

# **The Physics Argument for NLC Positron Polarization**

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## Motivation

Why do we need the Linear Collider?

- Discovery of new physics (if Tevatron/LHC miss it)
- High-precision measurements of SM (if Tevatron/LHC see nothing new)
- Quantifying new physics (once Tevatron/LHC find it)

Why do we need Electron Beam Polarization  $\mathcal{P}_-$ ?

- Sensitivity to chiral couplings
- Enhancing/suppressing special channels
  - Better statistics
  - Extraction of couplings (signal free from signal)
  - Background suppression

Do we also need Positron Polarization  $\mathcal{P}_+$ ?

What should be addressed for the Orange Book/Snowmass?

## $\mathcal{P}_+$ for Disentangling Susy

$$e^+e^- \rightarrow \tilde{e}_L\tilde{e}_L, \tilde{e}_R\tilde{e}_R, \tilde{e}_L\tilde{e}_R$$

s-channel  $\gamma/Z^*$

t-channel  $\tilde{\chi}^0$  exchange

*Example from Uli Martyn's LCWS2000 talk*

	$\mathcal{P}_- = -80\%$	$+\mathcal{P}_+ = 60\%$
$\tilde{e}_L\tilde{e}_L$	900 fb	1100 fb
$\tilde{e}_R\tilde{e}_L$	200 fb	100 fb
$\tilde{e}_R\tilde{e}_R$	50 fb	30 fb

$\tilde{e}_L\tilde{e}_R$  has only  $\tilde{\chi}^0$  dependence (in the absence of mixing)

Sensitivity to heavy states  $\Rightarrow$  right  $\sqrt{s}$  for NLC++

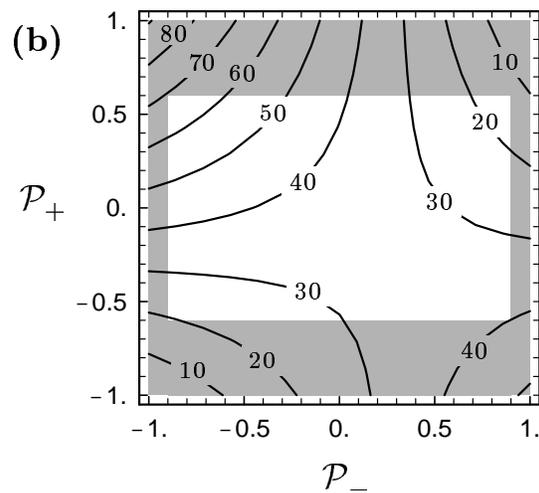
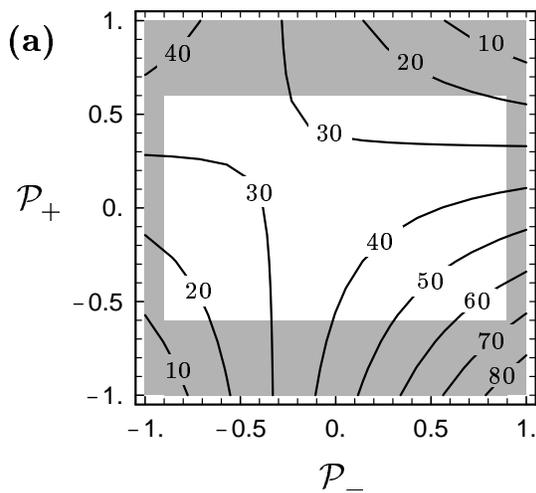
Sfermions difficult for hadron colliders except for kinematic accidents

$e^+e^- \rightarrow \tilde{t}_1\tilde{t}_1^* = (\tilde{t}_L \cos\theta_{\tilde{t}} - \tilde{t}_R \sin\theta_{\tilde{t}})(\tilde{t}_L^* \cos\theta_{\tilde{t}} - \tilde{t}_R^* \sin\theta_{\tilde{t}})$   
*Berggren, et al., hep-ph/9911345; Bartl, et al., hep-ph/0010018*

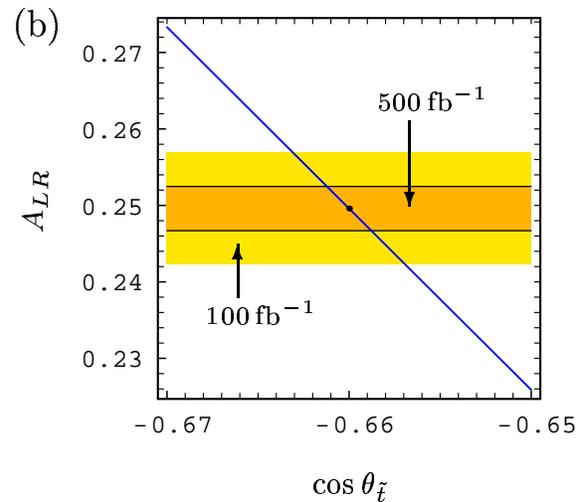
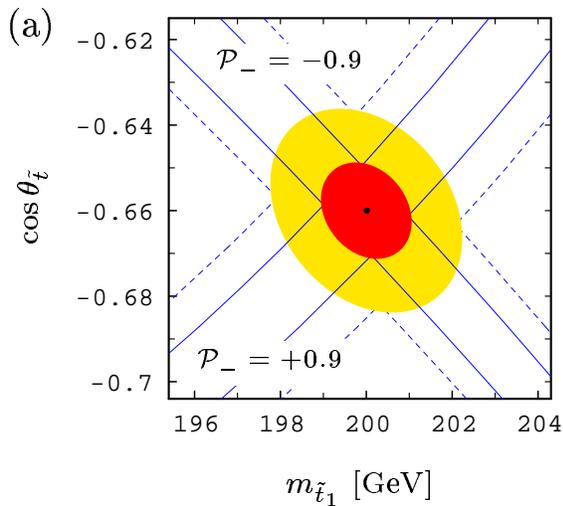
- $\sqrt{s} = 500 \text{ GeV}$ ,  $m_{\tilde{t}_1} = 200 \text{ GeV}$ ,  $\mathcal{L} = 500 \text{ fb}^{-1}$

