_c}$  using parabolic approx.

$$X = \frac{1}{2} K \cdot y^2 \Rightarrow K = \frac{2 \cdot d}{r^2}$$

y view



$$\Delta K = \frac{2 \cdot (4 \mu\text{m})}{(1 \text{ cm})^2} = 8 \mu\text{/cm}^2 \quad (12 \mu\text{/cm}^2 @ 1 \text{ GeV})$$

$$\Delta \phi = 4 \mu\text{/cm} \quad (12.5 \mu\text{/cm} @ 1 \text{ GeV})$$

z view



$$\Delta \lambda = \left( \left( \frac{4 \mu\text{m}}{1 \text{ cm}} \right)^2 + \left( \frac{4 \mu\text{m}}{2 \text{ cm}} \right)^2 \right)^{\frac{1}{2}} = 4.5 \mu\text{/cm} \quad (10.5 \mu\text{/cm} @ 1 \text{ GeV})$$

## Impact Params:

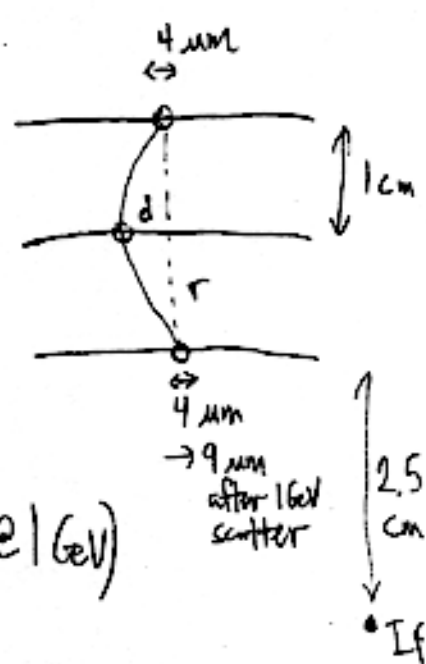
$$\begin{aligned} \Delta \xi &= \Delta \xi_0 + s \cdot \Delta \phi + \frac{1}{2} s^2 \cdot \Delta K \\ &= 4 \mu\text{m} + (2.5 \text{ cm}) \left( \frac{4 \mu\text{m}}{\text{cm}} \right) + \frac{1}{2} (2.5 \text{ cm})^2 (8 \mu\text{/cm}^2) \end{aligned}$$

$$\Delta \xi = 39 \mu\text{m} \quad (73 \mu\text{m} @ 1 \text{ GeV})$$

$$\Delta \eta = \Delta \eta_0 + s \cdot \Delta \lambda = 4 \mu\text{m} + (3 \text{ cm}) \left( \frac{4.5 \mu\text{m}}{\text{cm}} \right)$$

$$\Delta \eta = 17.5 \mu\text{m} \quad (36 \mu\text{m} @ 1 \text{ GeV})$$

Momentum:  $\Delta \frac{Q}{P_T} = \frac{1}{B} \Delta K \approx 0.44 \text{ %/GeV} \quad (0.67 \text{ %/GeV} @ 1 \text{ GeV})$

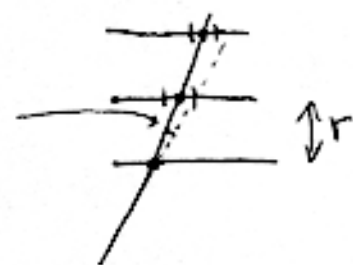


# What have we (I) learned?

- 3 hits = 6 transverse measurements

⇒ 2 positions, 2 angles, 1 curvature + 1 d.o.f

- Angle measurements are quickly dominated by scattering.

$$\Delta \lambda = \frac{\sqrt{\Delta_0^2 + (\Theta_{ms} \cdot r)^2}}{r} \approx \Theta_{ms}$$


- Curvature measurement can be controlled by increasing layer spacing

$$\Delta K \approx 2 \frac{\sqrt{\Delta_0^2 + (\Theta_{ms} \cdot \frac{r}{2})^2}}{r^2} \approx \frac{\Theta_{ms}}{2r}$$

← Function of measured curvature!  
Feeds back into errors:

- Having extra layers helps, gives  $\chi^2$  for bkgd rejection

- 'Scattered' hits get less weight.

- Extra curvature info may help with alignment

# $P_T$ resolution problem

$$\frac{1}{R_c} = \frac{QB}{P_T} = \frac{(3 \times 10^{-4}) \cdot b}{P_T}$$

$$= \frac{2d}{r^2} \quad \Rightarrow$$

High  $P_T$  tracks are very straight



$$d \approx \frac{9 \mu\text{m}}{P_T}$$

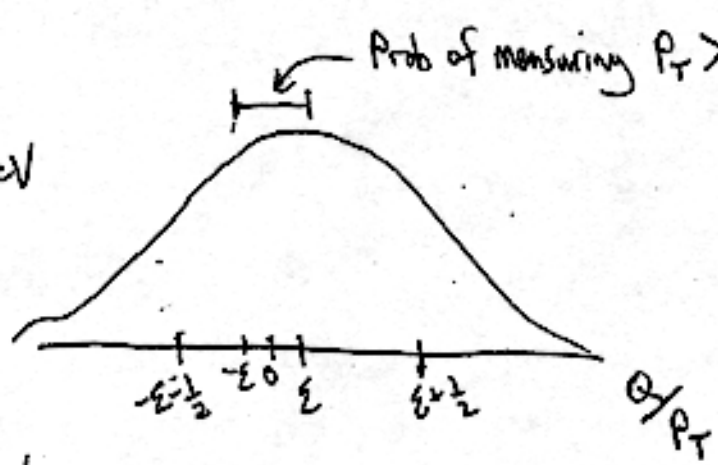
A.  $P_T = 2 \text{ GeV}$  track will have  $d \approx 4 \mu\text{m}$ .  
 But the cluster resolution is also  $\Delta d \approx 4 \mu\text{m}$ .

$\Rightarrow$  The intrinsic  $\frac{1}{P_T}$  resolution is  $\Delta \frac{1}{P_T} \approx \frac{1}{2} \text{ GeV}^{-1}$

$\Rightarrow$  High  $P_T$  tracks will have their  $P_T$  smeared down to  $2 \text{ GeV}$  (and get the wrong charge)  
 $\Delta \frac{Q}{P_T} \approx \pm \frac{1}{2} \text{ GeV}^{-1}$

## Example: High $P_T$ tracks

$\epsilon = \frac{Q}{P_{T,true}}$   
 $P_{T,true} > 2 \text{ GeV}$

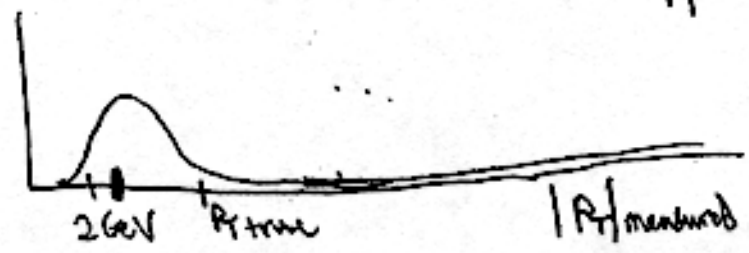


Prob of measuring  $P_T > P_{T,true} \approx \frac{1}{\sqrt{2\pi}} \cdot 2\epsilon \approx \frac{\epsilon}{\sigma} \approx 2\epsilon$

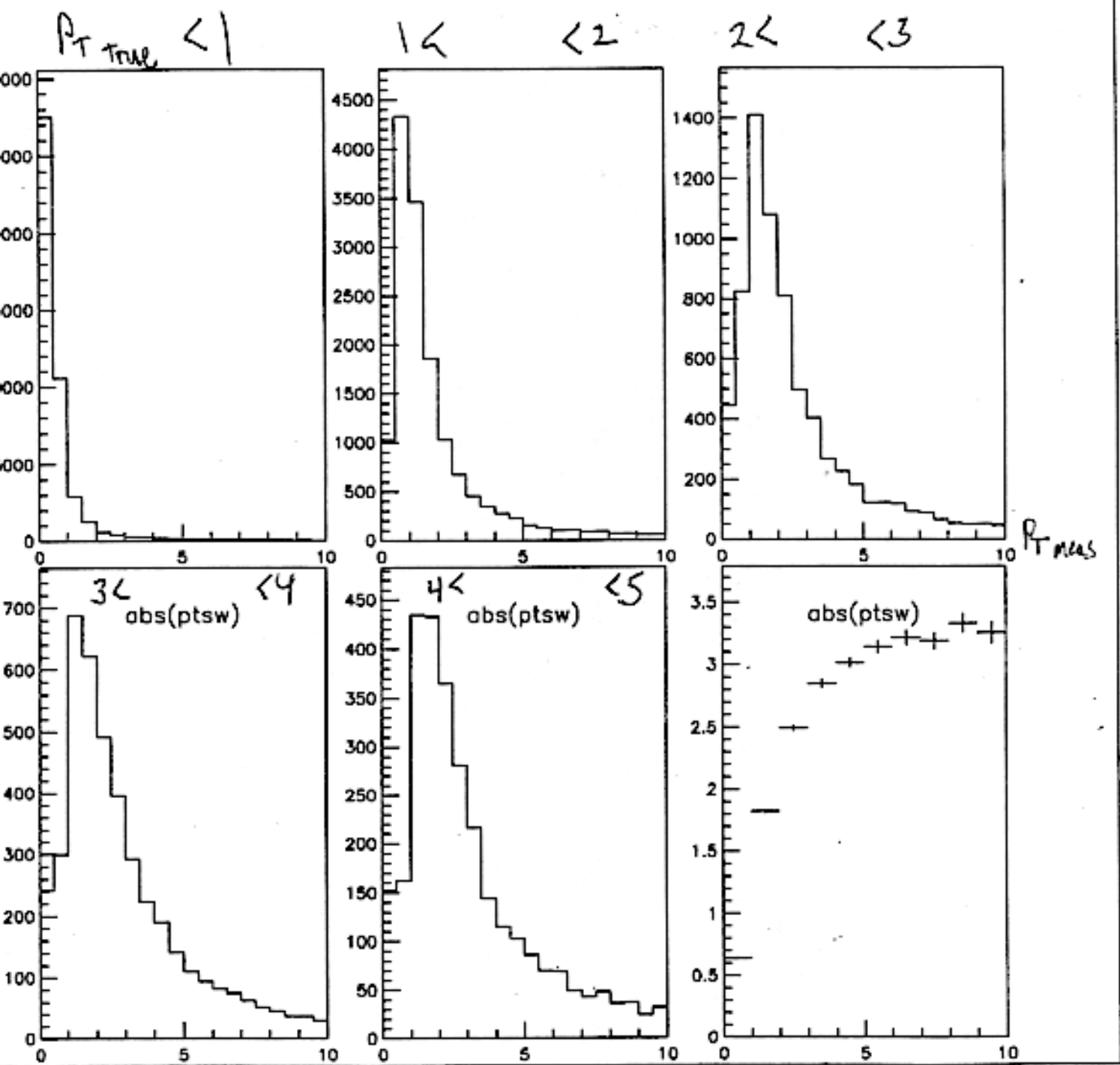
Prob  $P_T < P_{T,true} \approx 1 - 2\epsilon$

Prob right sign  $\approx \frac{1}{2} + \epsilon$

$P_T$  distribution  $\Rightarrow$



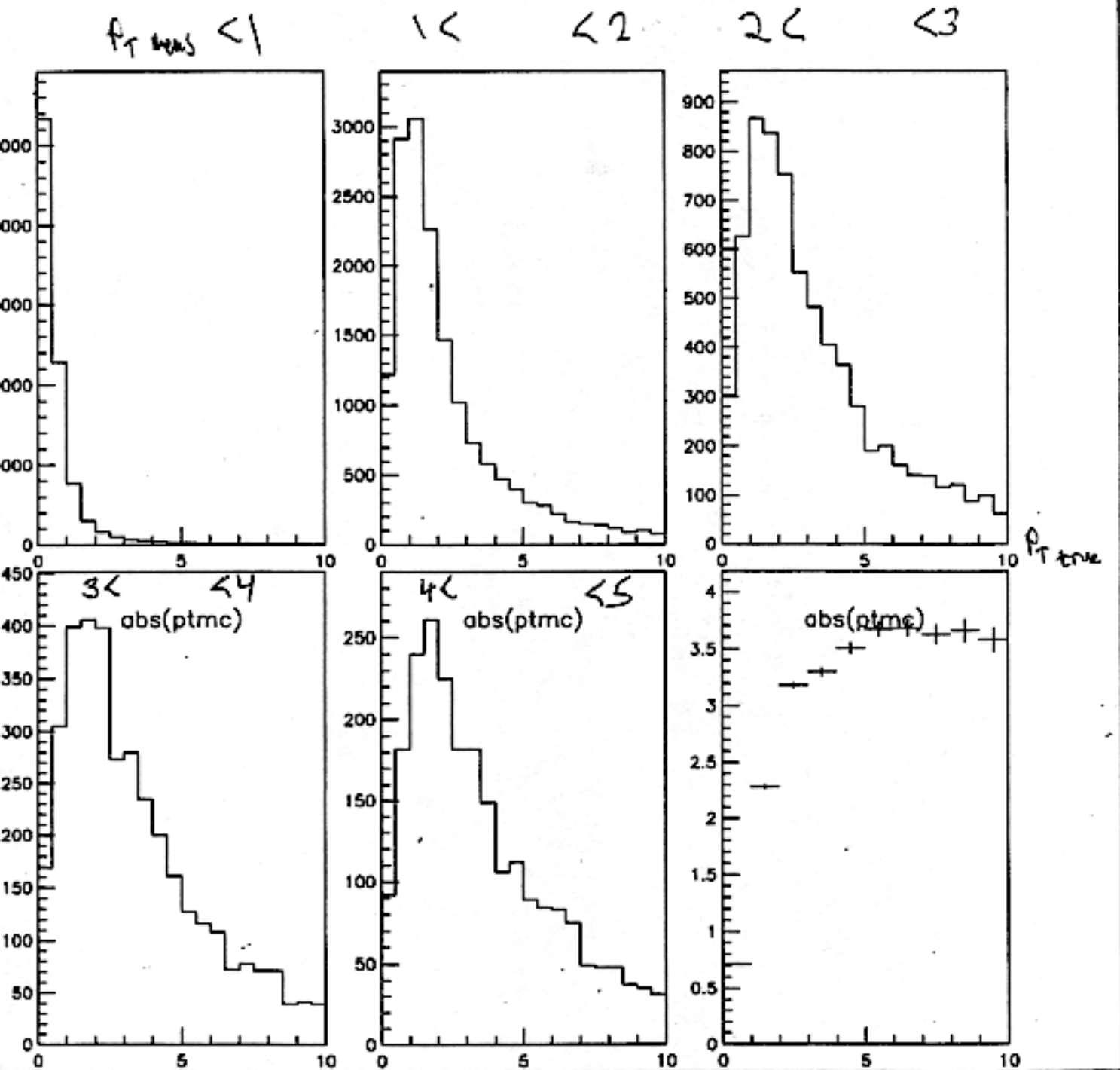
# Measured $P_T$ distributions as fun of True $P_T$



$\langle P_{T, \text{meas}} \rangle$  vs  $P_{T, \text{true}}$

- ⇒ High  $P_T$  tracks are smeared down to  $\sim 2$  GeV/c
- ⇒ Low  $P_T$  tracks have a long tail and are often measured at much higher  $P_T$  (thus, scattering errors are underestimated)

# True $P_T$ distributions as fcn of measured $P_T$

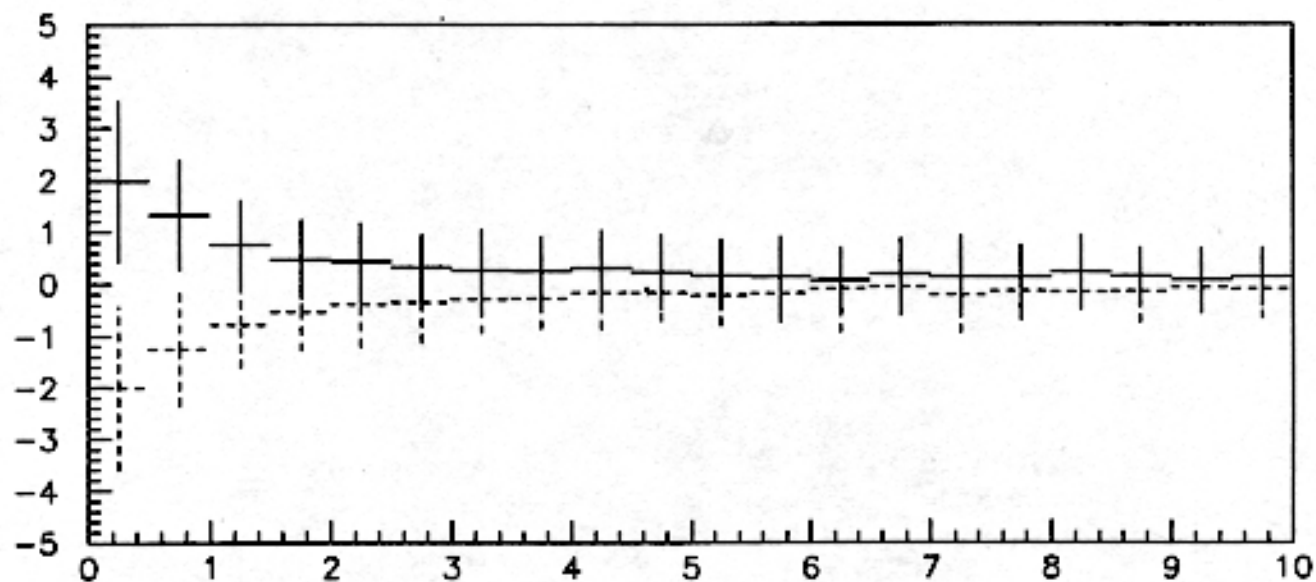


$\langle P_{T \text{ true}} \rangle$  vs  $P_{T \text{ meas}}$

$\Rightarrow$  Measured  $P_T$  is not a good estimator of true  $P_T$   
 (except at low  $P_T$ )  
 $P_T < \frac{1}{\Delta P_T}$