$\cos\theta_{\tilde{t}} = 0.4$

$\cos\theta_{\tilde{t}} = 0.66$



68% CL ellipse



Increased accuracy ( $\sim 25\%$ ) in stop mass and mixing angle

$$e^+e^- \rightarrow \tilde{\chi}^-\tilde{\chi}^+$$

- Measurement of  $M_2$ ,  $\mu$ ,  $\tan\beta$ ,  $m_{\tilde{\nu}_e}$  from:

$$\sigma_R = \int d\Omega \frac{d\sigma}{d\Omega} [P_L = -\bar{P}_L = +1]$$

$$\sigma_L = \int d\Omega \frac{d\sigma}{d\Omega} [P_L = -\bar{P}_L = -1]$$

$$\sigma_T = \int d\Omega \left( \frac{\cos 2\Phi}{\pi} \right) \frac{d\sigma}{d\Omega} [P_T = \bar{P}_T = +1, \eta = \pi]$$

using  $\tilde{\chi}_1^+\tilde{\chi}_1^-$ ,  $\tilde{\chi}_1^+\tilde{\chi}_2^- + \tilde{\chi}_1^-\tilde{\chi}_2^+$ ,  $\tilde{\chi}_2^-\tilde{\chi}_2^+$

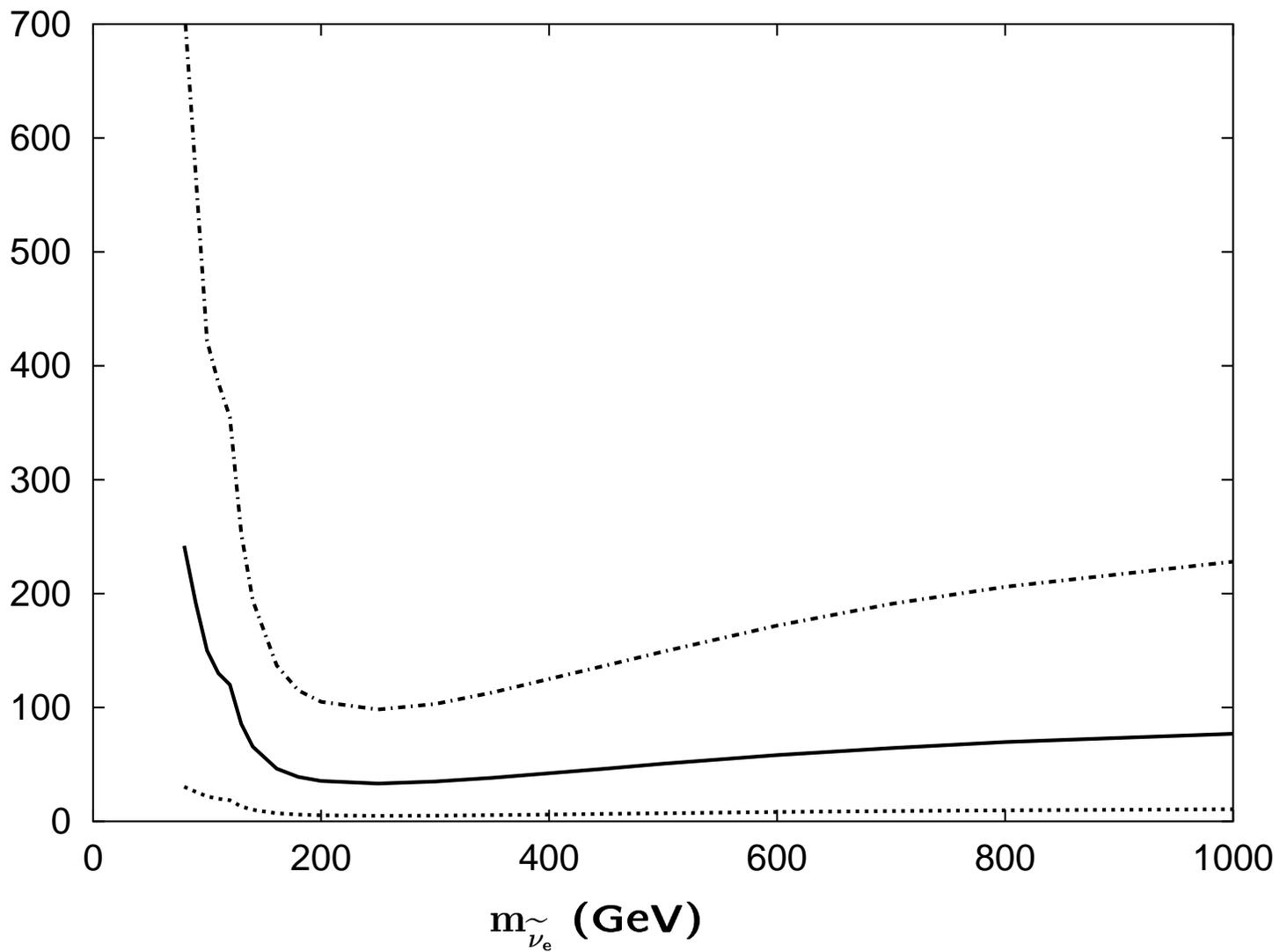
If only  $\tilde{\chi}_1^\pm$  is accessible, then  $+ m_{\tilde{\chi}^\circ} + \text{variable } \sqrt{s}$

Sensitivity to extra, charged states?