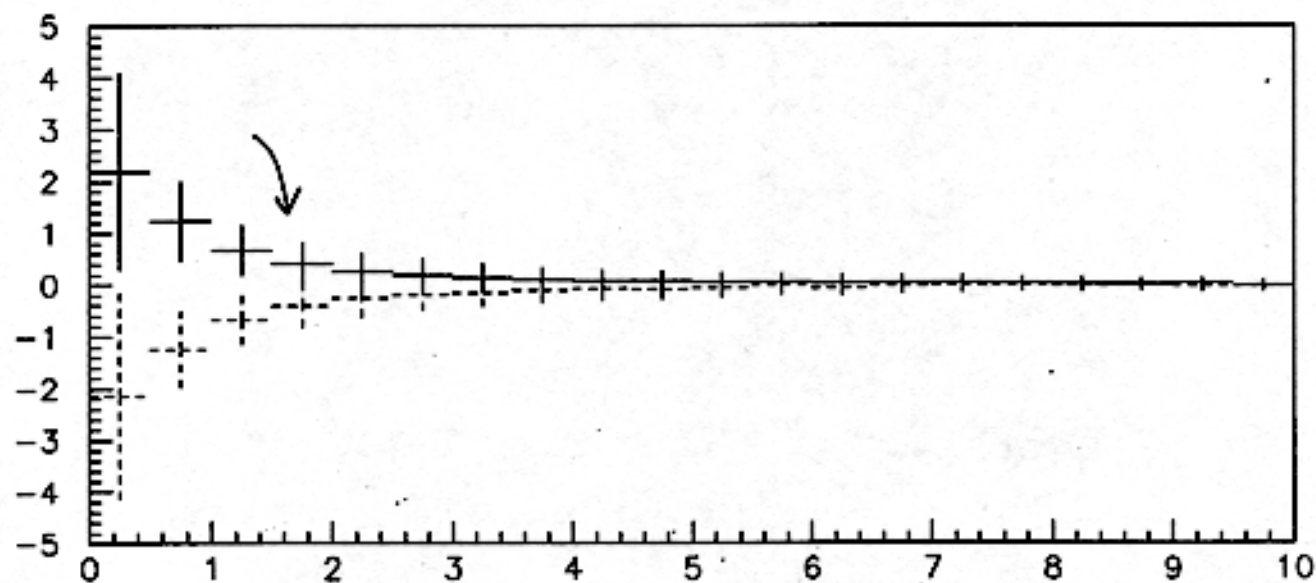
PHVXOV - only Charge Separation

$P_{T \text{ swim}} > 0.25 \text{ GeV}$



$Q/pt_{sw}$  vs  $pt_{mc}$

MC  $P_T$

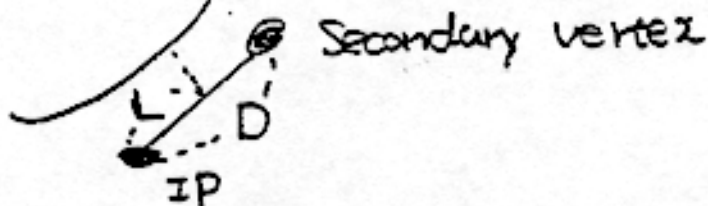


$Q/pt_{sw}$  vs  $pt_{sw}$

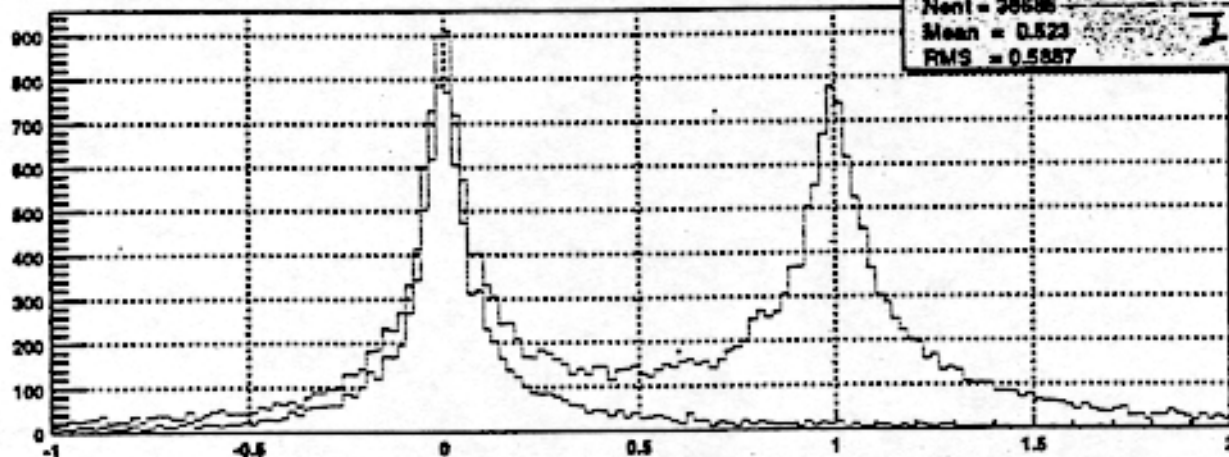
Measured  $P_T$

track. (using VXD3-only curvature)

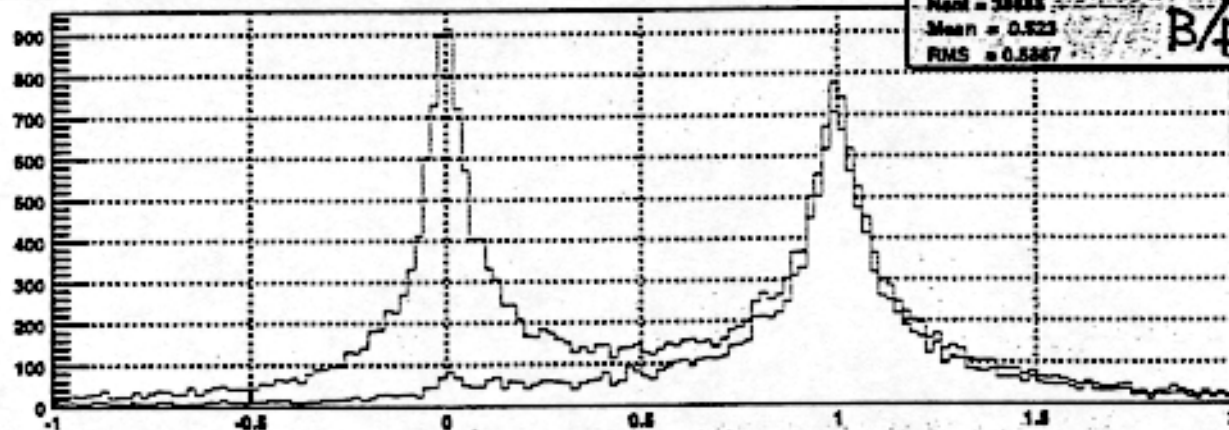
T. Abe



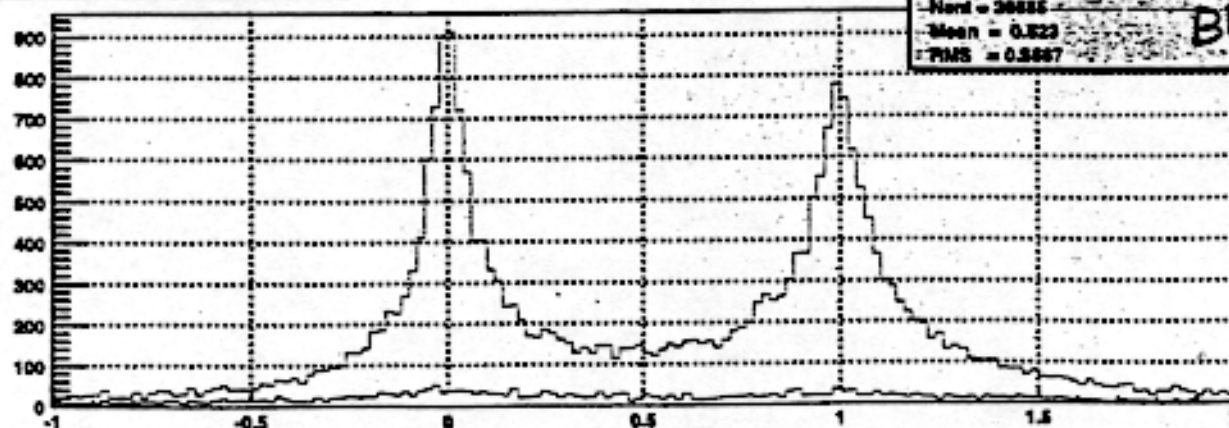
L/D all with CUT



L/D all with CUT



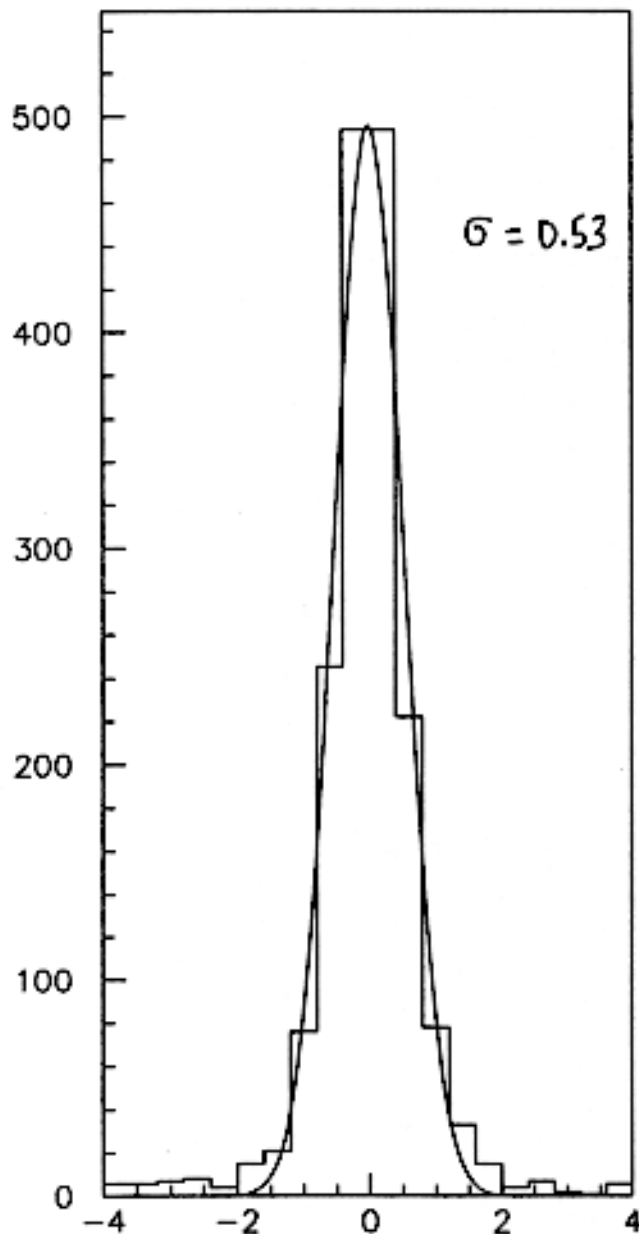
L/D all with CUT



$$\frac{Q}{P_T}$$

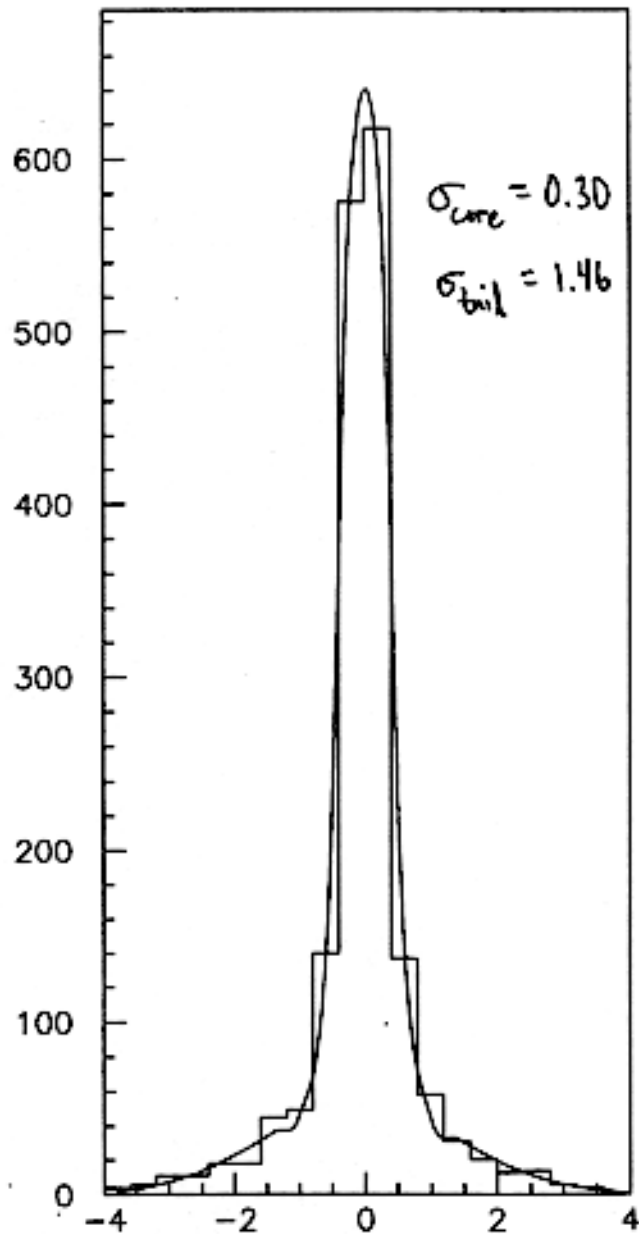
residuals for PHVXD3's

VXD3 only



$Q/ptsw - Q/iptmc$

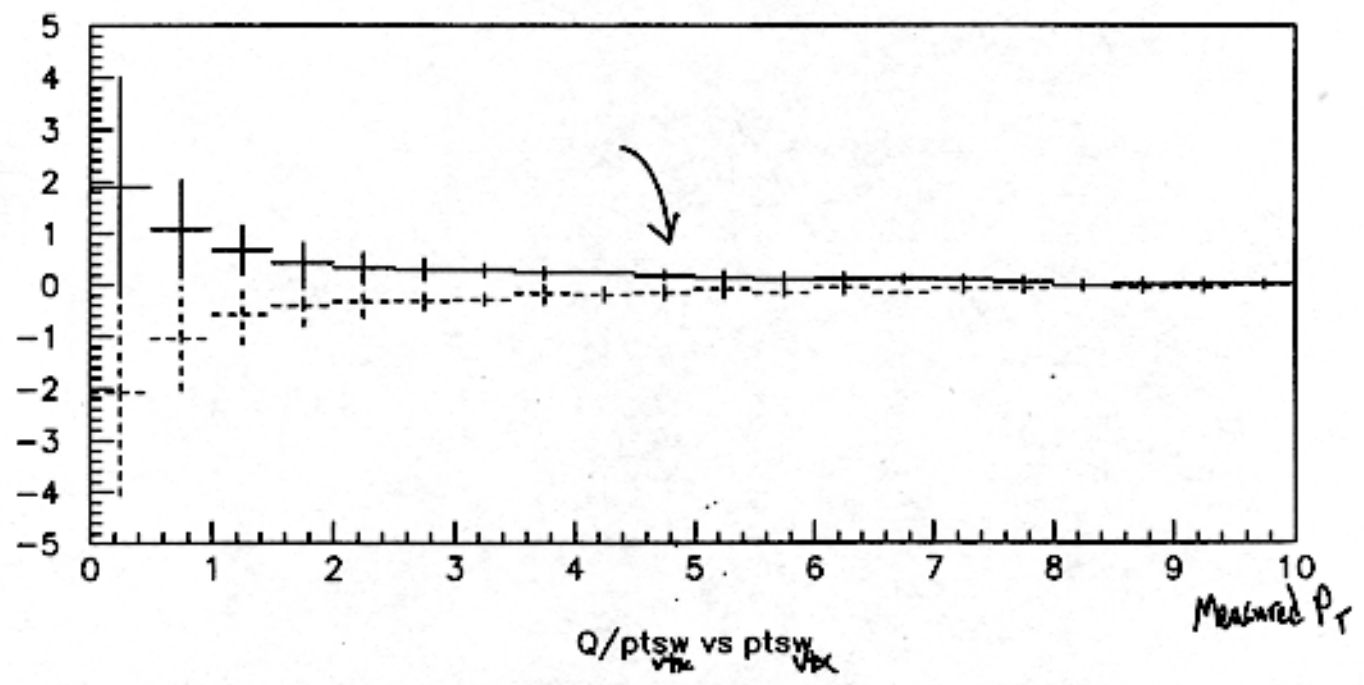
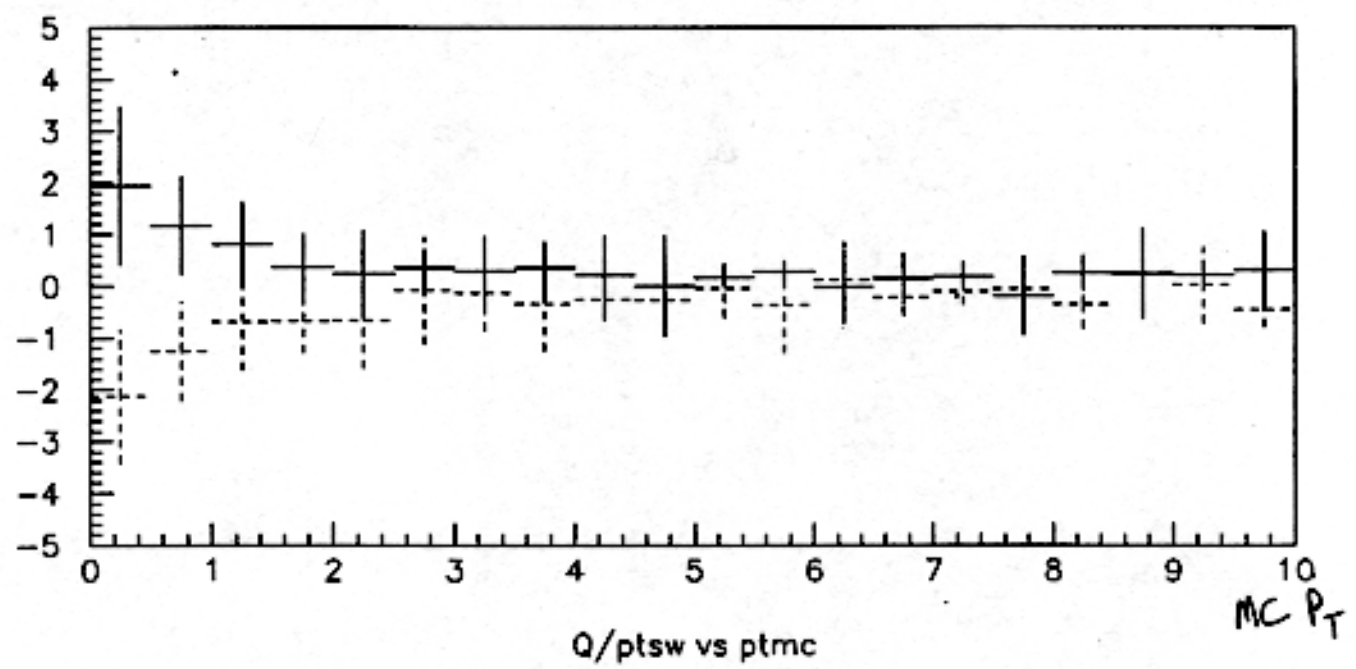
VXD3 + BZMSS sec vtx



$Q/ptvtxsw - Q/iptmc$

# PHVXOV + BZMASS vtx Charge Separation

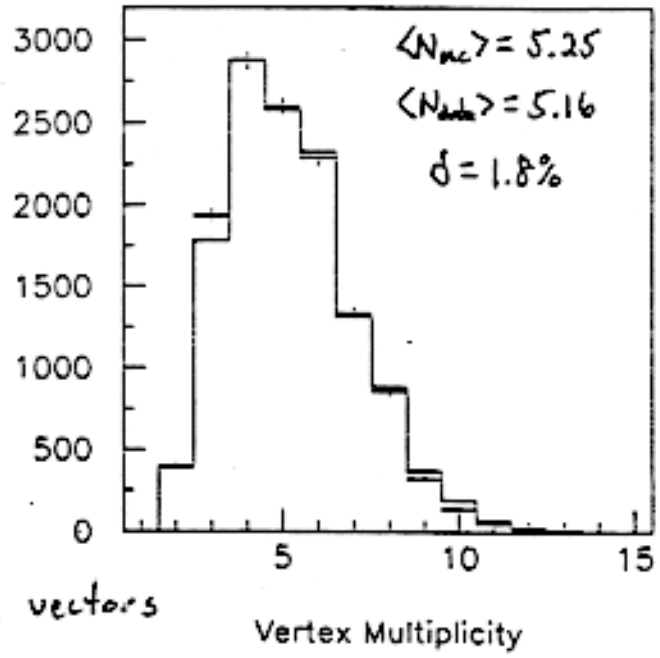
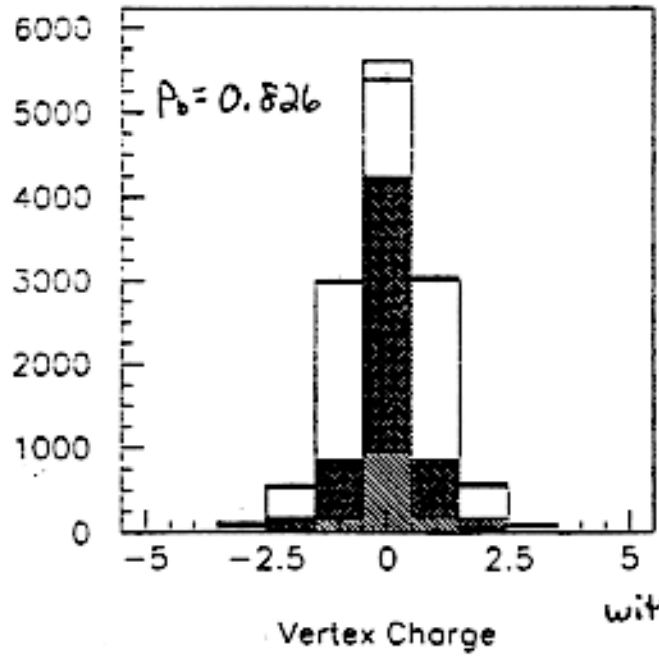
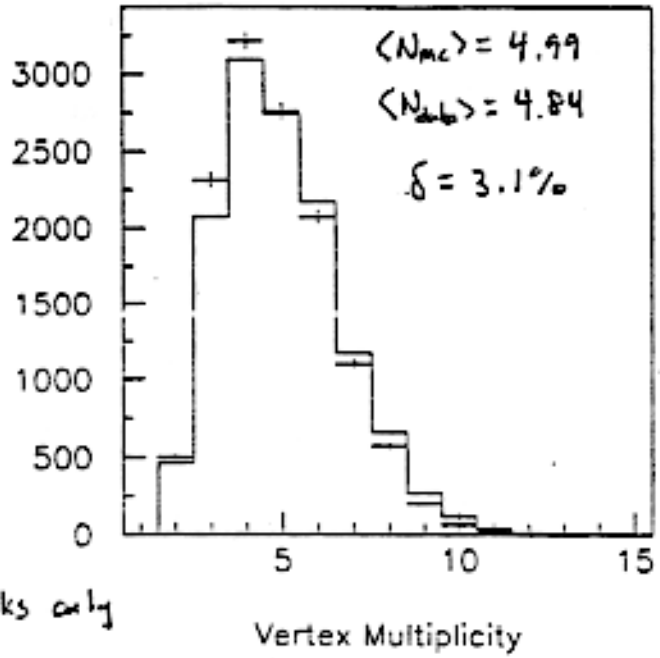
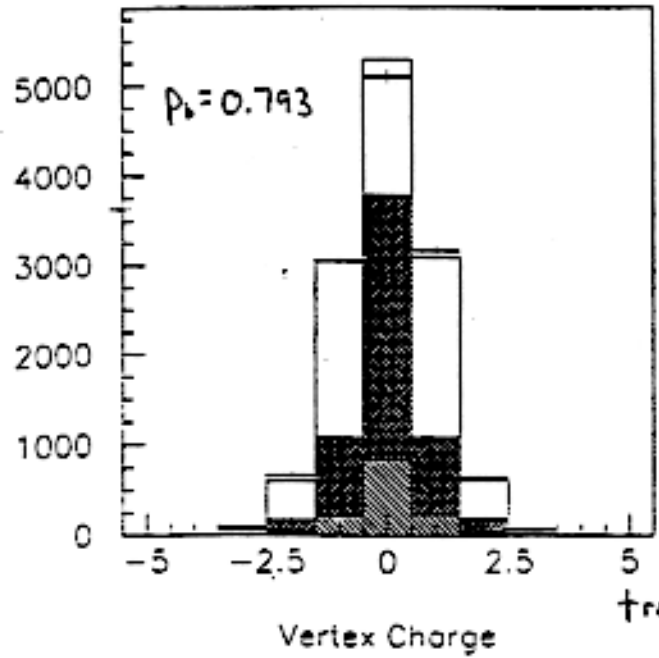
$P_{T \text{ vtx}} > 0.25 \text{ GeV}$