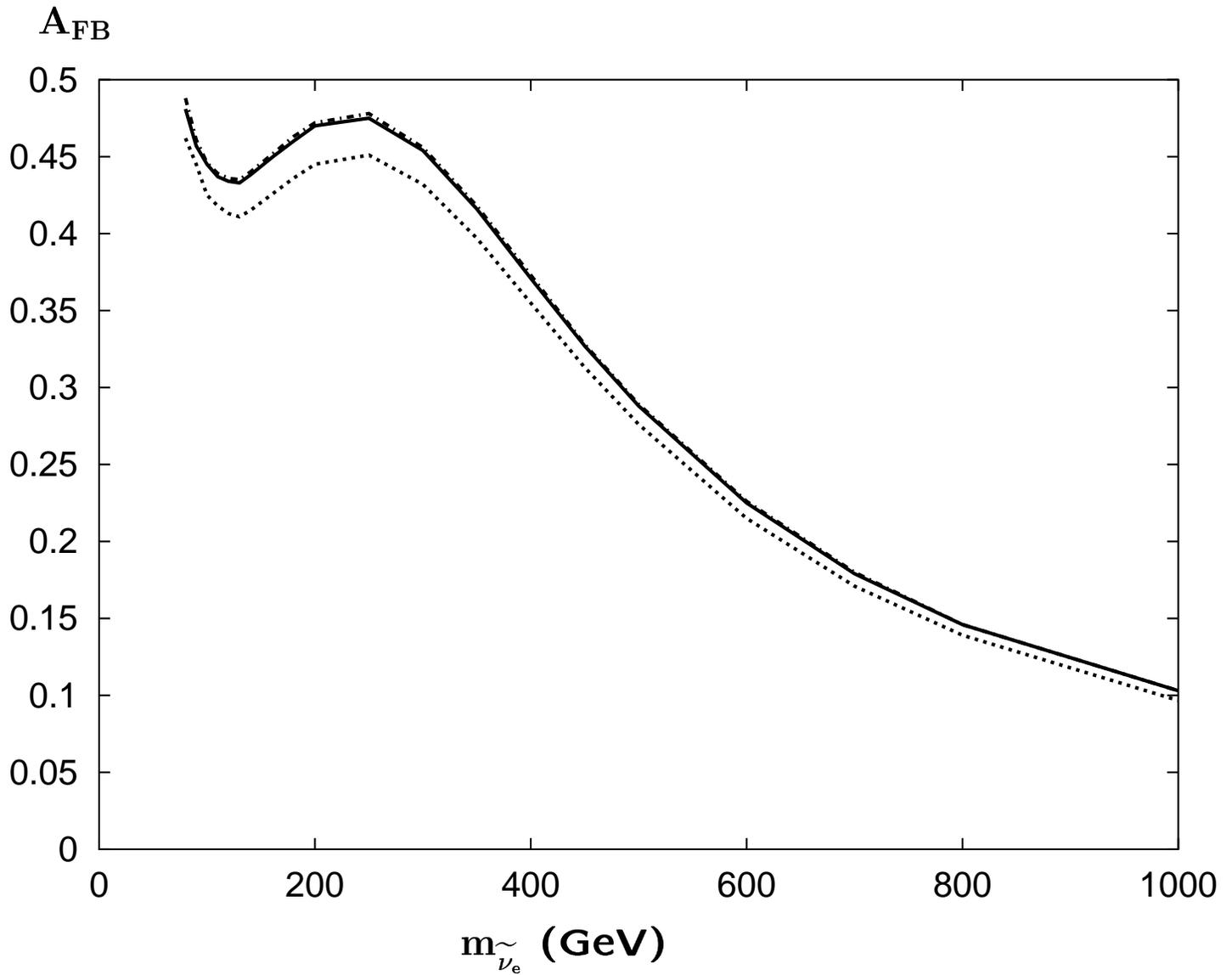
- Extraction of  $m_{\tilde{\nu}_e}$

*G. Moortgat-Pick and H. Fraas, [hep-ph/9904209]*

$$\sigma_{e^-} \equiv \sigma(\tilde{\chi}^- \tilde{\chi}^+) \times \text{BR}(\tilde{\chi}^- \rightarrow e^- + X) \text{ (fb)}$$



$(\mathcal{P}_-, \mathcal{P}_+)$   
 (0, 0)=solid, (0.85, 0)=dot, (-0.85, 0.6)=dash-dot