T. Wright

Using Neural Net PHOXOV attachment to sec. vtx.

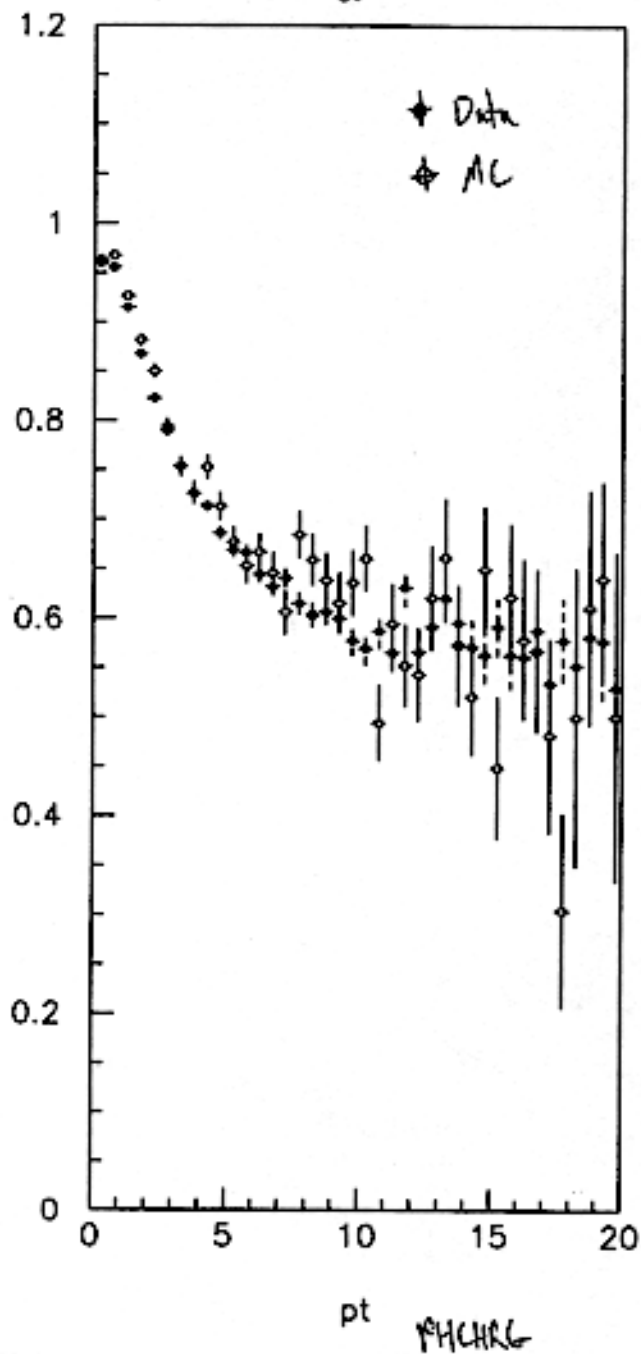
Bottom Tag



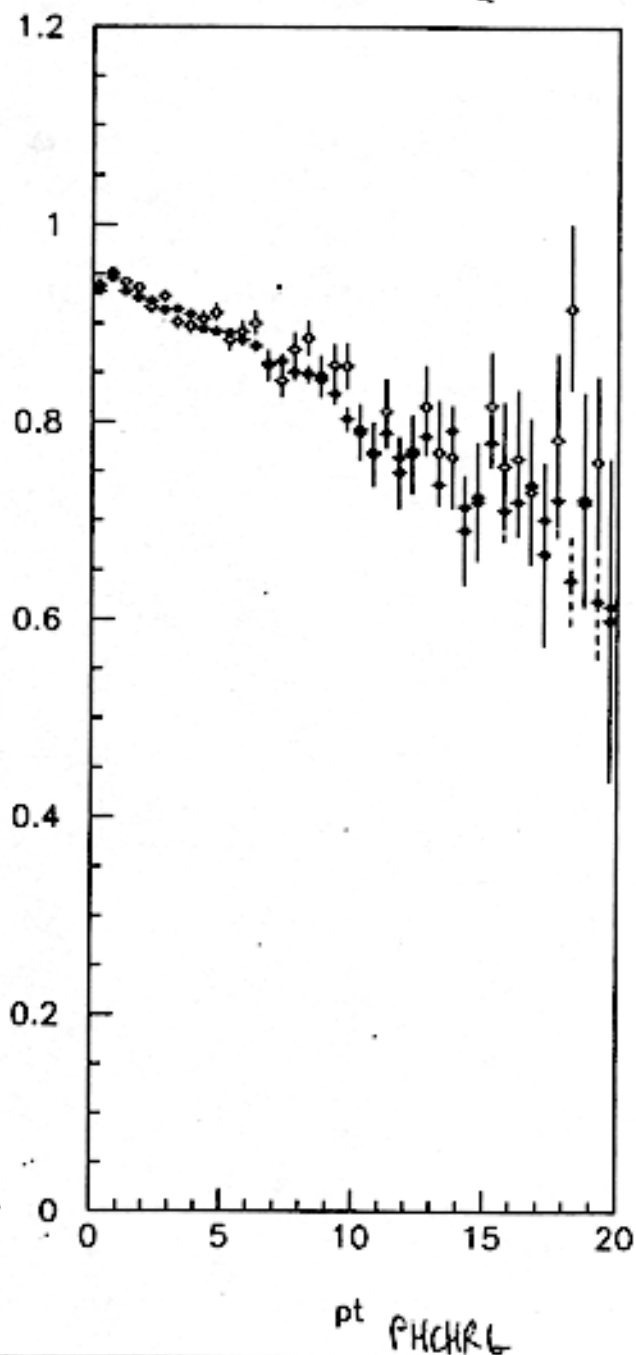
⇒ PHOXOV partially fixes tracking efficiency discrepancy

VXOV  
Fixed Charge purity vs  $P_T$  using free linked fits

VXalone  $P_a$

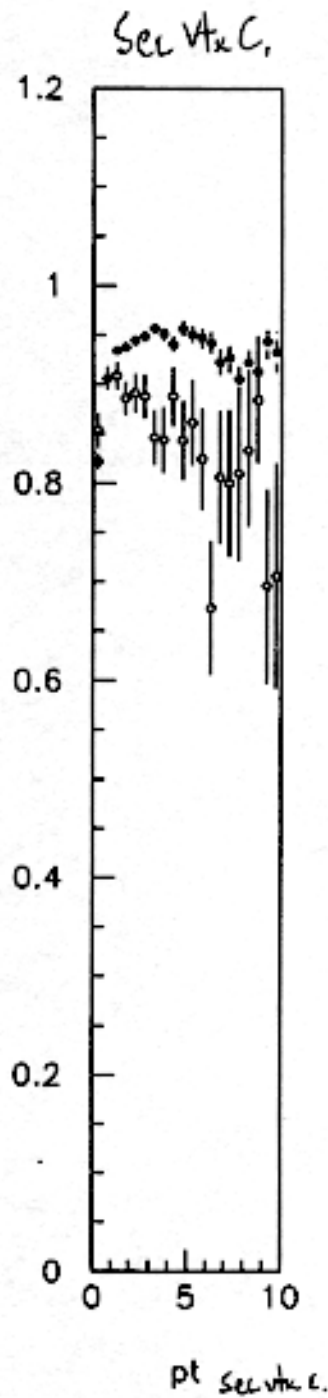
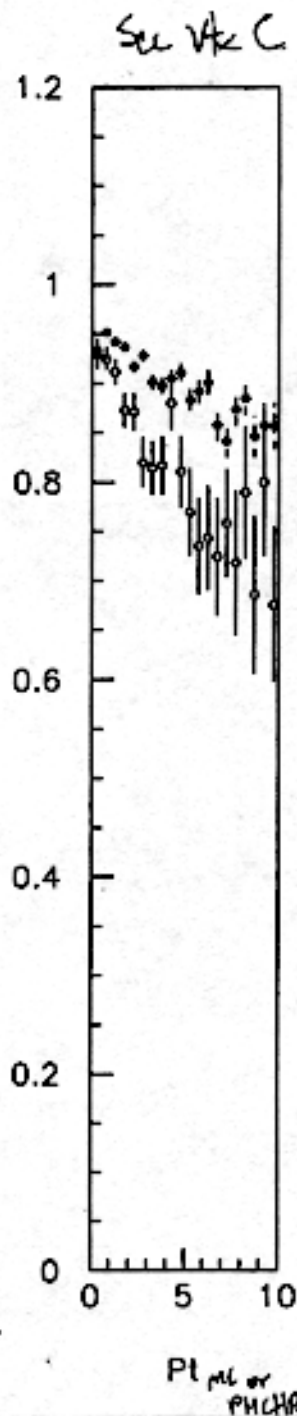
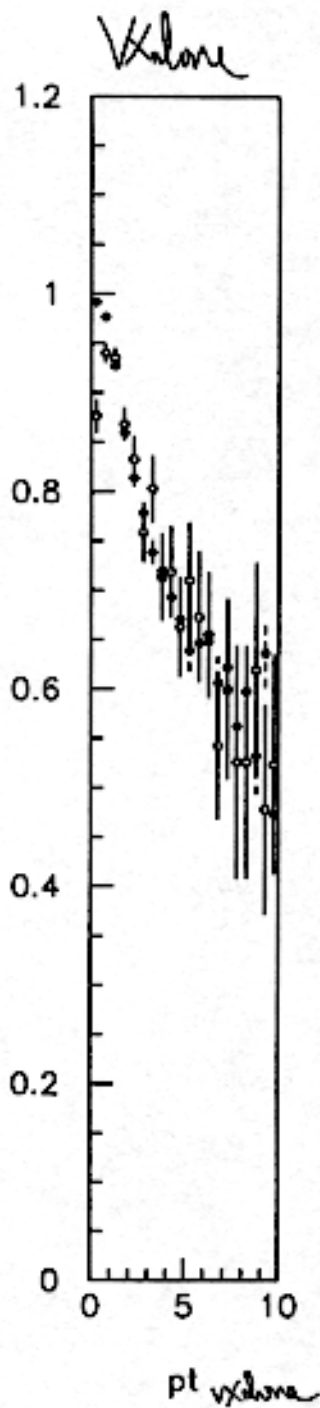
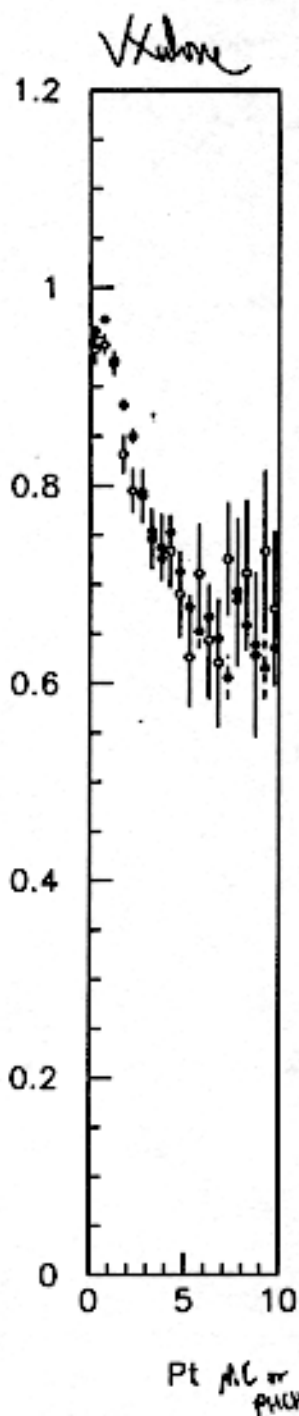


See Vix Constrained  $P_a$



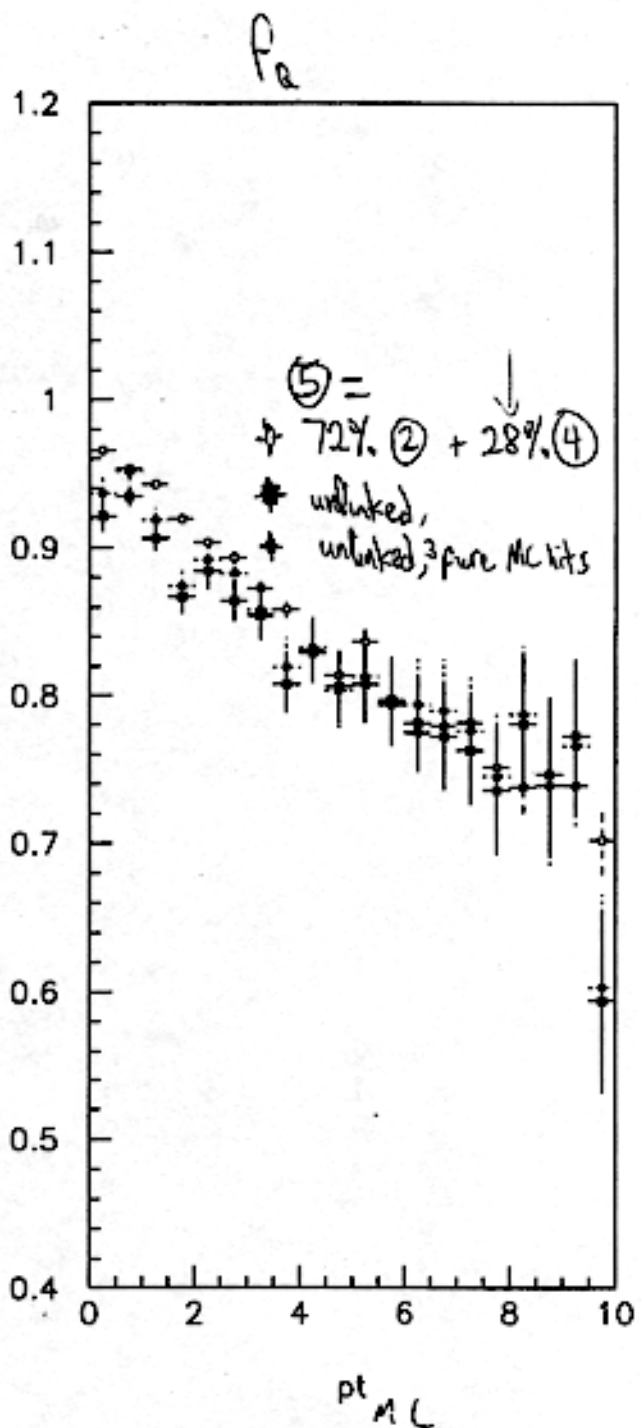
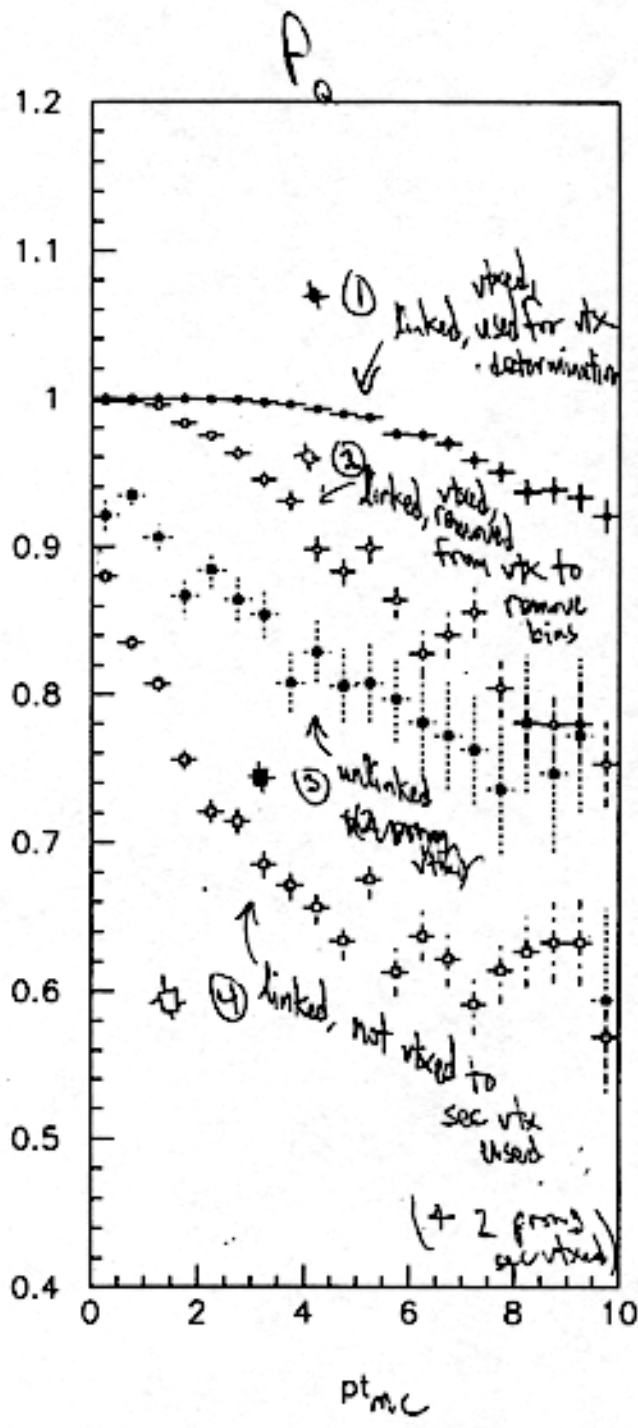
# Comparison of Charge Mass Purity for

+ linked PHXs  
 o unlinked PHXs



PHUXOV sec vtx const. Change Purity vs true  $P_T$   
for various samples

MC



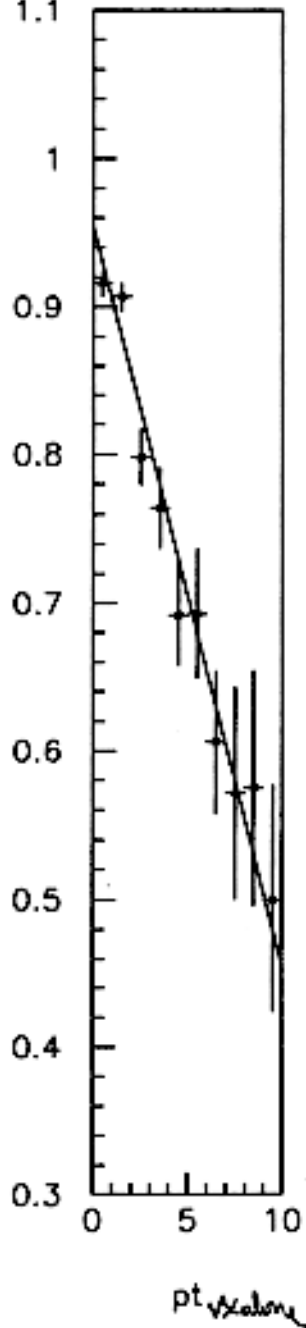
Model: Sample ② is like a tracking inefficiency causing hits to be missing from <sup>sec</sup>vtx  
Sample ④ " " " " for tracks not put on sec. vtx