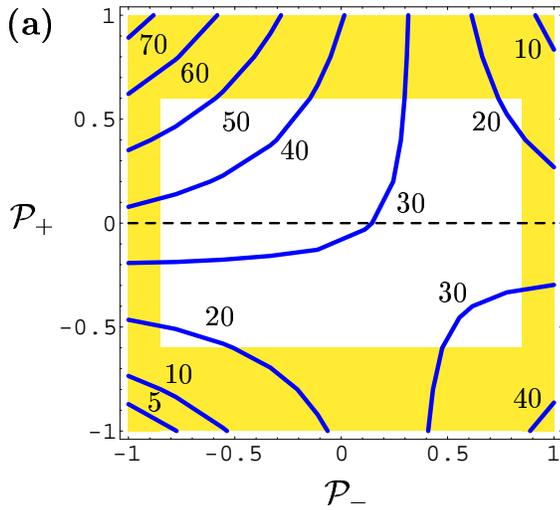


(0, 0)=solid, (0.85, 0)=dot, (-0.85, 0.6)=dash-dot

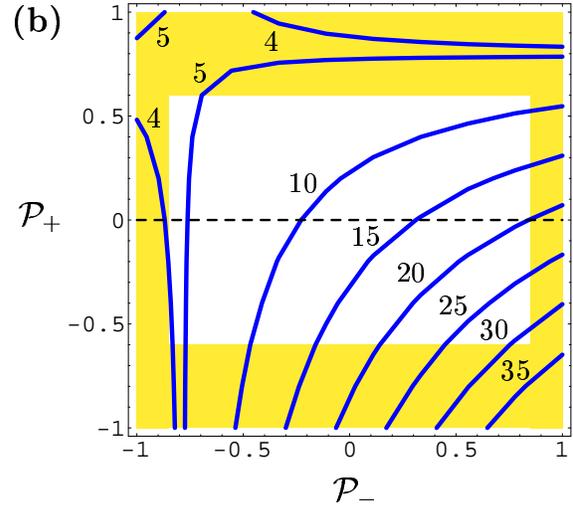
Higgsino-like models more difficult

$$e^+e^- \rightarrow \tilde{\chi}^{\circ}\tilde{\chi}^{\circ}$$

$$\sigma(e^+e^- \rightarrow \tilde{\chi}_1^{\circ}\tilde{\chi}_2^{\circ}), \sqrt{s} = 230 \text{ GeV}, m_{\tilde{\chi}_1^{\circ}} = 71 \text{ GeV}, m_{\tilde{\chi}_2^{\circ}} = 130 \text{ GeV}$$



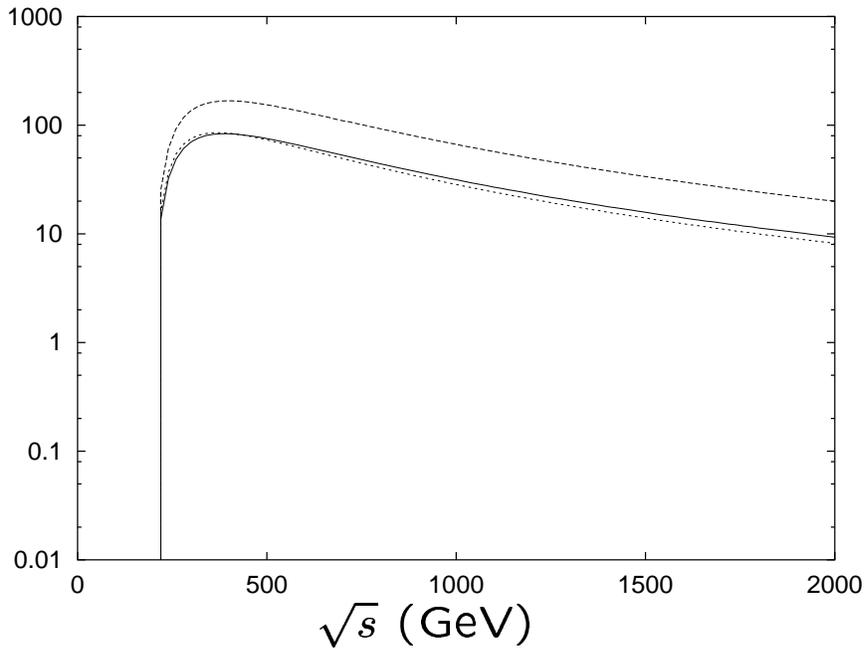
$$\tilde{e}_R, \tilde{e}_L = 132, 176 \text{ GeV}$$