For regular ~~the~~ linked tracks  $\frac{\#① + \#②}{\#① + \#② + \#④} = .72$ ,  $\frac{\#④}{\#① + \#② + \#④} = .28$   
⇒ Assume these fractions <sup>weighted, normalized</sup> are the same for recovered PHUXOV hits for plot ⑤

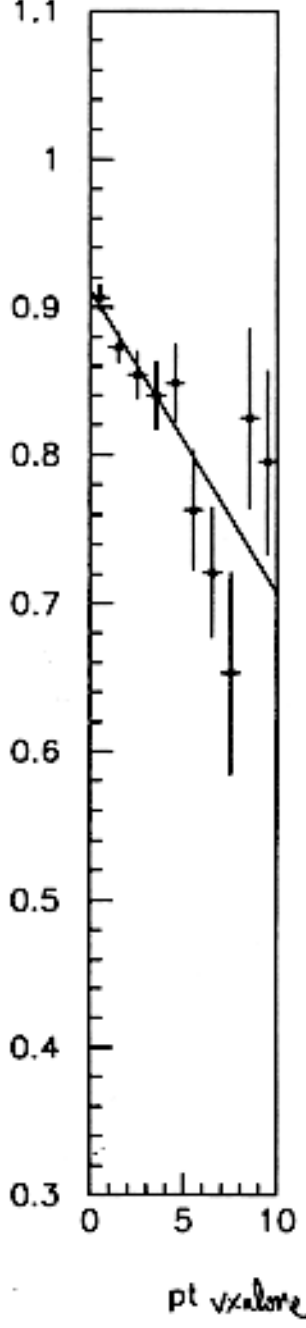
Fixed VXOV Charge Purity vs Measured  $P_T$   
using vertexed, unlinked PHKOVs

MC

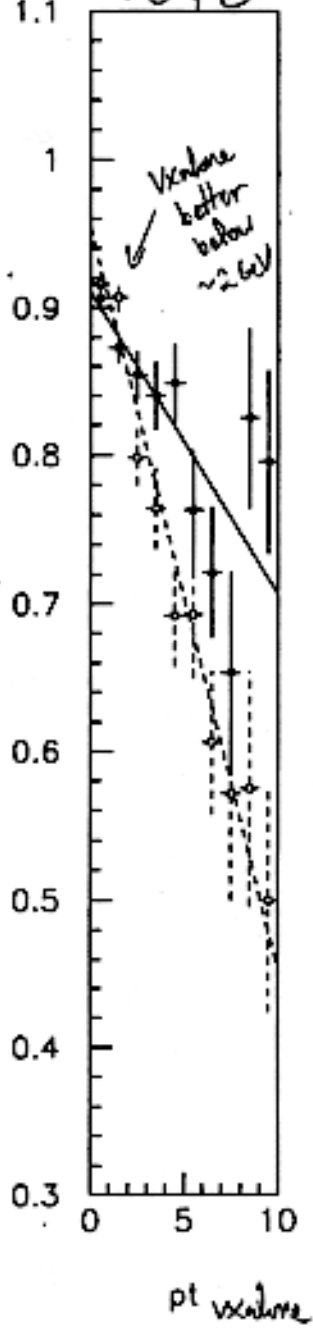
① Vxalone Q



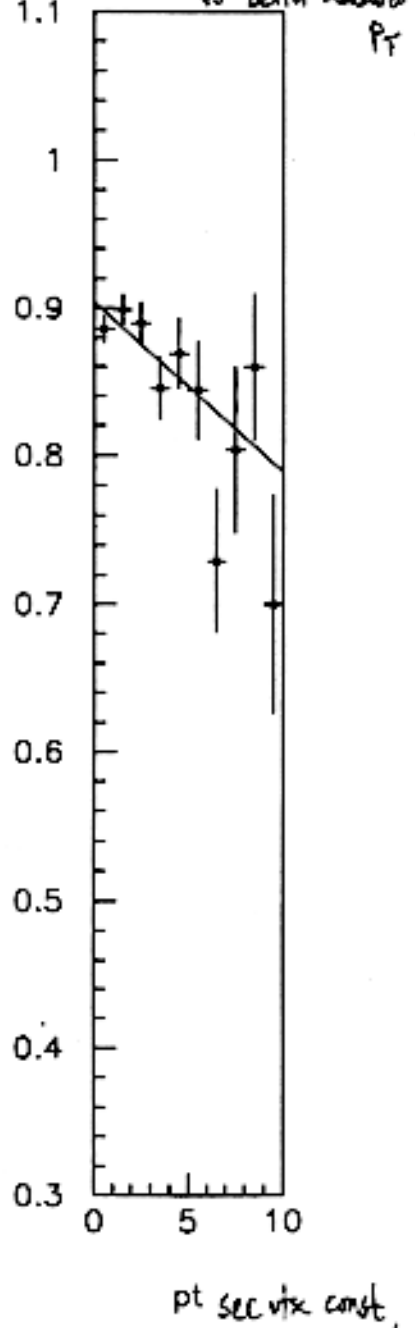
② Sec Vtx Const. Q



Comparison of ① & ②



Sec Vtx Const. Q vs better measured  $P_T$



Fits:

$$P_{Vxalone} \approx 0.954 - 0.050 P_{T_{Vxalone}}$$

$$P_{SVC} \approx 0.904 - 0.011 P_{T_{SVC}}$$

$$\approx 0.911 - 0.020 P_{T_{Vxalone}}$$

Still need to average in  
~ 2% Futures with  $P = 0.5$

# Re-linking the vectors (BBVLINK) (Leon)

- PHUXOV charge resolution is very poor at high momentum since the tracks are straight.
- Momentum measurement is very poor for all vectors.
- ⇒ Try to link orphaned vectors with unlinked PHCHRG tracks.

First attempt: Compare PHUXOV and PHCHRG track parameters at the outermost VXD3 hit.



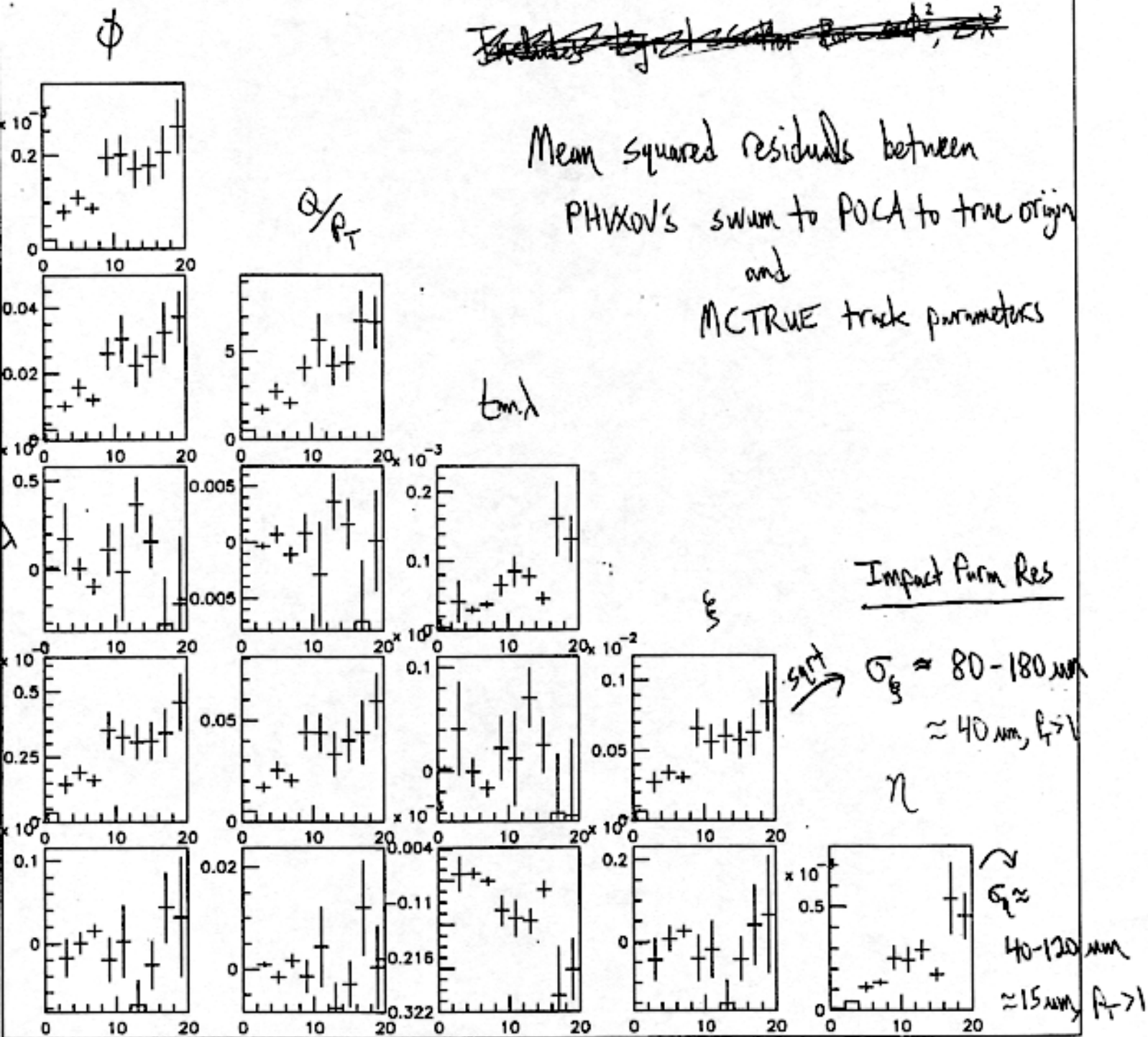
Make link if position and direction residuals are small.

Get 15% of PHUXOVs with 100% charge purity.

⇒ Increases overall  $P$  by  $\sim 2\%$ .