$$\tilde{e}_R, \tilde{e}_L = 132, 500 \text{ GeV}$$

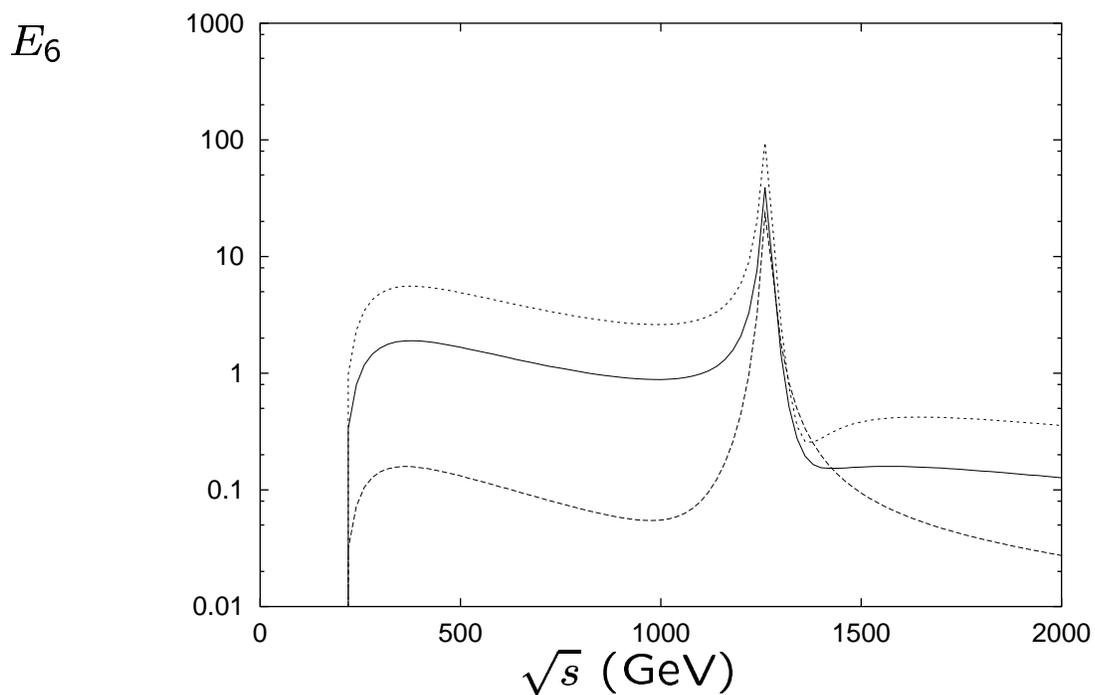
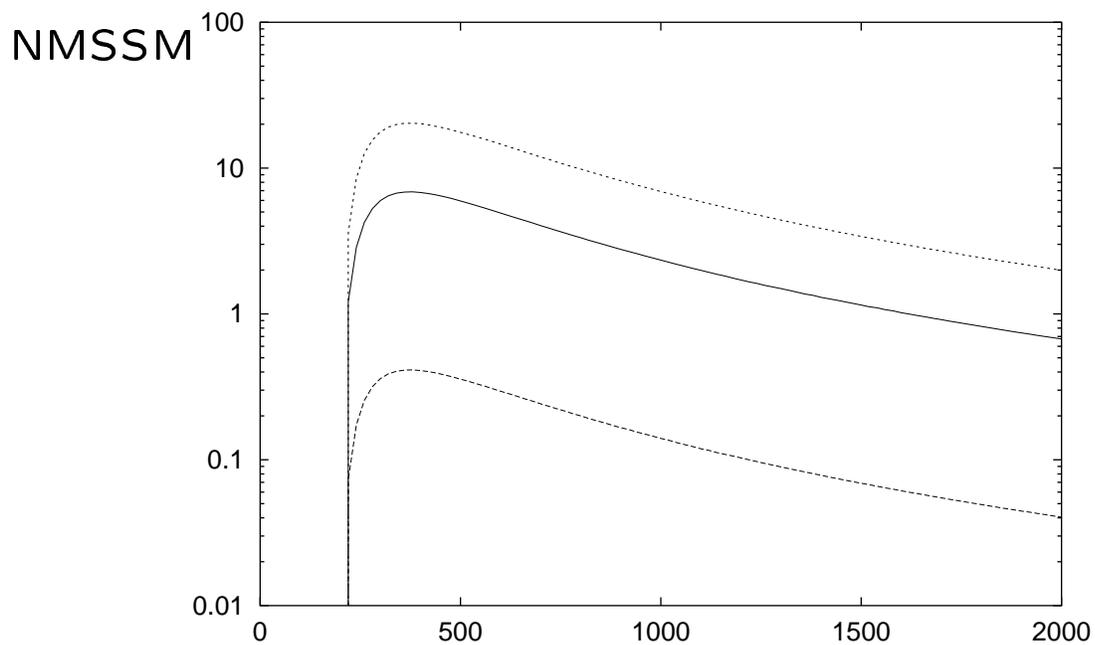
$\sigma(\tilde{\chi}_1^{\circ}\tilde{\chi}_2^{\circ})$  (fb); (00)=solid, (+-)=dot, (-+)=dash

MSSM



Extensions of the MSSM can contain Majorana fermion partners to gauge singlets – singletinos

$\sigma(\tilde{\chi}_1^0 \tilde{\chi}_2^0)$  (fb); (00)=solid, (+-) = dot, (-+) = dash



## Contact Interactions

- Compositeness (ETC)
- Heavy  $Z'$
- Leptoquarks

$$\mathcal{L}_{\text{contact}} = \frac{\tilde{g}^2}{\Lambda_{\alpha\beta}} \eta_{\alpha\beta} (\bar{e}_\alpha \gamma_\mu e_\alpha) (\bar{f}_\beta \gamma_\mu f_\beta), f \neq e, t$$

$$\frac{d\sigma}{d\cos\theta} = \frac{3}{8} [(1 + \cos\theta)^2 \sigma_+ (1 - \cos\theta)^2 \sigma_-]$$

$$\sigma_+ = \frac{D}{4} [(1 - P_{\text{eff}}) \sigma_{LL} + (1 + P_{\text{eff}}) \sigma_{RR}]$$

$$\sigma_- = \frac{D}{4} [(1 - P_{\text{eff}}) \sigma_{LR} + (1 + P_{\text{eff}}) \sigma_{RL}]$$

$$D = 1 - \mathcal{P}_+ \mathcal{P}_-, P_{\text{eff}} = \frac{\mathcal{P}_- - \mathcal{P}_+}{1 - \mathcal{P}_- \mathcal{P}_+}$$

Extract components by varying  $P_{\text{eff}} = \pm P$ :

$$\sigma_{LL} = \frac{1}{D} \left[ -\frac{1-P}{P} \sigma_+(P) + \frac{1+P}{P} \sigma_+(-P) \right], \text{etc.}$$

Reach on  $\Lambda_{\alpha\beta}$  increased by 20 – 40%.

## Standard-Model Like Higgs Boson

$\sigma(e^+e^- \rightarrow ZH)$			
$\propto (1 + \mathcal{P}_-)(1 - \mathcal{P}_+).58 + (1 - \mathcal{P}_-)(1 + \mathcal{P}_+).42$			
$\mathcal{P}_-$	$\mathcal{P}_+$	100% Pol.	80% $e^-$ , 60% $e^+$
0	0	1	1
+1	0	0.84	0.87
-1	0	1.16	1.13
+1	-1	1.68	1.26
-1	+1	2.32	1.70

$\sigma(e^+e^- \rightarrow \nu\bar{\nu}H) \sim \sigma(e^+e^- \rightarrow W^+W^-)$			
$\propto (1 + \mathcal{P}_-)(1 - \mathcal{P}_+)$			
$\mathcal{P}_-$	$\mathcal{P}_+$	100% Pol.	80% $e^-$ , 60% $e^+$
0	0	1	1
+1	0	0	0.2
-1	0	2	1.8
+1	-1	0	0.08
-1	+1	4	2.88

$\sigma(e^+e^- \rightarrow ZZ)$			
$\propto (1 + \mathcal{P}_-)(1 - \mathcal{P}_+).655 + (1 - \mathcal{P}_-)(1 + \mathcal{P}_+).345$			
$\mathcal{P}_-$	$\mathcal{P}_+$	100% Pol.	80% $e^-$ , 60% $e^+$
0	0	1	1
+1	0	0.69	0.75
-1	0	1.31	1.25
+1	-1	1.37	1.05
-1	+1	2.62	1.91

- Improve  $S/B$
- Dial off  $WW$ -fusion

## Excited Leptons

*Eboli, et al., hep-ph/9509257*

With Polarization:

- Determine if  $S = 1/2, 3/2$
- Study  $\gamma$  couplings
- $e^- \gamma$  is superior in sensitivity

## Anomalous Top Quark couplings

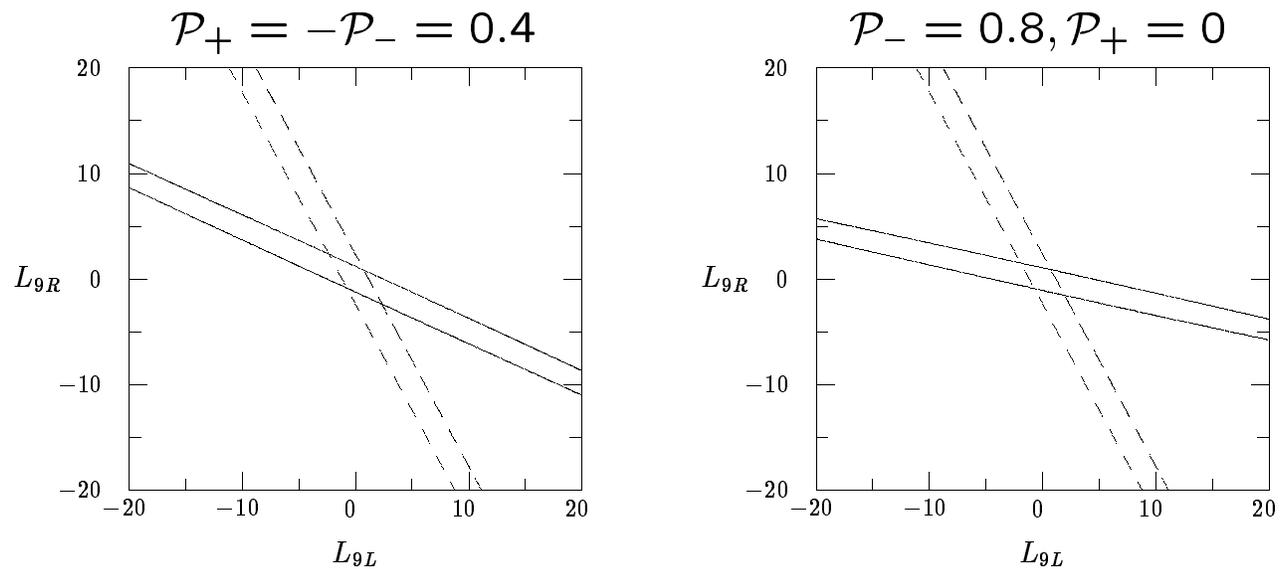
*Hioki, hep-ph/9908345*

- Consider  $e^+e^- \rightarrow t\bar{t} \rightarrow l^\pm + X, l^+l^- + X$
- Assume  $\delta g_{t\bar{t}\gamma, Z} \sim 0.1$
- $\mathcal{P}_+ \neq 0$  improves sensitivity from  $2\sigma \rightarrow 3\sigma$

$$e^+e^- \rightarrow W^+W^-$$

Likhoded, Han, Valencia, *Phys. Rev. D* **53**, 4811 (1996)