~~Residuals between PHOXO's sum to POCA to true origin and MCTRUE track parameters~~

Mean squared residuals between PHOXO's sum to POCA to true origin and MCTRUE track parameters



Impact Param Res

$\sigma_{\epsilon} \approx 80-180 \mu\text{m}$   
 $\approx 40 \mu\text{m}, P_T > 1$

$\eta$

$\sigma_{\eta} \approx$   
 $40-120 \mu\text{m}$   
 $\approx 15 \mu\text{m}, P_T > 1$

Correlations

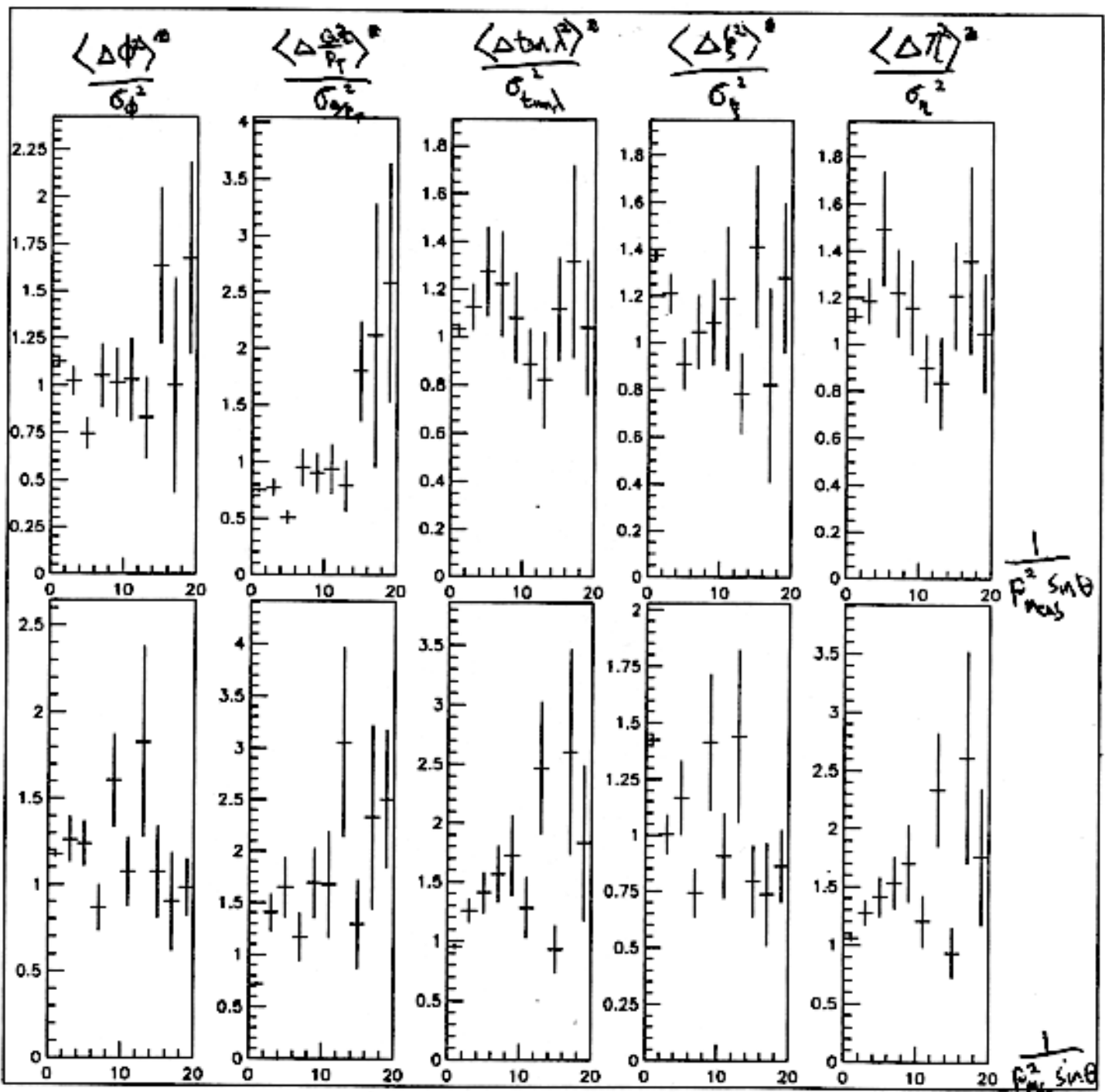
$\Delta\phi \sim s \cdot \Delta \frac{Q}{P_T}$

$s = \text{arclength}$

$\Delta\epsilon \sim s \cdot \Delta\phi \sim s \cdot \Delta\phi_0 + s^2 \Delta \frac{Q}{P_T}$

$\Delta\eta \sim s \cdot \Delta \tan \lambda$

# Normalized Mean Squared Residuals vs $\frac{1}{p^2 \sin \theta}$

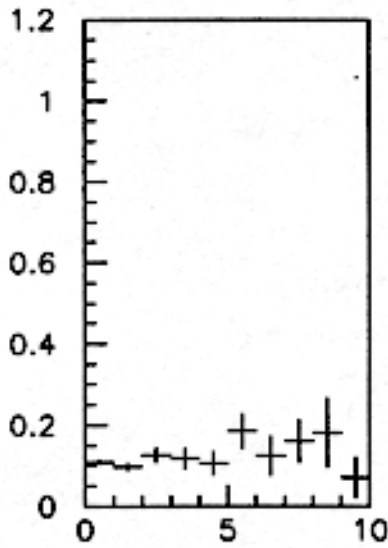


Using Ad Hoc correction to errors.

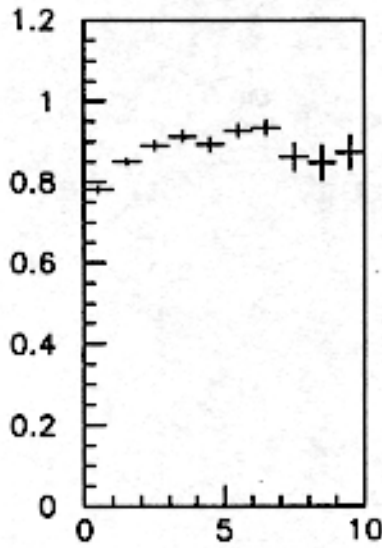
(correct initial  $\sigma_\phi, \sigma_{\frac{\partial \phi}{\partial r}}, \sigma_{\ln \lambda}$ , Let  $\sigma_\beta$  and  $\sigma_\tau$  fix themselves)

# Track Attachment

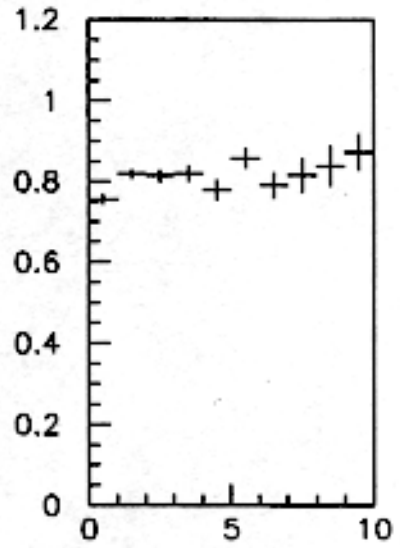
IP  $\rightarrow$  sec rate



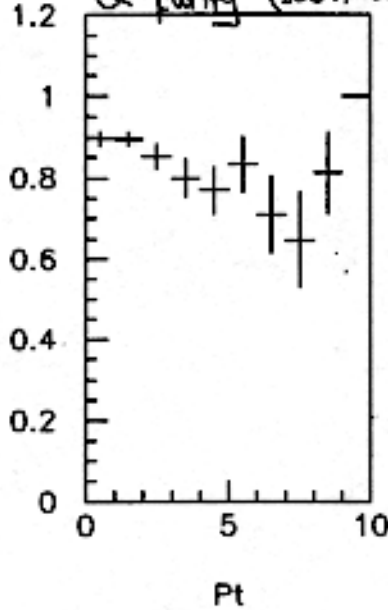
sec  $\rightarrow$  sec rate



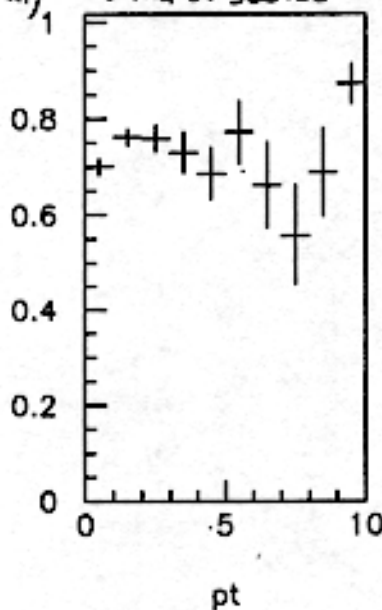
For sec  $\rightarrow$  sec fits,  
B  $\rightarrow$  B, D  $\rightarrow$  D rate



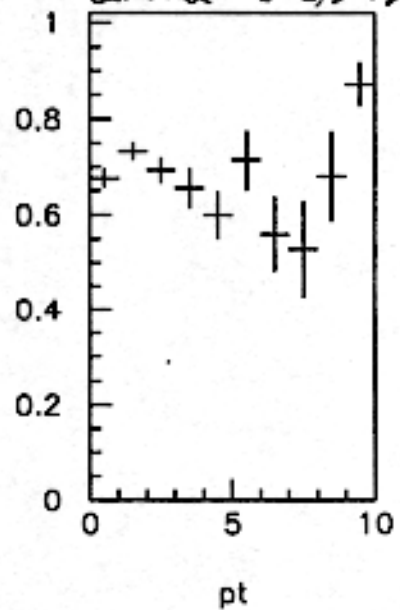
Q purity<sup>pt</sup> (sec vtx constraint)



Correct Q<sup>pt</sup> sec  $\rightarrow$  sec



Correct Q<sup>pt</sup> B  $\rightarrow$  B, D  $\rightarrow$  D



The Impact Param errors are so large that VXOVs do not often form their own new 1-prong vtx. They get absorbed into pre-existing ones.

↳ When they do, the vtx is not a good estimator of the true decay pos.

## Summary:

Next time, give me a  
longer lever arm!

- Charge measurement is understood and parameterizable
- Vertexing performance is marginal.
  - VXOVs can distinguish between pre-existing B, D vertices but are often consistent with both
  - VXOVs rarely form good new vertices.