- No-Higgs EW Chiral Lagrangian

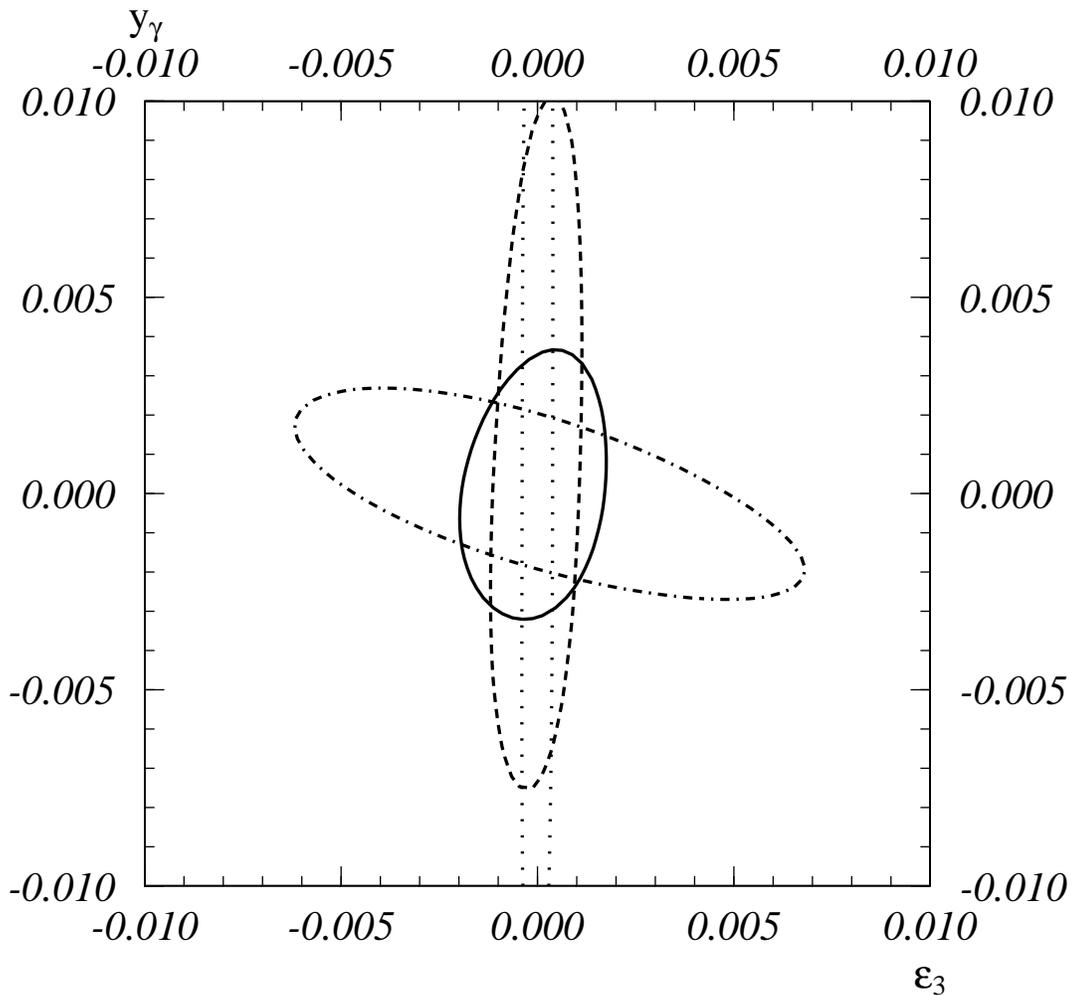


Allowed region for the  $L_{9L} - L_{9R}$  parameters at  $\hat{\alpha} = 0$  for cuts on the scattering angle  $-0.989 \leq \cos \theta \leq 0.4$  for beam polarizations (dashed contour represents the unpolarized case)

Casalbuoni, De Curtis, Guetta, hep-ph/9912377

- One Example:  $\gamma WW$ ,  $ZWW$  effective Lagrangian with global  $SU(2)_L$  symmetry

$$\mathcal{L}_{eff} = ie \frac{y_\gamma}{M_W^2} [A, W, W] + e\epsilon_3 \left( \frac{t_\theta}{c_{2\theta}} \bar{f} Z f - \frac{s_\theta}{c_{2\theta} 2\sqrt{2}} \bar{f} W f' \right)$$



90% CL bounds,  $\sqrt{s} = 500$  GeV,  $\mathcal{L} = 300$  fb $^{-1}$

(0.9, 0.6)=dash, (0.9, -0.6)=dot,  
(-0.9, 0.6)=dash-dot, (0, 0)=solid

## GIGA-Z

# ***$A_{LR}$ with Positron Polarization (Comment)***

JLC Group

**Keisuke Fujii, KEK**  
*in place of*  
**Tsunehiko Omori, KEK**

*This is to call your attention to the usefulness of positron polarization in reducing the systematic error on  $A_{LR}$  as described in our old note: KEK Preprint 95-127*

### **Combined Polarization**

$$P_{comb} \equiv \frac{P_- - P_+}{1 - P_- P_+}$$

*right-handed helicity basis:  
 $P=-1$  means 100% left-handed*

### **$A_{LR}$**

$$A_{obs} \equiv \frac{N_L - N_R}{N_L + N_R} = -P_{comb} A_{LR}$$

$$\frac{\Delta A_{LR}}{A_{LR}} \simeq \sqrt{\left(\frac{\Delta P_{comb}}{P_{comb}}\right)^2 + \frac{1}{N (P_{comb} A_{LR})^2}}$$

**Systematic Error on  $P_{comb}$  dominates if  $N \gg 1$**

# $A_{LR}$ with Positron Polarization (Comment)

JLC Group

## Reduction of Systematic Error

Polarization measurement will be dominated by systematic error

$$\Delta P_{comb} = \left( \frac{\partial P_{comb}}{\partial P_-} \right) \left( \frac{\Delta P_-}{P_-} \right) P_- + \left( \frac{\partial P_{comb}}{\partial P_+} \right) \left( \frac{\Delta P_+}{P_+} \right) P_+$$

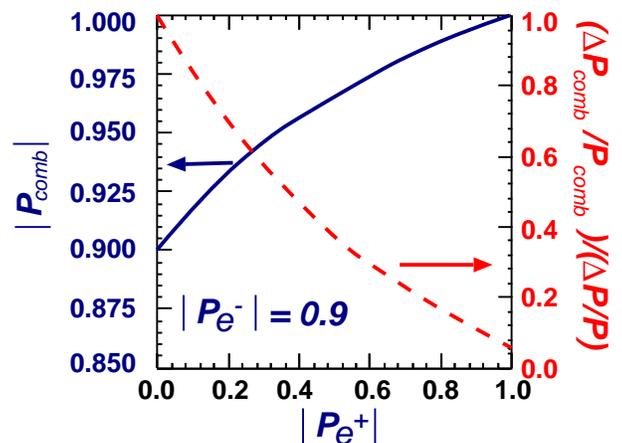
Linear Error Propagation

Identical apparatuses will be used for both electrons and positrons

$$\frac{\Delta P_-}{P_-} = \frac{\Delta P_+}{P_+} \equiv \frac{\Delta P_{\pm}}{P_{\pm}}$$

$$\frac{\Delta P_{comb}}{P_{comb}} = \frac{1 + P_- P_+}{1 - P_- P_+} \left( \frac{\Delta P_{\pm}}{P_{\pm}} \right)$$

Significant reduction of systematic error already at  $P_{e^+} = 0.5$



## TeV String Effects

*Peskin, Perelstein, Cullen, Phys.Rev.D62:055012(2000)*

- Multiply SM amplitudes by Veneziano amplitudes
- Factorize into resonances near string scale  $M_S$

$$\begin{aligned} \mathcal{A}(\gamma_R \gamma_R \rightarrow \gamma_{01}^*) &= \sqrt{2} e M_S & \mathcal{A}(\gamma_L \gamma_L \rightarrow \gamma_{02}^*) &= \sqrt{2} e M_S \\ \mathcal{A}(e_R^- e_R^+ \rightarrow \gamma_{03}^*) &= \sqrt{2} e M_S & \mathcal{A}(e_L^- e_L^+ \rightarrow \gamma_{04}^*) &= \sqrt{2} e M_S \end{aligned}$$

$$\begin{aligned} \mathcal{A}(e_R^- e_L^+ \rightarrow \gamma_1^*) &= \sqrt{\frac{3}{2}} e M_S \epsilon_+^\mu & \mathcal{A}(e_L^- e_R^+ \rightarrow \gamma_1^*) &= \sqrt{\frac{3}{2}} e M_S \epsilon_-^\mu \\ \mathcal{A}(e_L^- e_R^+ \rightarrow \gamma_2^*) &= \sqrt{\frac{1}{2}} e M_S \cdot \frac{1}{\sqrt{2}} [\epsilon_-^\mu \epsilon_0^\nu + \epsilon_-^\nu \epsilon_0^\mu] \\ \mathcal{A}(e_R^- e_L^+ \rightarrow \gamma_2^*) &= \sqrt{\frac{1}{2}} e M_S \cdot \frac{1}{\sqrt{2}} [\epsilon_+^\mu \epsilon_0^\nu + \epsilon_+^\nu \epsilon_0^\mu] \\ \mathcal{A}(\gamma_L \gamma_R \rightarrow \gamma_2^*) &= \sqrt{2} e M_S \epsilon_-^\mu \epsilon_-^\nu \end{aligned}$$

- Want  $\mathcal{P}_+$  (or  $\gamma\gamma$ ) to study spin-0 resonances?

## Final Thoughts (Questions)

- $\mathcal{P}_+$  is useful, but is it indispensable?  
Is there a No-Lose argument that requires  $\mathcal{P}_+$ ?
- If  $\mathcal{P}_- = \pm 1$  is not realistic, does  $\mathcal{P}_+$  help?  
What minimal  $\mathcal{P}_+$  with what  $\delta\mathcal{P}_+$ ?
- Is background suppression, signal enhancement enough?  
Reduction of systematic errors?
- What  $\mathcal{L}$  for  $\mathcal{P}_+ = 0$  versus  $\mathcal{P}_+ \neq 0$  to make the same measurement?
- Will signals be more confusing than we suspect?  
Better safe than sorry?
- Does it make sense to concentrate on SUSY?
- Is it intellectually interesting only to set better limits?
- What are the minimal requirements for the NLC to make scientific progress?  
Save  $\mathcal{P}_+$  for the NLC++?